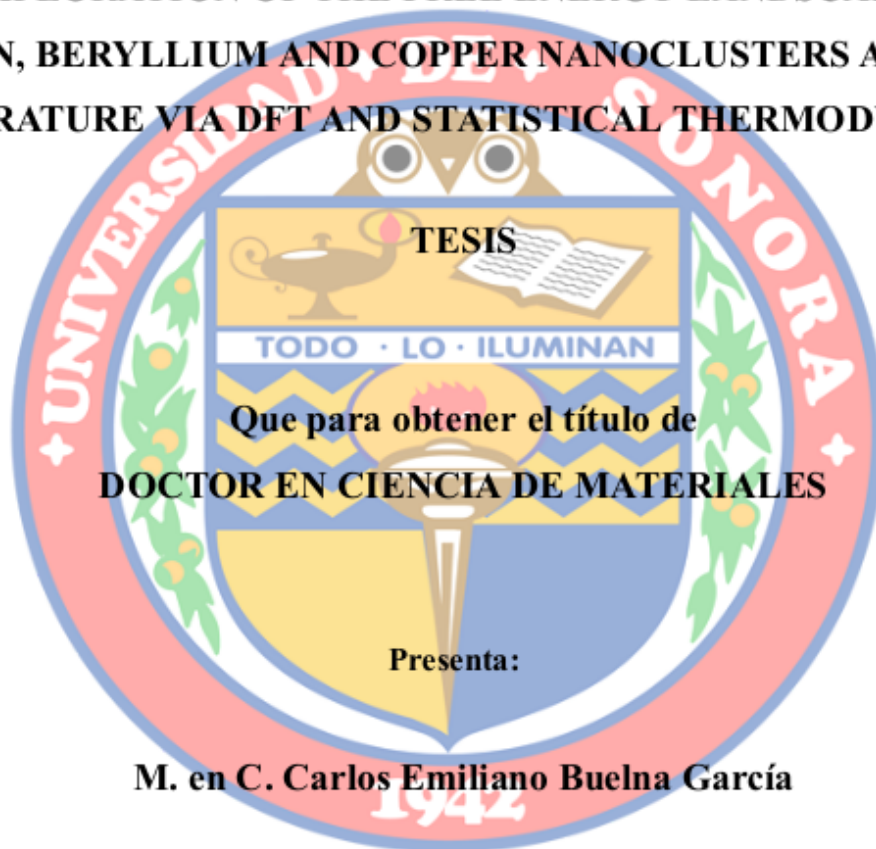


# UNIVERSIDAD DE SONORA

## DIVISIÓN DE INGENIERÍA

DEPARTAMENTO DE INVESTIGACIÓN EN POLÍMEROS Y MATERIALES

**“EXPLORATION OF THE FREE ENERGY LANDSCAPES OF  
BORON, BERYLLIUM AND COPPER NANOCCLUSERS AT FINITE  
TEMPERATURE VIA DFT AND STATISTICAL THERMODYNAMICS”**



**Que para obtener el título de  
DOCTOR EN CIENCIA DE MATERIALES**

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**Hermosillo, Sonora. 22 de Febrero del 2023**

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hará mi grandeza"**



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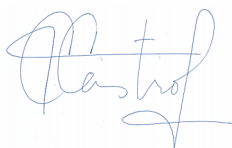


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Hermosillo, Sonora, february 22, 2023.

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## Declaration of Authorship

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I declare this thesis entitled: *Exploration of the free energy landscapes of boron, beryllium and copper nanoclusters at finite temperature via DFT and statistical thermodynamics* is a work of my own authority, which has been done to defend of my Doctoral work at the *Universidad de Sonora*. This work was made under the guidance of Dr. Jesús Manuel Quiroz-Castillo of the *Universidad de Sonora* and Dr. José Luis Cabellos-Quiroz of the *Universidad Politécnica de Tapachula*.

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## Dedication

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*I dedicate this work to my parents.*

---



# Acknowledgments

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Thanks to all **my friends and colleagues**

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## Abstract

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Clusters are aggregates of atoms that are too large to be called molecules and too small to resemble crystal fragments and their properties are highly dependent on structure, size, composition, and temperature; however, most theoretical studies of density functional assume that the temperature is 0 K and neglect temperature-dependent contributions as their finite-temperature properties remain virtually unexplored. Experimental studies are carried out at temperatures higher than 0 K, and it is necessary to understand the effect of temperature on the properties of the cluster and also on the determination of the lowest energetic structure at finite temperature. In this doctoral thesis, we conducted a theoretical-computational study at finite temperature of the structural, thermochemical, and electronic properties of atomic nanoclusters formed by elements of Boron, Beryllium and Copper using density functional theory and statistical thermodynamics. The knowledge of the minimum energy geometries and the most energetically unstable isomers are essential in calculating electronic, and geometric properties, which consequently provide a complete vision of the molecular system. The starting point for understanding the properties of the cluster is the putative global minimum and all lower energy structures near it; locating those low-energy structures is only the first difficult step. Combined DFT with statistical thermodynamics, we roughly calculated the relative thermal populations highly dependent on temperature and the effect of temperature on IR spectra. To elucidate the lowest energy structure and their neighbors, we conducted an extensive and systematic global exploration of potential/free energy landscapes to locate the low-energy structures of clusters formed by B, Be, and Cu atoms. To achieve what was mentioned above, we employed a hybrid genetic algorithm, developed and implemented by our research group, written in *Python* and coupled to any electronic structure program available; Also, we developed the computational codes necessary for calculating the thermochemical properties.

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## Resumen

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Los cúmulos son agregados de átomos que son demasiado grandes para llamarse moléculas y demasiado pequeños para parecerse a fragmentos de cristal, y sus propiedades dependen en gran medida de la estructura, el tamaño, la composición y la temperatura; sin embargo, la mayoría de los estudios teóricos del funcional de densidad asumen que la temperatura es 0 K y desprecian las contribuciones dependientes de la temperatura, como consecuencia sus propiedades a temperatura finita permanecen prácticamente sin explorar. Considerando que los estudios experimentales se llevan a cabo a temperaturas finitas, desde el punto de vista teórico, es necesario comprender el efecto de la temperatura sobre las propiedades del cúmulo y también sobre la determinación de la estructura energética más baja a temperatura finita. En esta tesis doctoral realizamos un estudio teórico-computacional a temperatura finita de las propiedades estructurales, termoquímicas y electrónicas de nanoclusters atómicos formados por elementos de Boro, Berilio y Cobre utilizando la teoría funcional de la densidad y la termodinámica estadística. El conocimiento de las geometrías de mínima energía y de los isómeros energéticamente más inestables es fundamental para el cálculo de las propiedades electrónicas y geométricas, que en consecuencia proporcionan una visión completa del sistema molecular. El punto de partida para comprender las propiedades del cúmulo es el mínimo global putativo y todas las estructuras de menor energía cercanas; ubicar esas estructuras de baja energía es solo el primer paso difícil. Combinando DFT con termodinámica estadística, calculamos aproximadamente las poblaciones térmicas relativas altamente dependientes de la temperatura y el efecto de la temperatura en los espectros IR. Para dilucidar la estructura de energía más baja y sus vecinos, llevamos a cabo una exploración global extensa y sistemática de los paisajes de energía libre/potencial para ubicar las estructuras de baja energía de los grupos formados por átomos de B, Be y Cu. Para lograr lo mencionado anteriormente, empleamos un algoritmo genético híbrido, desarrollado e implementado por nuestro grupo de investigación, escrito en *Python* y acoplado a cualquier programa de estructura electrónica disponible; Además, desarrollamos los códigos computacionales necesarios para el cálculo de las propiedades termoquímicas.

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# Introduction

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## 1.1 Introduction

The first step in understanding the molecular properties is elucidating the lowest energy structure and its isomers. The minimum energy structure, the distribution of its isomers, as well as its properties depend to a great extent on the temperature, and with the aim to compute the molecular properties of atomic clusters considering the temperature, it is necessary to consider statistical mechanics. Additionally, the cluster properties depend on the structure, size, and composition, and as mentioned earlier, the temperature plays an important role; however, most theoretical density functional studies assume that temperature is 0 K and their finite temperature properties remain virtually unexplored. On the other hand, experimental studies are carried out in non-zero temperatures, and it is necessary to understand the effect of the temperature on the cluster properties and the determination of the lowest energy structure at finite temperatures.

In this doctoral thesis, we employed density functional theory and statistics thermochemistry to elucidate the effects of the temperature on the determination of the lowest energy structure and its isomers on the potential/free energy surface and the importance of the contribution of the higher energy structures to the IR spectrum. These contributions are taken into account through weight's Boltzmann factors dependents on temperature and show that these high energy geometries are determinants in the IR and UV spectra, inducing changes in the spectrum's shape and amplitudes. In order to take into account these contributions, a couple of things were considered: first, An extensive and systematic search of the lowest energy structures was performed on the potential/free energy surfaces of atomic clusters, using an unbiased hybrid search algorithm coupled to density functional theory (DFT) based on kicking and basing genetic methodologies. Second, the temperature effects on the populations were taken into account through thermochemical properties. As a result, we present how the effect of the temperature is taken into account through the contributions of higher energy structures. As far as we know, for atomic clusters a) no work has attempted to investigate entropy-driven isomers distribution employing b) the effect of the temperature on the IR spectroscopy. To explore the basis set dependence of the optimized geometries, isomers distribution, and computed IR spectrum, we used a basis set Def2tzvp. The starting point requires searching the global minimum on the potential and free energy surfaces. This is a complicated task due to several factors. The degree of difficulty increases with the number of atoms; the calculation of energy requires quantum mechanical energy methodology

to produce a realistic energy value. Furthermore, the number of initial structures should be large enough to ensure that we are not missing structures making an incomplete sampling of the configurational space introducing a major problem in the computation of the thermodynamic properties. Although the problem of searching for global minimum in molecular systems is challenging, the design and use of algorithms dedicated to the search for global minima, such as simulated annealing, genetic algorithms [1, 2, 3], as Gradient Embedded Genetic Algorithm (GEGA), basin hopping, Monte Carlo, particle swarm optimization, graph theory, or the big bang search algorithm, has been made over the years and they have lead us to solve, in a targeted way, the minimum global search. The simplest and easiest way for searching global minimum consist in generating structures with random atomic positions within a finite box, which will be optimized using any quantum mechanical program. The kick method has been used extensively until nowadays; one of the emerging kick methods was used by Saunders in 1987 at the global minimum search of the cycloheptane molecule, and several years later used a complete automated kick procedure in small carbon molecules, imposing some restrictions to the starting point structures, coupled to Density Functional Theory (DFT) methods to find their global minimum. Many works have employed this technique or some variants in several systems, to find the global minimum. Although the search of the global and local minima is helpful in understanding reactivities and catalytic efficiencies, such studies often neglect temperature-dependent entropic contributions to free energy when increasing temperature. And has been done in sodium clusters. Temperature into account requires dealing with the thermodynamics of small systems, the thermodynamics of clusters have been studied by a variety of theoretical and simulation tools, these include Monte Carlo and molecular-dynamics simulations and analytic methods. This contributions can be computed within the so called harmonic superposition approximation or superposition method, this method originally developed for thermodynamics observable only, was improved phonologically by including anharmonic corrections, and extended to others cluster properties. In this approach the partition function is written as a sum over all the minimum on the potential energy surface, and by restricting the sum to a certain subset of the minimal the thermodynamic properties can be obtained. The solid-solid transition occurs when the partition function of two competing structures types area equal means that there are simultaneous coexistence of structural isomers at T, (the T<sub>ss</sub> computation can be obtained by parallel tempering) The structure corresponding to the global minimum ceases to be the most likely at high T so other structure prevail, As second step for understanding cluster properties relies on their spectroscopy, spectroscopy gives insight into structure and it was proposed as a way of detecting structural transformations into clusters. The influence of temperature on the spectroscopy has been computed before for a variety of clusters, for instance, such in the present study, we will use the statistical formulation of thermodynamics to compute thermodynamics properties and evaluate the relative populations among the isomers and the effects on IR spectra. As far as we know, this has not been carried out. In the present doctoral thesis a systematic unbiased search for the lowest energy structures of cluster.

We discuss the influence (or effects) of temperature on the Cu, Be, and B structures, thus the Gibbs energy of the isomers are evaluated statistical mechanically at every degree from 5 to 1500 K, relative populations, dependents of temperature, are computed based on the Boltzmann distribution using the Gibbs free energy also we investigate the effects of temperature on the IR spectrums. Features of the spectrum could be seen to originate from the competition among several clusters.

### 1.1.1 General objective

The general objective of this thesis is the development of a computational-theoretical study based on density functional theory and thermochemistry that considers the temperature effect on the computation of molecular properties of atomic clusters formed by Be, B, and Cu atoms.

### 1.1.2 Specific objectives

1. Implementation of the code *galgoYaqui* for the search of structures of minimum energy of atomic clusters based on *Darwinian* theory, written in *Python*, coupled with *Gaussian 09* and running on a parallel machine.
2. Exploration of free energy landscapes to search the putative global minima and the most energetically important isomers in atomic clusters, using the code *galgoYaqui*, and formed by atoms from group Be, B, and Cu atoms.
3. Implementation of the *termoYaqui* code for the inclusion of temperature effects in the calculation of atomic properties.
4. Exploration of free energy landscapes and thermal computation of  $\text{Be}_6\text{B}_{11}^{-1}$  cluster.
5. Exploration of free energy landscapes and thermal computation of  $\text{Be}_4\text{B}_8$  cluster.
6. Exploration of free energy landscapes and thermal computation of  $\text{Cu}_{13}$  cluster.
7. Exploration of free energy landscapes and thermal computation of  $\text{Cu}_{38}$  cluster.

### 1.1.3 Justification

Experimental studies are carried out at temperatures higher than 0 K; therefore, at a theoretical level, it is necessary to understand what is the effect of temperature on the properties of the cluster, and no less important is that the temperature is essential in achieving the activation energy needed to perform a chemical reaction. Taking temperature into account in the calculations of atomic and molecular clusters properties is a novel and cutting-edge topic, given that its inclusion makes

the theoretical-computational results have the best agreement with experimental measurements. Currently, these methods are being developed and used in international research groups such as *Truhlar Research Group*, the group of Prof. **Kieron Burke**, and Cabellos's group. The inclusion of temperature requires dealing with the thermodynamics of nanoscopic systems or nanothermodynamics. Emphasizing low-energy structures and temperature plays a preponderant role in determining molecular properties. The calculations, the research topic, and the developed methodologies are original and cutting-edge. All the computer codes were developed and implemented during this doctoral thesis development. This doctoral thesis generates scientific knowledge on the fascinating subject of nanothermodynamics and highlights the importance of temperature in chemistry at theoretical level.

#### 1.1.4 High temperature

The experimental studies are carried out in non-zero temperatures, and temperature is one of the parameters that can be manipulated (at a practical level) to observe novel reactions that do not occur at low temperatures. In accordance with Margrave *et al.* [4], *New molecules will be discovered and new theories required to explain events from 1000 to 1,000,000 K*. The term high temperature in chemistry refers to chemical phenomena which occur at temperatures of 1000 K and higher [4], volcanoes, lightning, and the sun and stars are examples of natural high-temperature sources where chemistry reactions happen in the range of hundreds to millions degrees of temperature. As temperature increases, chemical reactions are faster, and the chemical behavior differs from that found at room and cold temperatures. Dicyanoacetylene, a compound with chemical formula  $C_4N_2$  burns with a flame at a temperature of 5260 K [5]. In this thesis, the computed thermal probabilities for low and medium, or below the melting point temperatures of Cu, Be, and B atomic clusters, can be reasonably described with a harmonic approximation. When the temperature increases enough, melted material may be present instead of a solid and the theory needs to be validated at hot temperatures. We must consider the anharmonic terms to describe the vibrations at high energies correctly. In this thesis, for the mentioned above, we consider temperatures around or below the melting point to capture the system's thermal behavior at high temperatures.

#### 1.1.5 Organization of the thesis

The thesis is structured in seven parts as follows:

- Chapter 1, introduction and objectives.
- Chapter 2, the theory and methodology.
- Chapter 3, study of the  $Be_6B_{11}^{-1}$  cluster.
- Chapter 4, study of the  $Be_4B_8$  cluster.
- Chapter 5, study of the  $Cu_{13}$  cluster.

- Chapter 6, study of the  $\text{Cu}_{38}$  cluster.
- Chapter 7, conclusions and future work.



# Theory and methodology

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## 2.1 Density functional theory

In the last 30 years the *Density Functional Theory*, is one of the most active topics in the area of materials science, chemistry and physics [6]. For reference point, the most notable article on DFT has been cited 128902 times [7] (18/12/2022), and one of the most cited scientists is *John P. Perdew* [7, 6]. The DFT applied in atoms, molecules and solids, is a variational procedure that solves the non-relativistic time-independent Schrödinger Equation 2.1, considering many electrons and implemented in numerical methods and algorithms written in programming code, usually in *FORTRAN*.

$$\left[ -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} + V(x) \right] \Psi(x) = E\Psi(x), \quad (2.1)$$

In Eq. 2.1,  $\hbar$  is the reduced *Planck* constant,  $m$  is the mass of the electron,  $V(x)$  is the external potential,  $E$  the *eigen*-energies and  $\Psi(x)$  is the wave function associated to the state in which the system is located and contains all the information of the properties of it. The Hydrogen atom, a system with one electron, is one of the cases in which the solution of the Schrödinger equation has an analytical solution, (the free particle is another) for multi-electron atoms the Schrödinger equation has no solution with analytics, in the latter case finding the solutions is elaborate [8, 9]. Consequently, and in order to find a solution, DFT and/or other methods are used. The fundamental idea of DFT lies in the minimization of the total energy of the system with respect to the electron density of the ground state, instead of using the wave function. The DFT is a theory that adequately describes the properties of the ground state and its main advantage over methods that use the wave function is that the electron density depends only on the space coordinates  $x, y, z$ , contrary to the wave function, which has a large number of parameters. The first DFT was proposed by *Thomas* and *Fermi* [10, 11] in 1928, originally the model was proposed to study multielectron atoms. The foundations underlying modern DFT were published by *Peter Hohenberg* and *Walter Kohn* in their 1964 article [12], where they established that the energy is a functional of the density, that is to say, the energy is a function of the density and this is a function of the geometric coordinates, a function of functions. In their article[12] *Peter Hohenberg* and *Walter Kohn* showed that energy is a functional of electron density establishing the equation:

$$E[\rho] = E_{xc}[\rho] + \int \rho(\mathbf{r})v(\mathbf{r})d\mathbf{r} \quad (2.2)$$



where  $E_{xc}[\rho]$  is the functional that contains the kinetic energy and the energy due to the interaction electron-electron. The problem with DFT is that the exact form of the functional  $E_{xc}[\rho]$  is not known. They also established that the electron density that minimizes the energy functional is the density of the ground state, the energy evaluated at that density is the energy of the ground state. In 1965 *Walter Kohn* and *Lu Jeu Sham* in their article[13] proposed the term correlation and exchange which includes the contributions of dynamic electronic correlation and the unknowns, which are not considered in the DFT. The resulting equations are known as *Kohn-Sham equations* and are the ones that are implemented, using different strategies in a variety of electronic structure codes. For the development of the thesis, we employed the DFT as it is implemented in the electronic structure code *Gaussian G09* [14] for the minimization of molecules.

## 2.2 Theoretical methods and computational details

### 2.2.1 Global minimum search

Despite advances in computing power, the minimum global search in molecular and atomic clusters remains a complicated task due to several factors. The exploration should be systematic and unbiased; [15, 16] a molecule's degrees of freedom increase with the number of atoms; [16, 17, 18, 19, 20] a molecule composed of N number of atoms possesses 3N degrees of freedom (i.e., a linear molecule has [3N-5] degrees of vibrational modes, whereas a nonlinear molecule has [3N-6] degrees of vibrational modes); and, as a consequence, the potential/free energy surface depends on a large number of variables. The number of local minima increases exponentially as a function of the number of atoms in the molecule. Moreover, the total energy computation requires a quantum mechanical methodology to produce a realistic value for energy. In addition to that, there should be many initial structures. It is essential to sample a large region of the configuration space to ensure that we are not missing structures, making an incomplete sampling of the configurational space and introducing a significant problem to calculating the thermodynamic properties [21]. A Complete sampling of the potential/free energy surface is nearly impossible, but a systematic exploration of the potential energy surface is extremely useful. Although searching for a global minimum in molecular systems is challenging, the design and use of algorithms dedicated to the search for global minima, such as simulated annealing [22, 23, 24, 25, 26, 27], kick method [1, 28, 3, 29, 30, 31, 32] genetic algorithms [33, 34, 35], Gradient Embedded Genetic Algorithm (GEGA) [36, 30, 37], and basin hopping [38, 39], has been accomplished over the years. In the past few years, a member of our research group designed and employed genetic algorithms [3, 28, 40, 41, 42] and kick methodology [43, 44, 45, 46, 47, 48, 49, 41] coupled with density functional theory to explore atomic and molecular clusters' potential energy surfaces. They have led us to solve the minimum global search in a targeted way. In this paper, our computational procedure employs a recently developed and unbiased hybrid strategy for a search methodology that combines a

modified-kick heuristic and genetic algorithm with density functional theory that has been implemented in the *GALGOSON* code. *GALGOSON* systematically and efficiently explores potential/free energy surfaces (PES/FES) of the atomic clusters to find the minimum energy structure. The methodology consists of a three-step search strategy where, in the first and second steps, we explore the PES, and in the third step, we explore the FES. First, the code builds a generation of random initial structures with an initial population of two hundred individuals per atom in the  $\text{Be}_6\text{B}_{11}^-$  cluster using a kick methodology. The process to make 1D, 2D, and 3D structures is similar to that used in previous work. [42, 50] and are restricted by two conditions [42] that can be summarized as follows: a) All the atoms are confined inside a sphere with a radius determined by adding all atoms' covalent radii and multiplied by a factor established by the user, typically 0.9. b) The bond length between any two atoms are the sum of their covalent radii, modulated by a scale factor established by the user, typically close to 1.0; this allows us to compress/expand the bond length. These conditions avoid the high-energy local minima generated by poorly connected structures (too compact/ loose). Then, structures are optimized at the PBE0/3-21G level of theory employing Gaussian 09 code. As the second step, all energy structures lying in the energy range of 20 kcal/mol were re-optimized at the PBE0-GD3/LANL2DZ level of theory and joints with previously reported global minimum structures. Those structures comprised the initial population for the genetic algorithm. The optimization in this stage was at the PBE0-GD3/LANL2DZ level of theory. The criterion to stop the generation is if the lowest energy structure persists for 10 generations. In the third step, structures lying in 10 kcal/mol found in the previous step comprised the initial population for the genetic algorithm that uses Gibbs free energy extracted from the local optimizations at the PBE0-D3/def2-TZVP, taking into account the zero-point energy (ZPE) corrections. The criterion to stop is similar to that used in the previous stage. In the final step, the lowest energy structures are evaluated at a single point energy at the CCSD(T)/def2-TZVP//PBE0-D3/def2-TZVP level of theory. All the calculations were done employing the Gaussian 09 code. [51]

## 2.3 Thermochemistry properties

Classical thermodynamics describes large system's behavior; in contrast, nanothermodynamics is applied to small systems. The thermodynamics of macrosystems could apply to quantum systems. Nanothermodynamics were developed by Terrell Hill during the 1960 [52, 53, 54]. At temperatures different of zero, the Gibbs free energy determines the lowest-energy structure [55], whereas at temperature zero the enthalpy determines the putative global minimum [1, 2]. A simple analysis of the Gibbs free energy given by  $\Delta G = \Delta H - \Delta ST$  deals to a conclusion, in order to minimize the Gibbs free energy we must to maximize the entropy [1, 2, 56]. From the theoretical point of view, and first of all, with the aim to understand molecular properties, at non-zero temperatures, we must know the lowest Gibbs free energy

structure or the largest entropy structure, and all structures closest in energy to the lowest energy structure[1, 2] or all high-entropy structures closest in entropy to the largest. We must keep in mind that the experiments are performed at non-zero or finite temperatures. From a very general point of view, it has been shown that the validity of DFT can be extended to finite temperatures by the concept of ensemble DFT.[57]

### 2.3.1 Statistical thermodynamics

All the thermodynamic properties of an ensemble of molecules can be derived from molecular partition function [1, 2, 58] so, the molecular partition function contains all thermodynamic information in a similar way that the quantum wavefunction contains all the information about the system [1, 58]; In the statistical thermodynamics field the partition functions are central, and as I mentioned at the beginning of this chapter, it is an important function that allows us to compute all thermodynamic macroscopic properties [1, 59, 60, 61, 62]. Previous theoretical studies used the partition function to compute thermodynamic properties of  $\text{Cu}_n$  clusters ( $n=2, 150$ ) as a function of temperature and demonstrated that the magic clusters are temperature dependent [63] Zhen Hua-Li *et al.* [64] computed the thermodynamics of unsupported neutral  $\text{Al}_n$  ( $2 < n < 65$ ) particles evaluating rovibrational partition functions, they reported that the dominant cluster depends on temperature, and gives an overview of recent progress on the nanothermodynamics of metal nanoparticles [65]. Christopher Sutton *et al.* [56] in framework of atomistic thermodynamics predict the behavior of materials at realistic temperatures. Recently, Buelna-Garcia *et al.* [1, 2] used the partition function to compute the temperature-dependent relative population and IR spectra of neutral  $\text{Be}_4\text{B}_8$  and anionic  $\text{Be}_6\text{B}_{11}$  clusters, also Dzib *et al.* [58] employed a similar procedure to compute the reaction rate constants. Other previous theoretical studies computed the temperature-dependent entropic contributions on  $[\text{Fe}(\text{pmea})(\text{NCS})_2]$  complex.[66] In this thesis, the temperature-dependent Gibbs free energy is computed employing the partition function  $Q$  given in Equation, 2.3 under approximations:

1. Harmonic oscillator (HO)
2. The rigid rotor (RR)
3. Ideal gas
4. Particle-in-a-box
5. Born-Oppenheimer (BOA)

We have to underline that RR and HO approximations employed to compute the partition function are **not accurate at high temperatures**, so, to compare theory with experiment [67], the anharmonicity must take into account.

$$Q(T) = \sum_i g_i e^{-\Delta E_i/K_B T} \quad (2.3)$$

In Eq. 2.3,  $g_i$  is the degeneracy factor,  $k_B$  is the Boltzmann constant,  $T$  is the temperature, and  $-\Delta E_i$  is the total energy of a cluster [1, 58, 59]. An exact calculation of  $Q$  in Equation 2.3, could be complicated due to the coupling of the internal modes, a way to decouple the electronic and nuclei modes is through the use of Born-Oppenheimer approximation (BOA). This approach says that the electron movement is faster than the nuclei and assumes that the molecular wave function is the electronic and nuclear wavefunction product.  $\psi = \psi_e \psi_n$  The vibrations change the momentum of inertia and, as a consequence, affects the rotations; this fact tightly couple the vibrational and rotational degrees of freedom; The separation of rotational and vibrational modes is called the rigid rotor (RR), harmonic oscillator (HO,RRHO) approximation, under this approximation, the molecule is treated rigidly, this is generally good when vibrations are of small amplitude[68]. Here the vibration will be modeled in terms of harmonic oscillator and rotations in terms of the rigid rotor within BOA and RRHO approximations, we point out that the RRHO breakdown for low frequencies modes, and one possible solution. There are two approximations to avoid the low frequencies modes: The Truhlar approximation[69, 2] which set up the low frequencies smaller than  $100 \text{ cm}^{-1}$  to a value of  $100 \text{ cm}^{-1}$  and the Grimme's approximation for low-lying frequencies known as free-rotor approximation[70]. In this thesis the low-lying frequencies are treated by the Truhlar approximation[69, 2].

### 2.3.2 The harmonic oscillator approximation

The vibrations of a molecule can be described employing harmonic oscillators, which follow the force Hooke's Law [68, 59], the vibrational energy levels are determined by solving the Schrödinger Equation 2.4.

$$-\frac{\hbar}{2m} \frac{\partial^2 \psi}{\partial x^2} - \frac{1}{2} kx^2 = E_v \psi \quad (2.4)$$

Where  $\hbar$  is the Planck's constant,  $m$  mass of electron, and  $k$  is the Hooke's constant. The solution of Equation 2.4 is given by Equation 2.5

$$E_v = \left( n + \frac{1}{2} \right) \hbar \omega, \quad n = 0, 1, 2, 3 \dots \quad (2.5)$$

The vibrational energy levels are quantized, and with  $n = 0$  appears an energy level called zero point vibrational energy ( $\mathcal{E}_{ZPE}$ ) which is totally a quantum effect, and can be explained with the Heisenberg uncertainty principle. The harmonic potential is a good approximation only for low energies, and at higher energies anharmonicity appears and leads to the anharmonic vibrational problem that could be solved employing second-order vibrational perturbation theory (VPT2) [71, 72], so additional corrections should be done, as mentioned before and underlined here; We must consider the anharmonicity, with the aim of comparing theory with experiment[67].

### 2.3.2.1 $\mathcal{E}_{\text{ZPE}}$ energy correction

The Equation 2.6 gives the zero-point energy ( $\mathcal{E}_{\text{ZPE}}$ ), where  $\nu_i$  are all 3N-6 vibrational modes that the atomic cluster possesses.  $\mathcal{E}_{\text{ZPE}}$  is a pure quantum effect and is due to the fact the Equation 2.5 for  $n = 0$  it still retains a energy value at 0 K temperature.

$$\mathcal{E}_{\text{ZPE}} = \frac{\hbar c}{2\pi} \sum_{i=1}^{3N-6} \nu_i \quad (2.6)$$

In Equation 2.6,  $\hbar$  is the reduced planck's constant,  $c$  is the velocity of light, and  $\nu$  are the vibrational frquencies. The  $\mathcal{E}_{\text{ZPE}}$  can be simply computed with the vibrational modes employing Equation 2.6 under the harmonic oscillator approximation and is the energy due to vibrational at zero K. The electronic energy ( $\mathcal{E}_0$ ) plus  $\mathcal{E}_{\text{ZPE}}$  energy g leads to the real total energy at 0 K ( $\mathcal{U}_0$ ) given in Equation 2.7.

$$\mathcal{U}_0 = \mathcal{E}_0 + \mathcal{E}_{\text{ZPE}} \quad (2.7)$$

In this thesis, we establish that Equation 2.7 is the first thermodynamic correction.

### 2.3.3 The rigid rotor approximation

The simple model of the rigid rotor (RR) can be used to describe the rotational motion, a molecule constrained to rotate around an axis. The RR approximation considers that the atoms are connected by rigid bonds, so the molecule is a rigid object. The rotational energies,  $E_J$  are given by Equation 2.8

$$E_J = J(J+1) \frac{\hbar^2}{2I} \quad (2.8)$$

Where  $J$  is the rotational quantum number ( $J$  is for diatomic molecule,  $l$  for electron around nucleus)  $J = 0, 1, 2, 3 \dots$   $\hbar$  is the Planck's constant and  $I$  is the moment of inertia. Interesting for  $J = 0$ , there are not zero-point energy for rotations.

### 2.3.4 Ideal Gas

The ideal gas law is defined by the Equation 2.9 proposed by Horstmann [73]

$$PV = nRT \quad (2.9)$$

and relates thermodynamic variables, pressure, volume, temperature for a  $n$  number of gas moles. In Equation 2.9,  $R$  is the universal gas constant,  $n$  the number of moles,  $P$  presion,  $V$  volume and  $T$  absolute temperature. There are two assumptions:

1. There are no forces acting among the particles.
2. The particles have not volume.

The ideal gas has only translational and electronic energies.

### 2.3.5 Particle-in-a-box

A particle-in-a-box is a quantum approximation that describes the translational motion of a single particle inside an infinitely potential well. The nonrelativistic Schrödinger wave equation for the case of a particle-in-a-box is given by Equation 2.10

$$-\frac{\hbar}{2m} \frac{\partial^2 \psi}{\partial x^2} = E\psi \quad (2.10)$$

The solution to Equation 2.10 is given by Equation 2.11

$$E_n = \frac{\hbar^2 n^2 \pi^2}{2mL^2} \quad (2.11)$$

For the case in 3D Equation 2.11 leads to Equation 2.12

$$E_n = \frac{\hbar^2 \pi^2}{2mL^2} (n_x^2 + n_y^2 + n_z^2) \quad (2.12)$$

Where  $n$  is the principal quantum number  $n = 1, \infty$ ,  $L$  is the longitud of the box,  $m$  is the mass of electron,  $\hbar$  is the normalized planck's constant.

### 2.3.6 Born-Oppenheimer

Considering that the nuclei is heavier than electrones, the first step in solving the nonrelativistic Schrödinger equation for molecular systems is fix the nuclear positions, which implies that the wavefunctions of nuclei and electrons can be treated separatley. On the one hand, there are cases where the BOA approximation breakdown [74] and on the other, BOA allows us to factorize the partition function  $Q$  (Equation 2.3) into its contributions. In this thesis, we establish that is not possible to compute the partition function by factorization, if we do not consider the BOA approximation [2]. The partition function is factorized into electronic, translational, vibrational, and rotational energies as is displayed in Equation 2.13. Consequently, the partition function,  $Q$ , (Equation 2.3) can be given as a product of the corresponding contributions [54, 58]

$$Q = q_{trans} q_{rot} q_{vib} q_{elec} \quad (2.13)$$

### 2.3.7 Translational partition function

Inserting, the quantum single particle-in-a-3D-box solution, Equation 2.12, into Equation 2.3, and computed the summation, the translation partition function is given by:

$$q_{trans} = V \left( \frac{2\pi K_B T}{\hbar^2} \right)^{\frac{3}{2}} \quad (2.14)$$

where  $m$  is the mass of the particle,  $V$  is the volume and  $T$  is the temperature. Employing the ideal gas equation,  $PV = nRT$ , Equation 2.14 can be rewritten as Equation 2.15.

$$q_{trans} = \frac{K_B T}{P} \left( \frac{2\pi K_B T}{\hbar^2} \right)^{\frac{3}{2}} \quad (2.15)$$

Where  $P$  is the pressure (1 bar),  $K_B$  is the Boltzmann constant. The term  $\lambda_D$  given in Equation 2.16 is known as thermal Broglie wavelength

$$\lambda_D = \left( \frac{2\pi K_B T}{\hbar^2} \right)^{\frac{3}{2}} \quad (2.16)$$

### 2.3.8 Vibrational partition function

The vibrational energy for a vibrational mode is given by the solution of Equation 2.4 with solution given in Equation 2.5, inserting Equation 2.5 into Equation 2.3 leads to Equation 2.17b that describe the vibrational partition function for one vibrational mode,

$$q_{vib} = \sum_{i=0}^{\infty} e^{-\frac{h\nu(n+\frac{1}{2})}{K_B T}} \quad (2.17a)$$

$$= \frac{e^{-\frac{h\nu}{2K_B T}}}{1 - e^{-\frac{h\nu}{K_B T}}} \quad (2.17b)$$

The total vibration of a molecule is given by the summation of independent harmonic oscillators, considering that a non-linear molecule has  $(3N-6)$  vibrational modes ( $n_\nu$ ), the vibrational partition function is given in Equation 2.18a

$$q_{vib} = \prod_{i=1}^{n_\nu} \frac{e^{-\Theta_{vib_i}/2T}}{1 - e^{-\Theta_{vib_i}/T}}, \quad \Theta_{vib_i} = \frac{h\nu_i}{k_B}, \quad (2.18a)$$

### 2.3.9 Rotational partition function

The energy of a single rotational degree of freedom is given by Equation 2.8 that is the solution of Schrodinger Equation for vibrational modes. Inserting Equation 2.8 into Equation 2.3 leads to Equation 2.19b

$$q_{rot} = \sum_{\mathcal{L}=1}^{\infty} (2\mathcal{L} + 1) e^{-\frac{\hbar^2 \mathcal{L}(\mathcal{L}+1)}{2IK_B T}} \quad (2.19a)$$

$$= \sum_{\mathcal{L}=1}^{\infty} (2\mathcal{L} + 1) e^{-\frac{\Theta \mathcal{L}(\mathcal{L}+1)}{K_B T}} \quad (2.19b)$$

with  $\Theta$  given by Equation 2.20

$$\Theta = \frac{\hbar^2}{2I} \quad (2.20)$$

The approximate summation of the Equation 2.19b leads to rotational partition function for linear molecules, and is given by Equation 2.21

$$q_{rot} = \frac{K_B T}{\sigma \Theta} \quad (2.21)$$

Where  $\sigma$  is the symmetry number. For non-linear molecules the rotational partition function is given by Equation 2.22

$$q_{rot} = \frac{1}{\sigma} \left( \frac{\pi(K_B T)^3}{\Theta_A \Theta_B \Theta_C} \right)^{1/2} \quad (2.22)$$

Where  $\Theta_A, \Theta_B$ , and  $\Theta_C$  are the rotational constants, one for each dimension. In summary, Equations 2.23 are the contributions of electronic (2.23e), translational (2.23a), vibrational (2.23d), and rotational (2.23b, 2.23c) to the canonical partition function. Contributions to the canonical partition function

$$q_{trans} = \left( \frac{2\pi m k_B T}{h^2} \right)^{\frac{3}{2}} \frac{k_B T}{P}, \quad (2.23a)$$

$$q_{rot}^l = \frac{1}{\sigma_r} \left( \frac{T}{\Theta_r} \right), \quad (2.23b)$$

$$q_{rot}^{nl} = \frac{\pi^{1/2}}{\sigma_r} \left( \frac{T^{3/2}}{(\Theta_A \Theta_B \Theta_C)^{1/2}} \right), \Theta_i = \frac{\hbar}{2I_i k_B}, i = A, B, C, \quad (2.23c)$$

$$q_{vib} = \prod_{i=1}^{n_\nu} \frac{e^{-\Theta_{vib_i}/2T}}{1 - e^{-\Theta_{vib_i}/T}}, \Theta_{vib_i} = \frac{h\nu_i}{k_B}, \quad (2.23d)$$

$$q_e = \omega_0, \quad (2.23e)$$

### 2.3.10 Internal energy and entropy

The internal energy,  $U$  is given by Equation 2.24

$$U = K_B T^2 \left( \frac{\partial \ln(Q)}{\partial T} \right) \quad (2.24)$$

The  $K_B$  is the Boltzmann constant,  $T$  is the absolute temperature, the entropy can be computed employing the Equation 2.25

$$S = K_B T + \ln(Q) + K_B T^2 \left( \frac{\partial \ln(Q)}{\partial T} \right) \quad (2.25)$$

The internal energy is composed of terms given in Equation 2.26

$$U = U_{trans} + U_{rot} + U_{vib} + U_{elec} \quad (2.26)$$

The entropy is composed of terms given in Equation 2.27

$$S = S_{trans} + S_{rot} + S_{vib} + S_{elec} \quad (2.27)$$

We employ equations 2.26, 2.28, 2.29 to compute the total internal energy ( $U_T$ ), enthalpy (H), and Gibbs energy (G) of the atomic cluster at finite temperature employing Equations 2.30, 2.31. The equations to compute entropy contributions (S) is Equation 2.27 and those employed in a previous work [55, 1, 2] and any standard thermodynamics textbook [59, 54].

$$\mathcal{U}_0 = \mathcal{E}_0 + \mathcal{E}_{ZPE} \quad (2.28)$$



$$U_T = \mathcal{U}_0 + (E_{rot} + E_{trans} + E_{vib} + E_{elect}) \quad (2.29)$$

$$H = U_T + RT \quad (2.30)$$

$$G = H - TS \quad (2.31)$$

In Equations above,  $\mathcal{E}_{ZPE}$  is the zero-point energy correction,  $\mathcal{E}_0$  is the electronic energy, and  $E_{rot} + E_{trans} + E_{vib} + E_{elect}$  are the contributions to energy due to translation, rotation, vibration and electronic partitions as function of temperature, respectively. To compute the Boltzmann probability of occurrence of one particular neutral  $\text{Cu}_{38}$  cluster in an ensemble at thermal equilibrium and at finite temperatures, we employ the probability of occurrence [1, 2, 64, 75, 76, 77, 58, 78, 79, 63, 64] given in Equation 2.32

$$P_i(T) = \frac{e^{-\beta\Delta G^k}}{\sum e^{-\beta\Delta G^k}}, \quad (2.32)$$

where  $\beta = 1/k_{\text{B}}T$ , and  $k_{\text{B}}$  is the Boltzmann constant,  $T$  is the temperature, and  $\Delta G^k$  is the Gibbs free energy of the  $k^{\text{th}}$  isomer. We point out that Gibbs free energies must be corrected considering the symmetry, Buelna-Garcia *et al.* [2] in a previous work shows that the contribution of the rotational entropy to the Gibbs free energy calculated with and without symmetry behave linearly with the temperature and could be significant [55] Equation 2.32 is restricted so that the sum of all probabilities of occurrence, at fixed temperature  $T$ ,  $P_i(T)$  is equal to 1 and given by Equation 2.33

$$\sum_i P_i(T) = 1, \quad (2.33)$$

## 2.4 Chirality

The term chiral was coined by W. H. Thompson in 1884 and came from the Greek word for hand (*cheir*) [80]. Lord Kelvin wrote: *I call any geometrical figure, or group of points, chiral, and say that it has chirality, if its image in a plane mirror, ideally realized, cannot be brought to coincide with itself* [81] A chiral molecule cannot be superimposed on its mirror image by any translation and rotation on the plane. These two, L- and R-structures, are called enantiomers, which have identical chemical and physical properties, such refractive index, melting point, infrared spectrum among others. Figure 2.1 shows the most familiar example of chiral. Chi-



Figure 2.1: A chiral example, the hands

ality depends on symmetries,  $C_1$ ,  $C_n$  and  $D_n$  are the chiral point groups and any chiral molecule must belong to any of these groups [81]. Particularly, the chirality

of nanoclusters has attracted attention due to their chiroptical properties, potential application in efficient chiral discrimination [82, 83], nonlinear optics [84] and chiral materials with interesting properties, [85, 86, 87] and of course, not to mention that chiral structures play a decisive role in biological activity [88]. Another system with chiral structures, the lowest energy structures of Au<sub>28</sub> and Au<sub>55</sub> are chiral [89]. In this study, two systems were found chiral, the Cu<sub>13</sub> and Be<sub>4</sub>B<sub>8</sub>.

## 2.5 Chemical bonds

Chemical bonds are related to electron sharing between atoms [90], and they are not observable quantities. The chemical bond is a model to describe how atoms link to one another to build a molecule or solid and involve the atom connectivity concept. From the theoretical point of view, the physical interactions responsible for the cohesion of molecules can be studied by quantum chemistry. The definition of bond is *A bond is considered to exist when two adjacent atoms are so located that the potential energy is a minimum, and when appreciable energy must be supplied to cause the atoms to separate* [91]. There are some principles that must be observed:

1. The Helium atom and the atoms that have eight electrons in the frontier orbital can not form a chemical bond (neon, argon, krypton, xenon, and radon).
2. All atoms of the periodic table can form a chemical bond (except group 18).
3. Bonds are formed by sharing electrons by two or more atoms

When a chemical bond is formed between two atoms, the energy of the system must be decreased. Basically there are two types of chemical bonds

1. Ionic bonding, which implies complete transfer of electrons from one atom to another (NaCl).
2. Covalent bonding, in which there is share of electrons between atoms (H<sub>2</sub>).

There are others types of bonding:

1. Metallic bonds are formed by atoms with low ionization energy and the attraction between delocalized electrons and positive ions (Ag).
2. Hydrogen bonds are an intermolecular interaction that forms a type of dipole-dipole attraction, and they are indicated by ...
3. Van der Waals (vdW) bond, the [International Union of Pure and Applied Chemistry \(IUPAC\)](#), defines a Van der Waals bond as: *The attractive or repulsive forces between molecular entities (or between groups within the same molecular entity) other than those due to bond formation or to the electrostatic interaction of ions or of ionic groups with one another or with neutral molecules.*

Table 2.1 displays the typical bonding energies for different bonding types and compounds. In this thesis we employed the adaptive natural density partitioning (AdNDP) method to study the bonding in  $\text{Cu}_{13}$  and  $\text{Be}_4\text{B}_8$  clusters. The AdNDP employs the concept of the electron pair as central part of chemical bonding models [92]. It represents the electronic structure in terms of  $n$ -center two electrons ( $nc$ - $2e$ ) bond, where  $n$  are the number of atoms. The natural bond orbitals (NBOs) create the closest Lewis structure for a given structure, and they provide a valence bond-type of the quantum wavefunction in terms of the Lewis theory. From a computational point of view AdNDP is a generalization of NBO analysis by Weinhold [92], thus, the AdNDP method explains the bonding employing the quantum wavefunction in terms of the simple theory of Lewis. The AdNDP analyses the first-order reduced density matrix and recovers Lewis bonding ( $1c$ - $2e$  or  $2c$ - $2e$ , i.e., lone pairs (LPs) or two-center two-electron bonds) and delocalized bonding elements (associated with the concept of electron delocalization). The AdNDP analysis for chiral putative low-energy structures of  $\text{B}_4\text{B}_8$  and  $\text{Cu}_{13}$  are displayed in Figure 4.2, and Figure 5.2, respectively.

Table 2.1: Bonding energies

Bonding type	Substance	Bonding energy (kcal/mol)
Ionic	NaCl	193 (E) [93]
Covalent	C	170 (E) [94]
Metallic	Fe	98 (E) [95]
van der Waals	vdW-bonded organic molecule dimers	0.5 (T) [96]
Hydrogen bond	Isolated bond	5-6 (E) [97]
	Proteins in solution	0.5-1.5 (E) [97]

## 2.6 Applications of atomic clusters

In the chemistry field, the term *clusters* or *atomic clusters*, is used to describe a collection of atoms or molecules. Atomic clusters are ideal to study catalysis and provide fundamental understanding about the catalytic processes, there are several applications of atomic clusters, among them:

- Mechanisms of CO oxidation [98]
- $\text{CO}_2$  conversion
- Dehydrogenation
- Hydrogenation
- Electrochemical water splitting

The IUPAC, defines a cluster as: *A number of metal centres grouped close together which can have direct metal bonding interactions or interactions through a bridging*

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*ligand* , but are not necessarily held together by these interactions. On the other hand, a nanoparticle is a particle with dimensions in the 1–100 nm range, and they can be extended to 500 nm [99]. A nanocluster is a collection of a few atoms. In this doctoral thesis, we employed the term *Nanoclusters* because our systems are composed of few atoms.



# The $\text{Be}_6\text{B}_{11}^-$ cluster.

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## 3.1 Abstract

The starting point to understanding cluster properties is the putative global minimum and all the nearby local energy minima; however, locating them is computationally expensive and challenging due to the degrees of liberty associated with the molecule rise as a function of the number of atoms. Therefore, the number of possible combinations increases exponentially, leading to a combinatorial explosion problem. The relative populations and spectroscopic properties of a molecule that are a function of temperature can be approximately computed by employing statistical thermodynamics. Here, we investigate entropy-driven isomers distribution on  $\text{Be}_6\text{B}_{11}^-$  clusters and the effect of temperature on their infrared spectroscopy and relative populations. We identify the vibration modes possessed by the cluster that significantly contribute to the zero-point energy. A couple of steps are considered for computing the temperature-dependent relative population: First, using a genetic algorithm coupled to density functional theory, we performed an extensive and systematic exploration of the potential/free energy surface of  $\text{Be}_6\text{B}_{11}^-$  clusters to locate the putative global minimum and elucidate the low-energy structures. Second, the relative populations temperature effects are determined by considering the thermodynamic properties and Boltzmann factors. The temperature-dependent relative populations show that the entropies and temperature are essential for determining the global minimum. We compute the temperature-dependent total infrared spectra employing the Boltzmann factor weighted sums of each isomer's infrared spectrum and find that at finite temperature, the total infrared spectrum is composed of an admixture of infrared spectra that corresponds to the spectrum of the lowest energy structure and its isomers located at higher energies. The methodology and results describe the thermal effects in the relative population and the infrared spectra.

## 3.2 Introduction

In recent years, the pure boron clusters, the metal, and non-metal doped boron clusters, have attracted considerable attention [1, 2, 100, 101, 102, 103, 104, 105, 106, 107, 42, 28] due to their unpredictable chemistry [108, 109] and high potential to form novel structures [110]. Boron is the smallest and lightest semi-metal atom [107, 111] and a neighbor of carbon in the periodic table. It has electron deficiency [112, 113, 114, 110] and a high capacity to combine and form novel atomic and molecular boron structures that are planar and quasi-planar [115, 86, 116] It

can also form nanotubes [117, 110], borospherenes [118, 102, 119], borophene [102], cages [120], chiral helices [121, 3] and nanosheets [115, 122] consisting of triangle units of boron atoms. Boron can absorb neutrons that make it useful in nuclear and medical applications [123, 124, 125]. Aromaticity, antiaromaticity, and conflicting aromaticity dominate the chemical bonding in boron-based clusters [126, 127, 121, 128]. The two most-used indices for quantifying aromaticity are the harmonic oscillator model of aromaticity, based on the geometric structure, and the nucleus-independent chemical shift, based on the magnetic response. Aromaticity is not observable, cannot be directly measured [129], and it correlates with electronic delocalization [130]. However, with applications in molecular devices, the dynamic structural fluxionality in boron and boron-doped based molecular systems is due to electronic delocalization [121, 131]. Moreover, electronic localization/delocalization contributes significantly to stability, magnetic properties, and chemical reactivity [129]. Nowadays, dynamic structural fluxionality in boron nanoclusters is a topic of interest in nanotechnology [119, 132]. The fluxionality of an atomic cluster is highly relevant in terms of its catalytic activity [133], and in boron-based nanoscale rotors, it is a function of the atomic structure, size, bonding, and cluster charge [134]. Moreover, doping a boron cluster with metals [135, 103, 136, 105, 137, 138, 139] and non-metals [140] dramatically affects its structure, stability, and reactivity, as with the shut-down in the fluxionality of the boron-doped anion  $\text{B}_{19}^-$  [141]. It is important to mention, the emission of radiation as a competing cooling channel has to be considered in studying small cationic boron clusters' stabilities. Accordingly to Ferrari *et al.*, this improving agreement between experiment and theory [142].

In this chapter, we consider that temperature and entropy are critical in elucidating the low-energy structures and highlight the importance of understanding the thermal and entropic effects in the  $\text{Be}_6\text{B}_{11}^-$  fluxional cluster. In the past years, a boron molecular Wankel motor [143, 144, 101, 145, 146, 147] and subnanoscale tank treads have been reported [148, 149]; however, the entropic and temperature terms have not been considered. In collaboration with Merino's group and Zhai's group, some of us studied and reported fluxionality in  $\text{Be}_6\text{B}_{11}^-$  [3]. The computations indicated that there were two competitive low-energy structures: a helix-type cluster and a fluxional coaxial multiple-layered cluster. More recently, another lowest-energy structure was found in the  $\text{Be}_6\text{B}_{11}^-$  cluster by employing a cellular automaton algorithm. [50] However, the putative global minimum energy structure and its molecular properties depend strongly on the temperature-entropy term [16, 63, 150, 151, 152].

In several previous works, one of the authors computed the barrier energy in a chemical reaction by taking into account the effect of temperature-entropy term [58], computed the temperature-dependent dipole moments for the  $\text{HCl}(\text{H}_2\text{O})_n$  clusters [46], computed the temperature-dependent linear optical properties of the Si(100) surface [153], and more recently, it was considered in a study of gold clusters [79, 154, 78] and the thermochemical behavior of the sorghum molecule [77]. Nevertheless, most theoretical density functional studies assume that the temperature is zero and neglect temperature-dependent and entropic contributions; conse-

quently, their finite temperature properties remain unexplored [155, 156], whereas experimental studies are carried out in non-zero temperatures. Thus, it is necessary to understand the effect of the temperature on the cluster properties and the lowest energy structure's determination [155, 156]. Herein, we investigate the effect of temperature-entropy term on the relative population and its infrared spectra, which need the putative elucidation global minimum and its low-energy isomers [21, 157, 16]. The first starting point requires a minimum global search on the potential/free energy surfaces, which is a complicated task. Taking temperature into account requires dealing with small systems' thermodynamics; The Gibbs free energy of classical thermodynamics also applies for small systems, known as thermodynamics of small systems [158, 53, 159] or nanothermodynamics [65]. The thermodynamics of clusters have been studied by various theoretical and simulation tools [16, 52, 158, 160, 161, 162, 163, 155, 164, 165] like molecular-dynamics simulations [106], Monte Carlo, and analytic methods. Under the harmonic superposition approximation, the temperature-entropy term can be computed with the vibrational frequencies on hand. The entropy effects have been considered for gold, copper, water, and sodium clusters [154, 78, 79, 166, 63, 167, 168, 169, 170, 171]. As the second step for understanding cluster properties relies on the cluster's spectroscopy, spectroscopy gives insight into the structure and detects structural transformations in clusters [172, 173, 174]. The temperature effects on IR spectra have been studied experimentally and theoretically on small and neutral gold clusters [154, 79] and boron cluster [146]. In the same direction, the pristine Au<sub>13</sub> gold cluster's thermodynamical stability at finite temperature was studied using the replica-exchange method, which shows a fluxional behavior [166]. Au<sub>N</sub> clusters thermodynamics properties (30 < N < 147) were studied employing the Gupta potential and DFT methodology [78]. The total absorption spectra were computed as the sum of the different spectra of different isomers [175].

In this chapter will employ statistical thermodynamics to compute the Gibbs free energy entropic-temperature-dependency, evaluate relative populations as function of temperature, and take into account the effects of temperature on the IR spectra. We also identify the vibration modes that make a significant contribution to the zero-point energy of the cluster that is strongly dominated at temperatures higher than 377 K, and also we show this structure poses the shortest B-B bond length. We investigate the effect of long-range van der Waals interactions on solid-solid transformation points; moreover, we found the vibrational modes responsible for the fluxionality of the cluster. Adicionally, we computed the relative population at single point CCSD(T) level of theory. We believe that this yields useful information about which isomers will dominate at hot temperatures. No work has been attempted to investigate temperature-entropy driven isomers in the fluxional Be<sub>6</sub>B<sub>11</sub><sup>-</sup> cluster as far as we know. The rest of the chapter discusses the lowest energy structures, energetic ordering at DFT/CCSD(T) level of theory, the relative population, and IR spectra taking into account the temperature-entropy term.



### 3.3 Computational Details

#### 3.3.1 Boltzmann Population

The properties observed in a molecule are statistical averages over the ensemble of geometrical conformations or isomers accessible to the cluster [176]. So the molecular properties are ruled by the Boltzmann distributions of isomers that can change due to temperature-entropic term [46, 177, 63], and the soft vibrational modes that clusters possess make primary importance contributions to the entropy [169]. The relative populations of the low-energy isomers of the cluster  $\text{Be}_6\text{B}_{11}^-$  are computed through the probabilities defined in Equation 3.1

$$P(T) = \frac{e^{-\beta\Delta G^k}}{\sum e^{-\beta\Delta G^k}}, \quad (3.1)$$

where  $\beta = 1/k_{\text{B}}T$ , and  $k_{\text{B}}$  is the Boltzmann constant,  $T$  is the temperature in Kelvin,  $\Delta G^k$  is the Gibbs free energy of the  $k^{\text{th}}$  isomer. Equation 3.1 establishes that the distribution of molecules will be among energy levels as a function of the energy and temperature. It is worth mentioning that the energy of separation among isomers (energy gap between two isomers) is determinant in the computation of the solid-solid transition,  $T_{ss}$  point.  $T_{ss}$  occurs when two competing structures are energetically equaled, and there is simultaneous coexistence of structural isomers at  $T$ . In other words, the  $T_{ss}$  point is a function of the energy difference between two isomers and the energy  $\Delta G$  that the cluster possesses. Boltzmann distribution finds a lot of applications as to native protein structures [76] for a microscopy system, a temperature  $T$  or like method simulated annealing applied to the search of structures of minimum energy, rate of chemical reaction [58], sedimentation, among others. For the calculation of the Gibbs free energies at temperature  $T$  and the relative populations, we used a homemade *Python/Fortran* code called Boltzmann-Optics-Full-Ader (BOFA).

#### 3.3.2 IR Spectra

The vibrational spectra are useful for identifying phases and determining structures [178], among other applications mentioned above. In this study, the IR harmonic spectra for each isomer were calculated employing Gaussian code [51]. All isomers were characterized as minima because we found no negative frequencies in each isomer. The Lorentzian line shape, with a width at half maximum of  $20 \text{ cm}^{-1}$ , and a scaling factor of 0.98 were used to compute the IR spectra for each isomer. The most considerable contribution to total IR spectra is the putative global minimum atomic structure [175], while the isomers located at high energies contribute little to the molecular properties. Therefore, the total IR spectrum is dependent on the temperature results from the contributions of all IR spectra weighted according to their relative populations. In this chapter, to obtain the total IR spectrum at temperature  $T$ , we weighted the IR spectrum of each isomer according to the prob-

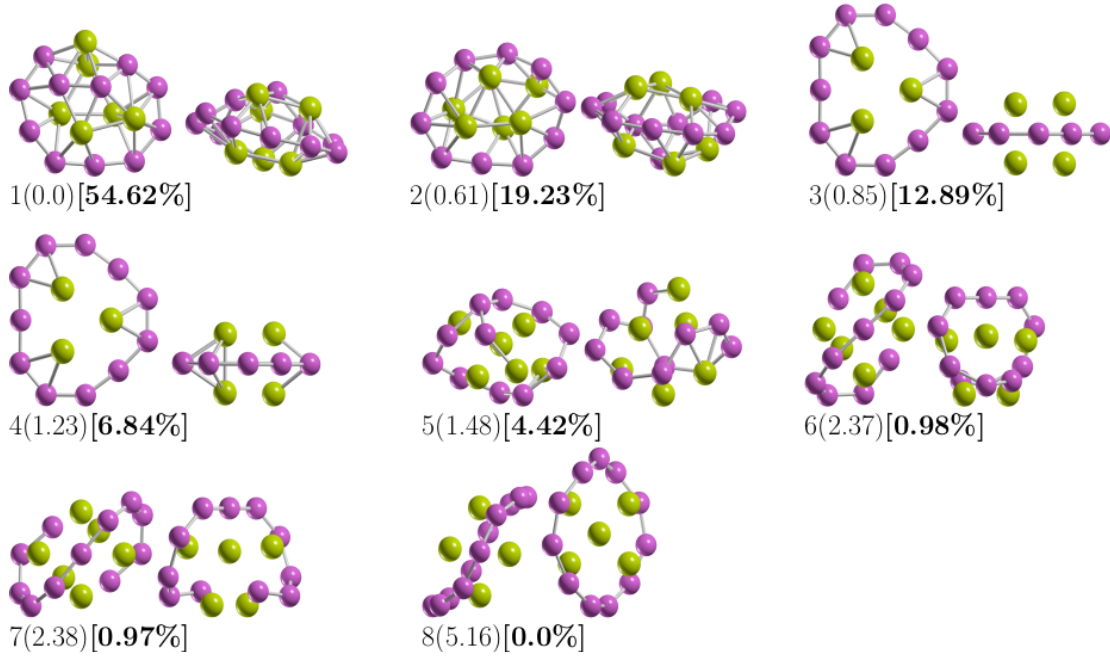


Figure 3.1: The optimized geometries of  $\text{Be}_6\text{B}_{11}^-$  cluster.

abilities computed in Equation 3.1 and the sum of all of them; thus, we computed the total IR spectrum as a function of the temperature.

The global exploration of the potential and free energy surfaces of the  $\text{Be}_6\text{B}_{11}^-$  was done with a hybrid genetic algorithm written in Python. All local geometry optimization and vibrational frequencies were carried out employing the density functional theory (DFT) as implemented in the Gaussian 09 [51] suite of programs, and no restrictions in the optimizations were imposed. Final equilibrium geometries and relative energies are reported at PBE0 [179]/def2-TZVP [180] level of theory, taking into account the D3 version of Grimme’s dispersion corrections [181], and including the zero-point (ZPE) energy corrections. (PBE0-D3/def2-TZVP) As Pan *et al.* [182] reported, the computed relative energies with PBE0 functional are very close to the CCSD(T) values in  $\text{B}_9^-$  boron cluster. The def2-TZVP basis set from the *Ahlrichs* can improve computations accuracy and describe the  $\text{Be}_6\text{B}_{11}^-$  cluster [3]. To gain insight into its energetics, we evaluated the single point energy at CCSD(T)/def2TZVP//PBE0-D3/def2-TZVP level of theory for the putative global minima and the low-energy isomers. The total IR spectra dependent on temperature are computed employing Boltzmann weighted sum of the IR spectra of each isomer, and the relative populations using Boltzmann factors, both of them implemented in a made in home Python/Fortran code called BOFA. The BOFA code is employed in the computation of the relative population and weighted IR spectra.

## 3.4 Results and Discussion

### 3.4.1 The lowest energy structures and energetics

We show in Figure 3.1 the lowest energy structure of  $\text{Be}_6\text{B}_{11}^-$  clusters and seven low-energy competing isomers computed at the PBE0-D3/def2-TZVP level of theory. The criterion for drawing the structures is until the percentage of the relative population is zero. The relative Gibbs free energy is given in kcal/mol (round parenthesis) and computed at 298.15 K and 1 bar. In square parenthesis, and in bold is given the percentage of the relative population computed employing Equation 3.1 at 298.15 K. For the putative global minimum at the PBE0-D3/def2-TZVP level of theory, the optimized average B-B bond length is 1.64 Å. In contrast, the optimized B-Be bond length is 2.01 Å. To observe the trend in B-B bond length in the low-energy

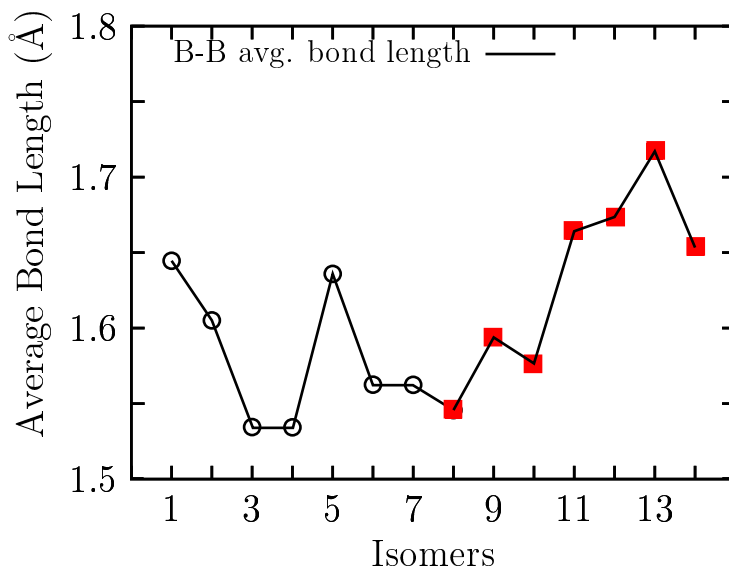


Figure 3.2: The average B-B bond length a function of the number of isomers.

structures, Figure 3.2 shows the average bond length for B-B for the fourteen lowest energy isomers energetically accommodated, from the most energetically favorable, isomer number 1, to the least stable, isomer number 14. Our calculations indicated that the largest average value of the B-B bond length is 1.71 Å and belongs to isomer number 13, which is 25 kcal/mol less stable than the putative global minimum. The lowest average value of the B-B bond length is 1.53 Å and corresponds to the isomers coaxial triple-layered structures with  $C_s$  and  $C_{2v}$  symmetries, located at energies of 0.85 and 1.23 kcal/mol above the putative global minima, respectively. The structures are depicted in Figure 3.1(3)(4). In these structures, the lowest average B-B bond length of 1.53 Å is considerably shorter compared with the: (a) length of a typical B-B single bond of 1.72 Å [183], (b) the bond length of the B8 and  $\text{B}_9^-$  molecular wheels [184, 3], and slightly shorter in 2.2% than the B-B double

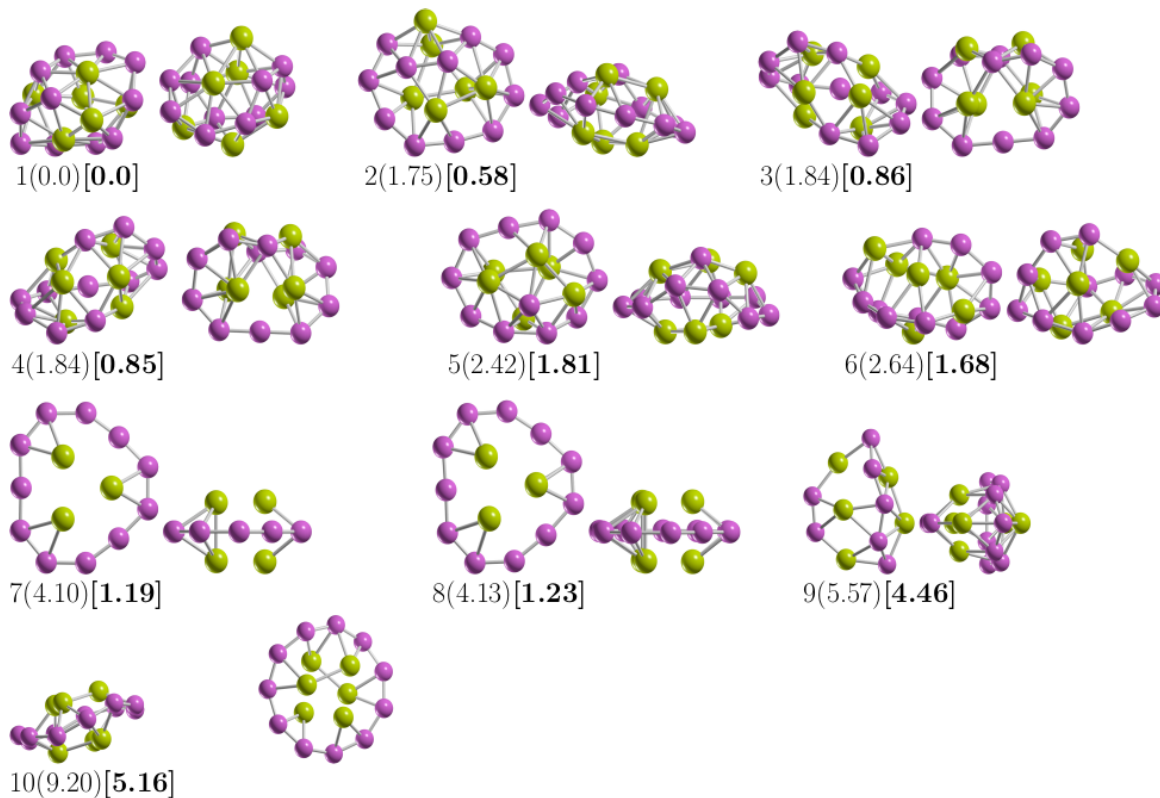


Figure 3.3: The most important energy isomers shown in two orientations, rotated 90 degrees up to plane paper and front.

bond length experimentally characterized in the range of 1.57-1.59 Å [185, 186]. The average B-B bond length shortens from 1.64 Å to 1.53 Å, suggesting strong hyperconjugation in the coaxial triple-layered structures. The shortening of the B-B bond length is caused by orbital interaction, which is also a cause of C-C bond shortening in the Butyne molecule. [187] Hyperconjugation has been shown in the shortening of B-B and C-C bond lengths [188, 187] and which causes increases in the number of electrons shared between region. Figure 3.4 shows the average bond length for Be-B for the 14 low-energy isomers. The largest average value of the Be-B bond length is 2.0 Å and 2.10 Å, which correspond to the isomer coaxial triple-layered structures with  $C_s$  and  $C_{2v}$  symmetries, respectively. This suggests that if the shortening of the bond length increases the number of electrons shared in that region [187], the increase in bond length should decrease the number of electrons; consequently, the electron delocalization occurs in the ring of boron atoms. In Figure 3.1(1), is depicted the putative global minimum with 54% of the relative population, and it has  $C_1$  symmetry with a singlet electronic state  $^1A$ . It is a distorted, oblate spheroid with three beryllium atoms in one face and two in the other face. Nine boron and one beryllium atoms form a ring located around the spheroid's principal axes, and the remaining two boron atoms are located close to the boron ring on one of its

faces. The second higher energy structure, at 298.15 K, lies at a Gibbs free energy of only 0.61 kcal/mol above the putative global minimum; it has  $C_1$  symmetry with a singlet electronic state  $^1A$ . It is a prolate spheroid with 19% of the relative population at a temperature of 298.15 K. The next two higher energy isomers, at 298.15 K, are located at 0.85 and 1.23 kcal/mol Gibbs energy above the putative global minimum. They are prolate, coaxial, triple-layered structures with  $C_s$ , and  $C_{2v}$  symmetries and singlet electronic states  $^1A$  and  $^1A_1$ , respectively. This clearly shows that the low-symmetry structure  $C_s$  becomes energetically preferred compared to the  $C_{2v}$  symmetry, with a Gibbs free energy difference of 0.38 kcal/mol at 298.15 K due to the entropic effects. This is in agreement with a similar result found in  $\text{Au}_{32}$  [15]. According to our computations, those structures are strongly dominant at temperatures higher than 377 K. The next structure shown in Figure 3.1(5) is located 1.48 kcal/mol above the global minimum; it is close to spherical in shape and corresponds to a prolate structure with  $C_1$  symmetry and a singlet electronic state  $^1A$ . This structure makes up only 4.4% of the relative population at 298.15

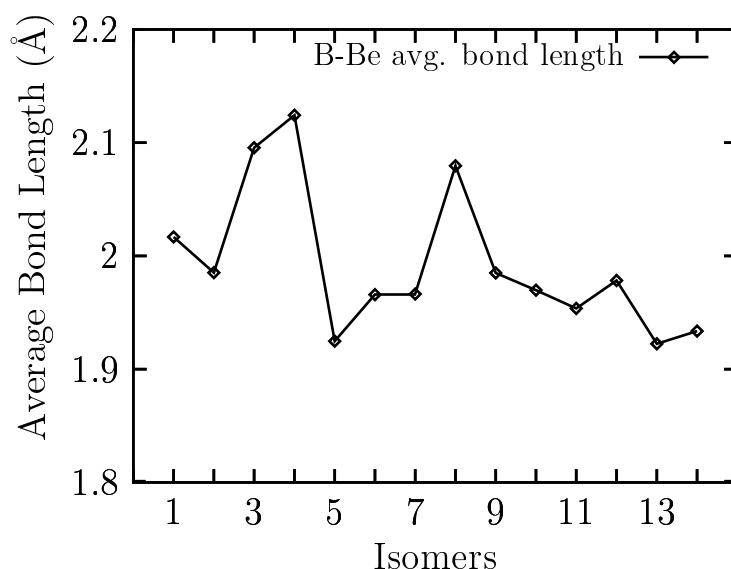


Figure 3.4: The average Be-B bond length a function of the number of isomers.

K. The next two structures, located at a Gibbs free energy of 2.37 kcal/mol above the global minimum, are the chiral helix-type structures. These were previously reported by Guo *et al.* [3] as the global minimum and also found with *GALGOSON* code. They are prolate structures with  $C_{2v}$  symmetries and their relative population is around only 1%. We note that the chiral-helix structures are never the lowest energy structures throughout the entire temperature range. The relative population is zero for structures located at relative Gibbs free energies higher than 5.1 kcal/mol, and at 298.15 K, there is no contribution of these isomers to any total molecular property. A full understanding of the molecular properties requires the search for the global minimum and all its closest low-energy structures [21]. The separation

among isomers by energy difference is an important and critical characteristic that influences the relative population and, consequently, the overall molecular properties. To gain insight into how the energy difference among isomers changes and how the energy ordering of the low-energy structures is affected. We computed the putative global minima and the first seven low-energy structures a single point energy at the CCSD(T)/def2-TZVP level of theory corrected with the zero-point energy computed at the PBE0 D3/def2-TZVP level of theory. Figure 3.3 shows the isomers energetic-ordering considering CCSD(T) energy in kcal/mol in parentheses, and the corrected in kcal/mol in square brackets. At the CCSD(T) level of theory, the global minimum, the seven lowest energy isomers, and the energy order agree with those in a previous work [50], as shown in the first row of Table 3.1 The second row of Table 3.1 shows the corrected Interestingly, the energetic ordering of isomers does not change when considering the ZPE. Nevertheless, the energy-difference among

Table 3.1: The relative energies in kcal·mol<sup>-1</sup>, coupled cluster single-double and perturbative triple.

Be <sub>6</sub> B <sub>11</sub> <sup>-</sup>	Level	Isomers						
		<i>i</i> <sub>1</sub>	<i>i</i> <sub>2</sub>	<i>i</i> <sub>3</sub>	<i>i</i> <sub>4</sub>	<i>i</i> <sub>5</sub>	<i>i</i> <sub>6</sub>	<i>i</i> <sub>7</sub>
	CCSDT	0.0	1.75	1.84	1.84	4.10	4.13	2.64
	CCSDT+ $\mathcal{E}_{\text{ZPE}}$	0.0	0.58	0.85	0.86	1.19	1.23	1.68
	$\Delta G$	0.0	-1.48	0.89	0.88	-0.63	-0.25	4.14
	$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.0	-0.29	1.51	1.52	2.41	2.42	5.0
Be <sub>6</sub> B <sub>11</sub> <sup>-</sup>	$\mathcal{E}_0$	0.0	0.87	2.50	2.50	5.32	5.32	5.96
	Point group symmetry	<i>C</i> <sub>1</sub>	<i>C</i> <sub>1</sub>	<i>C</i> <sub>2</sub>	<i>C</i> <sub>2</sub>	<i>C</i> <sub><i>s</i></sub>	<i>C</i> <sub>2<i>v</i></sub>	<i>C</i> <sub>1</sub>
	Electronic ground state	<sup>1</sup> A	<sup>1</sup> A	<sup>1</sup> A	<sup>1</sup> A	<sup>1</sup> A'	<sup>1</sup> A <sub>1</sub>	<sup>1</sup> A
	Frequencies	230	119	102	100	46	43	161

isomers were reduced drastically. For example, the energy difference between the first and second isomers was reduced by 66%, from 1.75 to 0.58 kcal/mol; the energy difference between the second and third isomers was increased almost 300%, from 0.1 to 0.27 kcal/mol, as shown in rows one and two of Table 3.1, respectively. This change (increase/decrease) in energy difference among isomers has an enormous impact on the relative population. Consequently, we deduced that the ZPE inclusion is essential to the isomers' energy ordering and molecular properties. The third row of Table 3.1 shows the energy order considering the Gibbs free energy computed at 298.15 K; at this temperature, the isomers' energy ordering changes: the second isomers are the putative global minima, and the first isomers have the fifth lowest energy. Interestingly, this energy ordering occurs at 298.15 K, and it is a function of the temperature, which we discuss later in the relative population section. The fourth row in Table 3.1 shows the electronic energy considering the ZPE. It follows the same trend in energy ordering when considering the Gibbs free energy, and it is

the same putative global minima. The fifth row in Table 3.1 details the electronic energy. It almost follows the CCSD(T) energies trend, except isomer number 8 takes second place, located at 0.52 kcal/mol above the putative global minimum. The sixth, seventh, and eighth rows in Table 3.1 show the point group symmetry, electronic ground state, and the lowest vibrational frequency of each isomer, respectively. When we use the Gibbs free energy to energy order the structures, the second isomers change to first place, becoming the lowest energy structure; the energy ordering changes drastically, whereas the electronic energy follows a similar trend to that of CCSD(T) energy ordering. This shows us that the level of theory and the inclusion of entropy and temperature change the energy ordering and, therefore, the overall molecular properties.

### 3.4.2 Relative population

Table 3.2: The five points temperature solid-solid.

$T_{\text{ss}_i\text{-g}}/T_{\text{ss}_i}$	PBE0-D3/def2-TZVP	PBE0/def2-TZVP
1	(377)/[ <b>33</b> ]	(388)/[ <b>34.5</b> ]
2	(424)/[ <b>22.9</b> ]	(444)/[ <b>22.8</b> ]
3	(316.7)/[ <b>14</b> ]	(305.4)/[ <b>14.7</b> ]
4	(349)/[ <b>17.6</b> ]	(343.6)/[ <b>12.2</b> ]
5	(258)/[ <b>5.7</b> ]	(246.7)/[ <b>4.2</b> ]

We show in Figure 4.4 panel (a) the most important and strongly dominating  $T_{\text{ss}_1\text{-g}}$  point that is located at 377 K temperature scale with a relative population of 33%. For temperatures ranging from 10 to 377 K, the relative population is strongly dominated by the putative global minima isomer distorted oblate spheroid with  $C_1$  symmetry and this relative population is similar to  $-T^{-3}$  function with one point of inflection located at 180 K. After decreases monotonically up to 377 K. At the  $T_{\text{ss}_1\text{-g}}$  point, the distorted oblate spheroid with  $C_1$  symmetry co-exist and compete with the coaxial Triple-Layered structures with  $C_s$  symmetry; This implies that the distorted oblate spheroid will be replaced with the coaxial Triple-Layered structures. Above temperature 377 K, the relative population is strongly dominated by the coaxial Triple-Layered structures with  $C_s$  symmetry, located at 0.85 kcal/mol above the global minima at temperature 298.15 K. This relative population depicted in blue-solid line in panel (a) has behavior as a sigmoid function, from temperatures ranging from 377 to 600 K, it grows rapidly and from temperatures ranging from 600 to 1500 K, it almost keeps constant with 60%. The second  $T_{\text{ss}_2\text{-g}}$  point is located at temperature 424 K with a relative population of 22.9%, and this point the global minima distorted oblate spheroid with  $C_1$  symmetry co-exist, and compete with the coaxial Triple-Layered structures with  $C_{2v}$  symmetry, located at

1.23 kcal/mol above the global minima at 298.15 K. The relative population of the coaxial Triple-Layered  $C_{2v}$  symmetry depicted in green-solid line in panel (a) also has a behavior of a sigmoid function and up to 600 K it keeps constant with 32% of relative population. The  $T_{ss3-g}$  and  $T_{ss4-g}$  points, displayed in Figure 4.4 panel (a),

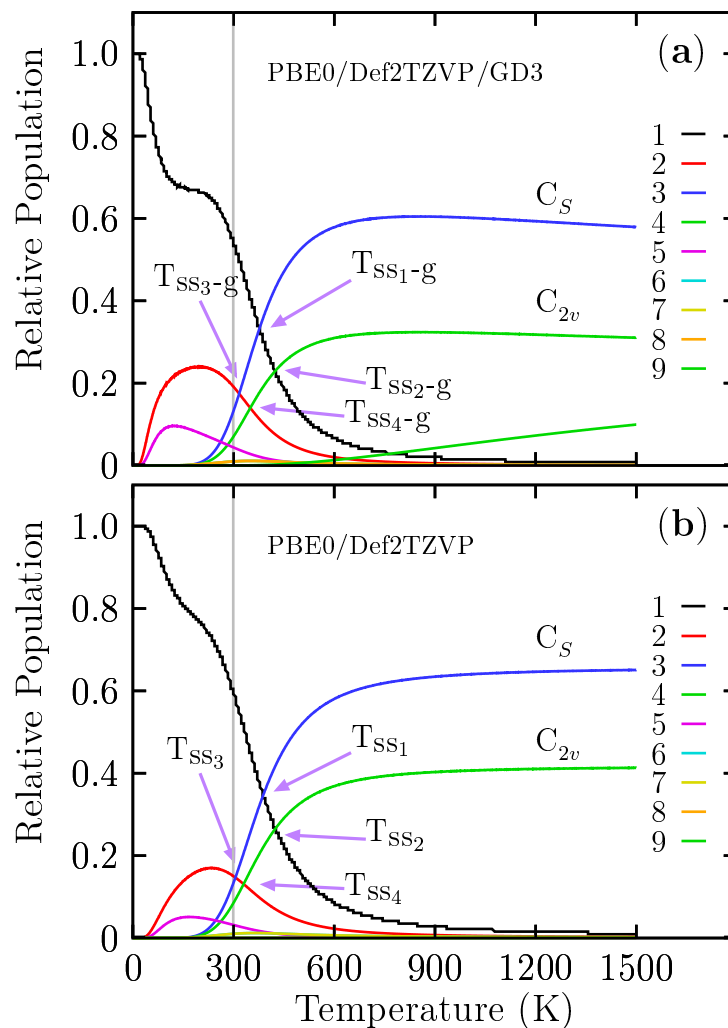


Figure 3.5: The panels shows the relative population for the temperatures ranging from 10 to 1500 K.

are located at 316.7 K, and 349 K axis temperature with relative populations 14% and 17%, respectively. These relative populations correspond to the second isomer located just 0.61 kcal/mol at 298.15 K above the global minima, and co-existing at the temperatures 316.7 K and 349 K with the coaxial Triple-Layered structures with  $C_s$ , and  $C_{2v}$  symmetries, respectively. At low temperatures range, this isomer's relative population depicted in red-solid line of Figure 4.4a is around only 20%, and up to room temperature, it decreases exponentially to zero. At temperatures up to 600 K, the relative population is zero; hence, at high temperatures these isomers do



not contribute to the molecular properties. The relative population lower than 10%, depicted in violet-solid line shows in Figure 4.4a, correspond to the isomers located at 1.48 kcal/mol above global minima at 298.15 K. Interesting, this structure is the putative minimum global when the CCSD(T) energy is employed in the ordering energetic, despite that, this structure's relative population clearly shows that this structure does not contribute to molecular properties in all ranges of temperatures. The average B-B bond length for this structure is 1.63 Å, distant for the lowest average B-B bond length of 1.53 Å. Moreover, this structure has the largest positive contribution to the relative zero-point energy. This suggests that not just the global minimum and its closest energy isomers of a potential/free energy surface are important, but also the contribution entropic effects and temperature are decisive in which isomers are going to contribute to molecular properties in a temperature ranging of interest. It should be pointed out that neither the helix-type structure reported by Guo *et al.* [3] nor the putative global minimum found in this study, also reported by Yañez *et al.* [50] at a high level of theory, is the putative global minimum when we take into account the entropic term. Our results lead to that the entropic effect should be taken into account. So far, at this point, one may ask if there is a simple and easy method to elucidate which isomers have the largest entropic contributions. This question is going to be boarded in the relative zero-point energy decomposition section. Another interesting question is: What is the effect of Grimme's dispersion (D3) on the relative population?. Figure 4.4, panel (b) shows four transitions solid-solid temperature points  $T_{\text{ss}_1}$ ,  $T_{\text{ss}_2}$ ,  $T_{\text{ss}_3}$ , and  $T_{\text{ss}_4}$ , without Grimme's dispersion (D3), and for ease of comparison displayed in round parenthesis in Table. 3.2 together with the probability of occurrence in bold and square brackets. The  $T_{\text{ss}_1}$ , and  $T_{\text{ss}_2}$  point shifts in the temperature axis to a higher temperature by 10 K, and 20K, whereas the relative population has a little variations not larger than 1.5%. The  $T_{\text{ss}_3}$ ,  $T_{\text{ss}_4}$ , and  $T_{\text{ss}_5}$  shifts to low temperature, at the first glance, it suggest that the effect of the dispersion on the relative population is a little shift of the two dominant  $T_{\text{ss}}$  points from low temperatures to higher temperatures, almost keeping the relative populations constant. In contrast with the  $T_{\text{ss}}$  points, with lower probability occurrence, shows a little shift from high temperature to lower temperatures with little changes in the relative population. The total properties in a molecule are statistical averages over the ensemble of isomers. Thus, it is crucial as far as possible to make a complete sampling of the potential energy surface to consider all isomers. The search of the low-energy structures is not straightforward, and many times this could be lead to missing some low-energy isomers. In this respect, One might well ask what happens if we have a missing low-energy structure when we compute the relative populations and their consequence on the computation of any molecular properties. Figure 3.6 shows the computed relative population when the two coaxial Triple-Layered  $C_5$  and  $C_{2v}$  structures have been taken out of the isomers pool database. Indeed, in the temperature ranging from 773 to 1500 K, the relative population depicted in yellow-solid line in Figure 3.6 indicate that the dominant structure is a distorted coaxial Triple-Layered depicted in Figure 3.3(10) and located at 9.20 kcal/mol above the putative global minimum at

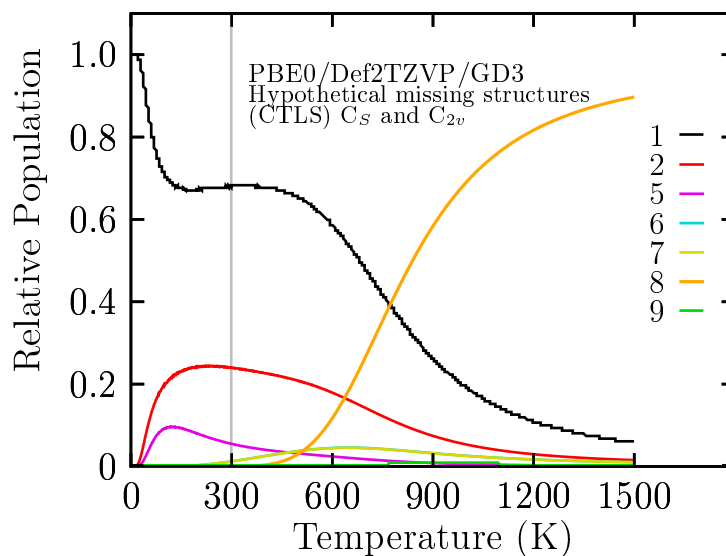


Figure 3.6: The relative population of  $\text{Be}_6\text{B}_{11}^-$  cluster.

CCSD(T) level of theory. Furthermore, analysis of results on the average B-B bond length shows in Figure 3.2 indicates that the structure with the second-lowest bond length is also the same distorted coaxial Triple-Layered structure. This result leads to a couple of interesting observations in the case of  $\text{Be}_6\text{B}_{11}^-$  cluster. Even at the high level of theory, the lowest energy structure (at  $T=0$ ) does not necessarily have the associated largest entropic effect, and the structure with the lowest B-B bond is correlated with the largest entropic effects. It is worthwhile to note that in the temperature ranging from 377 to 1500 K, in Figure 4.4 panel (a), the relative population depicted blue-solid line indicates that the coaxial Triple-Layered structures with  $C_s$  symmetry is energetically more favorable than the coaxial Triple-Layered structures with  $C_{2v}$  symmetry. Moreover, those two structures strongly dominate in this range of temperature. These results pointed out that we must consider more than one more isomer with point-group symmetries, ranging from the low-symmetry to high-symmetry. Figure 3.7 panel (a) display the relative population computed without taking into account the  $C_{2v}$  symmetry coaxial Triple-Layered structure in the pool database, and panel (b) displays the relative population computed without taking into account the  $C_{2v}$  symmetry coaxial Triple-Layered symmetry in the pool database. A Comparison between the relative population shows in panel (a) and panel (b) of Figure 3.7 indicates, on the one hand, that that dominant  $T_{ss}$  point does not shift when we do not consider the high-symmetry, and on the other hand, the dominant  $T_{ss}$  point shifts from 379 to 425 K when we no take into account the low-symmetry structure. This result leads to the observation that it is more important to calculate the relative population considering the low-symmetry structure than only structures with high symmetries. The reason is when we consider low-symmetry structures; the  $T_{SS}$  point does not change. In contrast, when we take

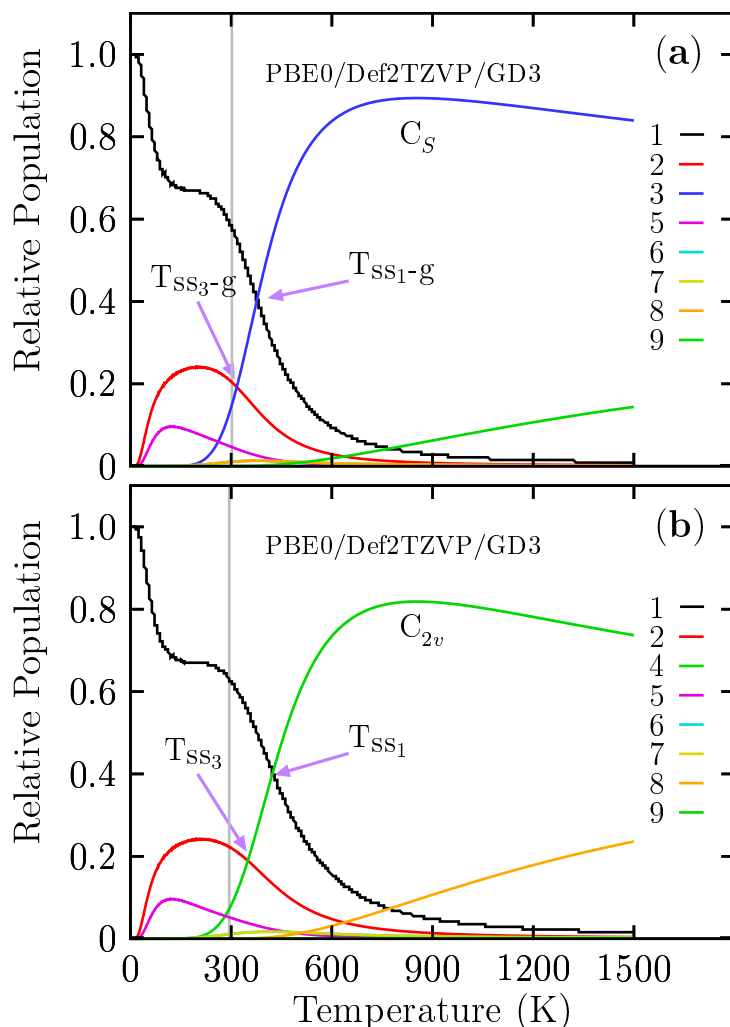


Figure 3.7: The relative population of  $\text{Be}_6\text{B}_{11}^-$  cluster.

only higher -symmetries structures, the  $T_{SS}$  shift with important consequences in the molecular properties when we compute the molecular properties as statistical averages over the an ensemble of isomers.

### 3.4.3 Relative population at CCSD(T) level of theory

Figure 3.8 shows the relative population computed at single point CCSD(T)/def2-TZVP//PBE0-D3/def2-TZVP level of theory. For temperatures ranging from 10 to 357 K, the relative population is strongly dominated by the putative global minima isomer with  $C_1$  symmetry and the relative population decreases monotonically up to 357 K. At the  $T_{ss1-c}$  point, the distorted  $C_1$  symmetry co-exist and compete with the coaxial Triple-Layered structures with  $C_s$  symmetry. The dominant structure at low tmeperatures is the lowest energy structure depicted in Figure 3.3(1) with

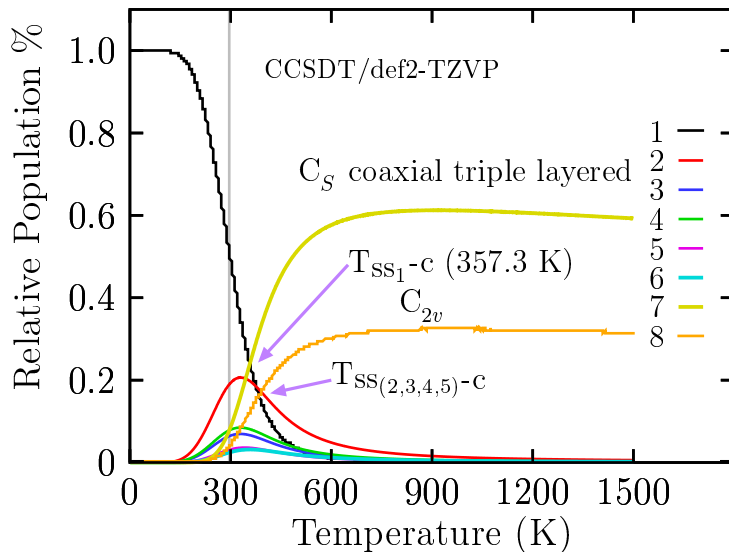
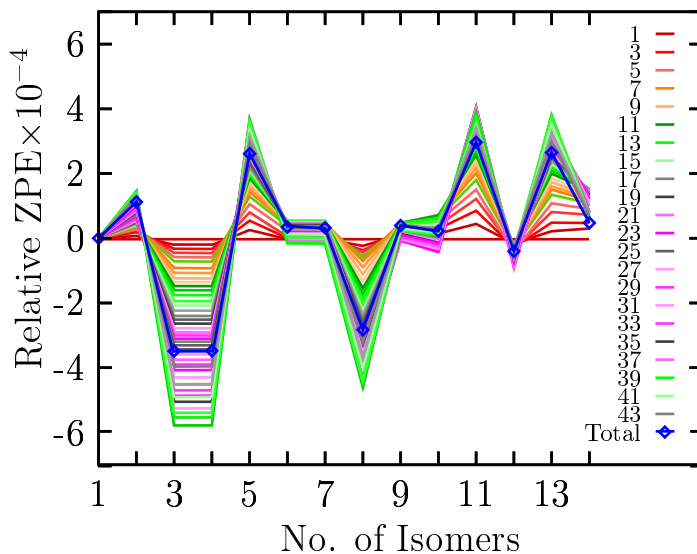


Figure 3.8: The thermal population computed at CCSD(T) level of theory.

$C_1$  symmetry at SP CCSD(T) level of theory.

### 3.4.4 Molecular Dynamics

In this study to explore and gain insights into the dynamical behavior of  $\text{Be}_6\text{B}_{11}^-$  a Born-Oppenheimer molecular dynamics (BOMD) was performed employing the deMon2K program [189] (deMon2k v. 6.01, Cinvestav, Mexico City 2011) at three different temperatures, 1600 K, 2000 K, and 2500 K, and the PBE/DZVP level of theory. We have chosen the temperatures from 1600K to 2500 K due to these temperatures are close to the melting points of boron (2349 K) and beryllium (1560 K). The BOMD's were started from the initial configuration of the coaxial-triple layered structure (the putative global minimum at a temperature of 1500 K), employing a Hoover thermal bath with random initial velocities imposed to the atoms, and for a simulation time of 25 ps with a step size of 1 fs. As the temperature increases,  $\text{Be}_6\text{B}_{11}^-$  cluster is subject to dissociation phenomena. Based on the BOMD simulation results, we found the dissociation processes of the  $\text{Be}_6\text{B}_{11}^-$  cluster occurs at a temperature of 2000 K, whereas there is no dissociation during the BOMD simulation at 1600 K; the cluster maintains its connectivity at this temperature. At a temperature of 2500 K, the dissociation processes are stronger, and more beryllium atoms are escaped. Min Li noted that nanoparticles of tungsten dissociate when the temperature of tungsten nanoparticles is higher than the melting temperature. Our results make sense if we considered that the BOMD of  $\text{Be}_6\text{B}_{11}^-$  cluster there is not dissociation at 1600 K, whereas at the temperature of 2000 K, there are dissociation phenomena. From the mentioned previously, we can infer that the melting point of the  $\text{Be}_6\text{B}_{11}^-$  cluster is in the temperature ranging from 1600 K to 2000 K.

Figure 3.9: Relative  $\mathcal{E}_{\text{ZPE}}$  decomposition.

### 3.4.5 Contributions of the vibrational modes to the ZPE energy.

At temperature zero, the lowest energy structure has the electronic energy plus zero-point energy computed as the sum of all vibration modes. If one increases the system's temperature, entropic effects start to play an important role, and Gibbs's free energy determines the lowest energy structure. The significant contribution to entropy comes from low vibrational modes, and it is approximately proportional to the logarithmic sum of low frequencies, [190] in the other hand, high vibrational modes yield small contributions to vibrational entropy. The Equation 3.2 gives the zero-point energy ( $\mathcal{E}_{\text{ZPE}}$ ), where  $\nu_i$  are all  $3N-6$  vibrational modes that the cluster possesses. Figure 3.9 shows the relative  $\mathcal{E}_{\text{ZPE}}$  as a function of vibrational modes and isomers that are arranged in energy, from the lowest (1) to the highest energy isomer (14). Remarkably, the smallest value of the total relative  $\mathcal{E}_{\text{ZPE}}$  (the minimum of  $\mathcal{E}_{\text{ZPE}}$ ) correlates with the lowest energy structure at high temperatures. The relative population displayed in Figure 4.4 panel (a) shows that the isomer three and four, that correspond to coaxial triple-layered structure with  $C_s$  and  $C_{2v}$  symmetries respectively, strongly dominate in the temperature range up to 377 K.

$$ZPE = \frac{1}{2} \sum_{i=1}^{3N-6} \nu_i \quad (3.2)$$

Figure 3.9 shows the relative  $\mathcal{E}_{\text{ZPE}}$  as a function of vibrational modes and isomers that are energetically ordered, from the lowest (1) to the highest energy isomer (14). Remarkably, the smallest value of the total relative ZPE (the minimum of  $\mathcal{E}_{\text{ZPE}}$ ) correlates with the lowest energy structure at high temperatures. The relative population displayed in Figure 4.4 panel (a) shows that the isomer three and four,

that correspond to coaxial triple-layered structure with  $C_s$  and  $C_{2v}$  symmetries respectively, strongly dominate in the temperature range up to 377 K. In Figure 3.9, one can see that isomers three and four, the coaxial Triple-Layered structures with  $C_s$  and  $C_{2v}$  symmetries possess the lowest value of the relative ZPE. Interestingly, the structures with the lowest relative  $\mathcal{E}_{\text{ZPE}}$  are correlated with the structures that strongly dominate the putative global minima at high temperatures. This suggests that those structures possess the highest entropic effects. To understand which lowest vibrational modes contribute to the lowest ZPE, we decompose the relative  $\mathcal{E}_{\text{ZPE}}$  as a function of the number of modes, adding the number of modes needed to build the smallest value of  $\mathcal{E}_{\text{ZPE}}$ . The blue-solid line in Figure 3.9 depicts the total relative ZPE employing the forty five vibrational modes, the red-solid lines depicts the relative ZPE with employing modes from first to the sixth and so on. The  $\text{Be}_6$   $B_{11}^-$  cluster posse forty five vibrational modes, we found that we have to add the lowest thirty eight vibrational modes to make the smallest value of relative ZPE. The frequency of mode thirty eight is  $1026 \text{ cm}^{-1}$ , which indicates that is the highest frequency (cutoff frequency) that contributes to making minimum relative ZPE and, therefore, those vibrational frequencies that are in the range of 46 to  $1026 \text{ cm}^{-1}$  makes the significant contribution to entropy. The vibrational modes number 39 to 45 ( $1036\text{-}1518 \text{ cm}^{-1}$ ) does not make contributions to lowering the relative ZPE, as shown in Figure 3.9

### 3.4.6 Infrared spectroscopy

In this chapter, each isomer's IR spectra and how the relative stabilities contribute to the total IR spectra are discussed. In this study, each isomer's IR spectra were computed using DFT as it is implemented in *Gaussian 09* code; under the harmonic approximation, anharmonic effects are not considered. The effect of temperature on the total spectra and the total IR spectra were computed as a Boltzmann weighted sum of each isomer's IR spectra, implemented in BOFA. As the Boltzmann factors depend on temperature, the total resulting IR spectra depend on temperature. In a previous work, [46] one of the authors computed the total dipole moment as a dipole moment weighted by the Boltzmann factors and successfully compared it with experimental data. From the experimental point of view, Sieber *et al.* [175] compared the measured absorption spectrum of the  $\text{Ag}_9$  cluster to a sum of different absorption spectra of the  $\text{Ag}_9$  cluster computed by DFT. Concerning boron clusters, the vibrational spectrum of boron cluster  $B_{13}^+$  was measured by infrared photodissociation spectroscopy and also compared with computed spectra. Experimental spectroscopy studies employing anion photoelectron spectroscopy on boron anions cluster up to  $B_{40}^-$  clusters have been done. Additionally, the structure of neutral boron clusters  $B_{11}$ ,  $B_{16}$ , and  $B_{17}$  was also probed by IR. The IR spectrum is related to vibrations that alter the dipole moment. These spectra are usually used to identify functional groups and chemical bond information, and are useful in organic/inorganic chemistry. However, from an experimental perspective, the assignment of IR bands to vibrational molecular modes can be somewhat difficult and

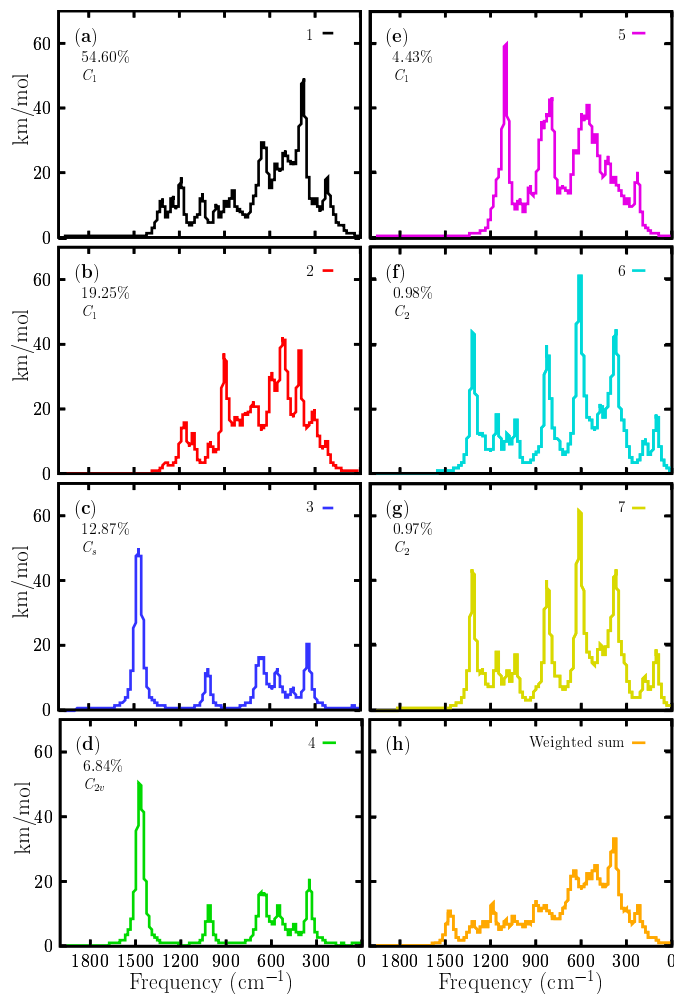


Figure 3.10: Panels (a) to (g) shows computed infrared spectra of boron clusters.

requires *ab-initio* calculations. In these computations, the temperature is generally not considered, and discrepancies between experimental and calculated IR spectra can result from finite temperature and anharmonic effects. It is also important to remember that the experiments are essential of multi-photon nature, whereas calculations IR spectra assume single-photon processes. Figure 3.10(a-g) display the individual IR spectra that belong to the putative global minima and the six lowest energy structures, respectively, located in the relative energy range up 0 to 2.38 kcal/mol at 298.15 K. Figure 3.10h shows the Boltzmann weighted spectrum at 298.15 K computed with BOFA. Interestingly, 93% of the total weighted IR spectra was found to be composed of the individuals spectral contributions of the four lowest energy structures located at an energy scale-up of 0 to 1.23 kcal/mol. The other 7% of the Boltzmann weighted spectra is composed of the IR spectra of the three structures located in the energy range from 1.48 to 2.38 kcal/mol. In the total

weighted Boltzmann IR spectrum in Figure 7h, there are three segments on its frequency axis. The first segment is located in the frequency range of 0 to 700  $\text{cm}^{-1}$ . The main bands observed in this range correspond to the IR vibrational modes of the global minimum. The highest peak is located in the 387  $\text{cm}^{-1}$  frequency axis, which corresponds to compression of the main ring formed by 10 boron atoms. It is located mainly on one side of the ring, accompanied by the vibrations of the two beryllium atoms. The second band is located at 669  $\text{cm}^{-1}$  in the frequency axis. This corresponds mainly to the 10-ring boron's small asymmetric vibration and a minor vibration of the six beryllium atoms. The third peak is located at 225  $\text{cm}^{-1}$  on the frequency axis. It corresponds mainly to a stretching of the boron atom that does not form part of the boron ring, together with the two beryllium atoms located close to the boron. The second segment is located in the frequency range of 700 to 1400  $\text{cm}^{-1}$ . In the Boltzmann weighted IR displayed in Figure 3.10h, the band observed at 900  $\text{cm}^{-1}$  is mainly composed of the 19.2% contribution of the individual IR spectrum of the second isomer that lay 0.61 kcal/mol above the global minimum; this vibrational mode of the second isomer corresponds to the stretching of the three beryllium atoms located on one side along with a boron atom, together with the stretching of one of the boron atoms. The band observed at 1200  $\text{cm}^{-1}$  (Figure 3.10h) is mainly associated with the global minima's IR spectrum, which corresponds to the boron atoms unique stretching. There is almost no vibration of the beryllium atoms. The band observed at 1500  $\text{cm}^{-1}$  (Figure 3.10h) is completely composed of the contribution of 12% of the individual IR spectra of the third isomer, which has a coaxial triple-layered structure with  $C_s$  symmetry located 0.85 kcal/mol above the putative global minima. The fourth isomer's contribution is the coaxial triple-layered structure with  $C_{2v}$  symmetry located 1.23 kcal/mol above the global minimum. The different symmetries of the coaxial triple-layered structures ( $C_{2v}$  and  $C_s$ ) are responsible for the different contributions to the total weighted IR spectrum. The low-symmetry isomers become more stable at high temperatures as a result of entropic effects. Interestingly, neither individual IR spectrum of the putative global minimum nor the individual IR spectrum of the second isomer, which was 0.61 kcal/mol above the putative global minimum, has any IR band in the range of 1500  $\text{cm}^{-1}$ . Based on this, we assigned this band at 1500  $\text{cm}^{-1}$  in the total Boltzmann weighted IR spectrum to the third and four isomers, which have a coaxial triple-layered structure with two different symmetries. The helix-type structures proposed by Guo *et al.* [3] have a small contribution to the IR spectra in all ranges of temperature. The methodology employed in this paper for the assignment of the IR bands demonstrates that the total IR spectra are a mixture of many contributions from the low-energy structures. In this cluster, the total IR spectrum's low-energy region is attributed to the putative minimum global contribution. In contrast, the high-energy region of the total IR spectrum is attributed to the isomers contribution on the high-energy axis. Figure 3.11 displays the IR spectra computed as a function of temperature. Figure 3.11a shows the total Boltzmann weighted IR spectra in the temperature range of 10 to 300 K. Note that the IR spectrum at low temperatures is strongly dominated by the individual IR spectrum of the putative



global minimum; this finding is in agreement with the relative population displayed in Figure 4.4. Below 377 K, the relative population is strongly dominated by the putative global minimum. The band observed at  $1500\text{ cm}^{-1}$  in Figure 3.11a starts

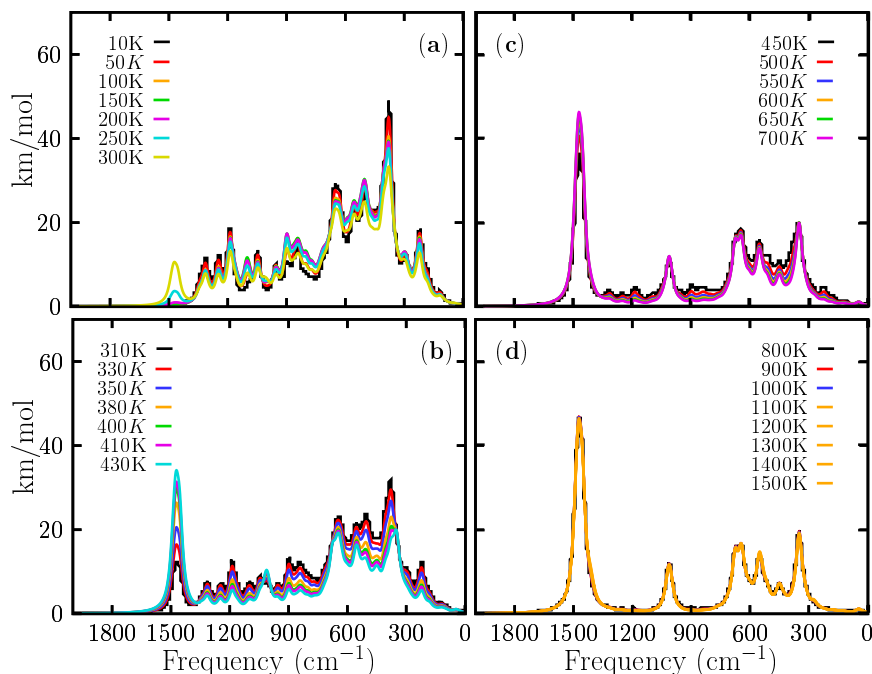


Figure 3.11: Panels (a) to (g) show the computed infrared spectra of boron clusters.

to increase at 200 K (pink line), increases again at 250 K (cyan line), and increases further at 300 K (yellow line). This IR band has contributions from the individual IR spectra of the coaxial triple-layered structures with  $C_s$  and  $C_{2v}$  symmetries. It is in complete agreement with the relative population displayed in Figure 4.4a. The relative population of the coaxial triple-layered structures start to increase at 200 K. Figure 3.11b shows the IR spectra in the range of 310 to 410 K. Within this temperature range, most transformation solid-solid point occur with different probabilities of occurrences as shown in Figure 4.4a; therefore, large changes in the total weighted IR spectra are also expected. In Figure 3.11b, the IR band located at  $1500\text{ cm}^{-1}$  continues increasing at 310 K, and it persists, increasing to 430 K (cyan line). This vibrational mode pertains to an individual IR spectrum of the isomer with coaxial triple-layered structures displayed in Figure 3.10c. This is completely in agreement with the relative population displayed in Figure 4.4. From 377 to 1500 K, the relative population is strongly dominated by the coaxial contributions of the triple-layered structures with  $C_s$  and  $C_{2v}$  symmetries. The appearance and constant growth of the peak located at  $1500\text{ cm}^{-1}$  in the weighted total IR spectrum displayed in Figure 3.11b, as a function of temperature, indicate the coexistence and competition of at least two strongly dominant structures at a specific finite

temperature (377 K). Most importantly, the constant growth of the peak located at  $1500\text{ cm}^{-1}$  is indicative that putative global minimum interchange occurs as a function of temperature. This suggests that we must search exhaustively and systematically for the putative global minimum on the potential/free energy surface and its full distribution of all low-energy structures if we want to assign IR bands to specific vibrational modes. This paper shows how some IR bands in the Boltzmann weighted total IR spectrum belong to the IR spectra of isomers located on the higher energy axis. In summary, in the Boltzmann weighted total IR spectrum shown in Figure 3.11b, the low-frequency range is dominated by the contributions of the putative global minimum, whereas the high-frequency range is dominated by geometric structures located at higher energies. Figure 3.11b shows the IR spectra in the range of 310 to 410 K. Within this temperature range, most solid-solid transitions occur with different probabilities, as shown in Figure 4.4a; therefore, large changes in the total weighted IR spectra are also expected. In Figure 3.11b, the IR band located at  $1500\text{ cm}^{-1}$  continues increasing at 310 K, and it persists, increasing up to 430 K (cyan line). This vibrational mode pertains to an individual IR spectrum of the coaxial triple-layered isomer displayed in Figure 3.10c. This is completely in agreement with the relative population displayed in Figure 4.4a. The peak located at  $1500\text{ cm}^{-1}$ , shows in Figure 3.11, panels (a-d), is present only in temperatures higher than 300 K, where the coaxial-triple layer structures start to be the lowest energy structures. The abovementioned reasons indicate that the vibrational modes located in the range of  $1036$  to  $1518\text{ cm}^{-1}$  are responsible for the cluster's fluxionality. The B-B stretching modes of the  $B_{11}$  ring are located in the range of  $1036$  to  $1518\text{ cm}^{-1}$ . This is correlated to hyperconjugation, delocalization, and fluxionality of the cluster.

### 3.5 Conclusions

In summary, we systematically explored the potential and free energy surface of the  $Be_6B_{11}^-$  cluster using an unbiased hybrid, efficient, and multistep/multilevel algorithm implemented in Python and coupled to density functional theory. The temperature effects were considered employing Gibb's free energy. If the system's temperature is increased, entropic effects start to play an important role, and Gibbs's free energy determines the lowest energy structure.



# The $\text{Be}_4\text{B}_8$ cluster

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## 4.1 Abstract

The lowest-energy structure, distribution of isomers, and their molecular properties depend significantly on the geometry and temperature. The total energy computations under DFT methodology are typically carried out at zero temperature; thereby, entropic contributions to total energy are neglected, even though functional materials work at finite temperature.

In this chapter, the probability of occurrence of one particular  $\text{Be}_4\text{B}_8$  isomer at temperature  $T$  is estimated within the framework of quantum statistical mechanics and nanothermodynamics. To locate a list of all possible low-energy chiral and achiral structures, an exhaustive and efficient exploration of the potential/free energy surface is done by employing a multilevel multistep global genetic algorithm search coupled to DFT. Moreover, we discuss the energetic ordering of structures computed at the DFT level against single-point energy calculations at the CCSD(T) level of theory. The computed VCD/IR spectrum of each isomer is multiplied by their corresponding Boltzmann weight at temperature  $T$ ; then, they are summed together to produce a final Boltzmann weighted spectrum. Additionally, we present chemical bonding analysis using the Adaptive Natural Density Partitioning method in the chiral putative global minimum. The transition state structures and the enantiomer-enantiomer and enantiomer-achiral activation energies as a function of temperature, evidence that a change from an endergonic to an exergonic type of reaction occurs at a temperature of 739 K.

## 4.2 Introduction

The potential of boron atom to form stable molecular networks [191, 131] lies in the fact that it has three valence electrons and four available orbitals, which implies it is electron deficient. Moreover, it has a small covalent radius of 0.8-1.01 Å [192, 193], high ionization energy 344.2 kJ/mol [192], and an affinity for oxygen atoms, which is the basis of borates [194, 192]. Boron electron deficiency gives origin to vast number of allotropic forms and uncommon geometries [102, 110, 131] such as nanotubes, [117, 28] borospherenes [119], borophene [110], cages [28, 120], planar [115], quasi planar [86], rings [177, 138], chiral [116, 195], boron-based helix clusters [3, 121], and fluxional boron clusters [3, 144] that have recently attracted the interest of experimental and theoretical researchers. Since the molecular properties depend greatly on their geometry and temperature [16, 1]; boron cluster ex-

hibit a large number of molecular properties that yield potential applications in medicine [109, 125, 196, 197], molecular motors [147, 3], superhard materials [198], hydrogen storage [199], batteries [200, 201, 202, 203], catalysis [204], and energy materials [205] among many others.

Particularly, the chirality of nanoclusters has attracted attention due to their chiroptical properties, potential application in efficient chiral discrimination [82, 83], nonlinear optics [84] and chiral materials with interesting properties, [85, 86, 87] and of course, not to mention that chiral structures play a decisive role in biological activity. [88]

Previous theoretical studies joint with experimental photoelectron spectroscopy reported the first pure boron chiral  $\text{B}_{30}^-$  structure as the putative global minimum. [86] In these pair of planar enantiomers, the chirality arises due to the hexagonal hole and its position. A year later, the lowest energy structures of the  $\text{B}_{39}^-$  borospherene were reported as chiral due to their hexagonal and pentagonal holes. [118] Similarly, the  $\text{B}_{44}$  cluster was reported as a chiral structure due to its nonagonal holes. [195] That is, in these clusters, holes in the structure cause chirality. Regarding beryllium-doped boron clusters, they exhibit remarkable properties such as fluxionality, [3, 206, 207, 110, 208, 209] aromaticity, [3, 210] and characteristics similar to borophene. [107] Furthermore, previous theoretical studies showed that the boron fullerenes  $\text{B}_{60}$  and  $\text{B}_{80}$  can be stabilized by surrounding the boron clusters with beryllium atoms, [211, 212] which effectively compensates for boron electronic deficiency. [212] These effects make beryllium-doped boron clusters interesting.

Particularly attractive are the chiral helices  $\text{Be}_6\text{B}_{11}^-$ , reported by Gou *et al.* [3], Yanez *et al.*, [50] and Garcia-Buelna *et al.* [1] as one of the low-lying and fluxional isomers, and later a chemical bonding and mechanism of formation study of the beryllium-doped boron chiral cluster  $\text{Be}_6\text{B}_{10}^{2-}$  and coaxial triple-layered  $\text{Be}_6\text{B}_{11}^-$  sandwich structure were reported. [121, 209] In these structures, the chirality arises due to the formation of a boron helix.

However, there are only a few theoretical studies on vibrational circular dichroism (VCD) and infrared spectroscopy (IR) as a function of temperature in beryllium-boron clusters [213, 1]. We emphasize that there are neither theoretical nor experimental studies of VCD / IR spectra in chiral  $\text{Be}_4\text{B}_8$  clusters, although VCD/IR spectra give insight into the geometrical structure. [214, 215, 216, 217] Recently, Castiglioni *et al.* reviewed experimental aspects of solid-state circular dichroism, [218] and Avilés Moreno *et al.* reported the experimental and theoretical IR/VCD spectra of various compounds. [219, 220, 221, 222] VCD is differential spectroscopy sensitive to the difference in the absorption for the left and right polarized light. [214, 223, 217] It usually is four times in magnitude smaller than IR absorption [224] and yields information on the lowest energy conformation in solution; [225] thus, the chiral molecule's absolute configuration can be determined employing the VCD spectra. [226]

The IR frequencies are related to the second derivative of the potential energy and they are useful in identifying transition states and computing thermodynamics through the vibrational partition function. [1, 58, 178] Additionally, the structure

of neutral boron clusters  $B_{11}$ ,  $B_{16}$  and  $B_{17}$  was probed by IR. [146]. The DFT VCD/IR spectra depend on the functional and basis set employed [216] and significantly on the lowest- and the low-energy achiral and chiral structures, so we need an efficiently sampling of the free energy surface to know the distribution of isomers at different temperatures. [2, 1, 16, 65, 64, 63] A considerable change in the isomer distribution and the energetic separation among them is the first notable effect of temperature. [1, 2] Useful materials work at finite temperatures; in that conditions, Gibbs free energy is minimized [56] and determines the putative global minimum at given temperature, [1] whereas, entropy of the atomic cluster is maximized. [56] Although in the mid 1960's, Mermin *et al.* [227] studied the thermal properties of the inhomogeneous electron gas, most of DFT calculations are typically performed at zero temperature. Recently, over again, DFT was extended to finite temperature, [228, 229, 230] but nowadays, as far as we know, it is not implemented in any software. However, molecular dynamics and other simulation tools have been employed to study atomic clusters at finite temperatures. [106, 155, 231, 101, 52, 165] In this study, based on the Gibbs free energy of each isomer and Boltzmann factors, we computed the probability of occurrence (Boltzmann weights) of each particular isomer of  $Be_4B_8$  as a function of temperature using quantum statistical mechanics. The computed VCD/IR spectrum of each isomer is multiplied by their corresponding Boltzmann weight at temperature  $T$ ; then, they are summed together to produce a final Boltzmann weighted spectrum. In the mid 1980, P. J. Stephens with co-workers implemented the atomic axial tensors in Gaussian 80 code that allows them to compute the VCD spectrum of propylene oxide and compare with the experimental spectrum [232] Later, Nafie and Stephens employed the Boltzmann weights scheme, they computed the VCD spectrum for each isomer, and the total resulting spectra were averaged and weighted by Boltzmann factors. [233, 214, 234, 235] Recently these factors were used in other previous works. [65, 1, 64, 228, 63].

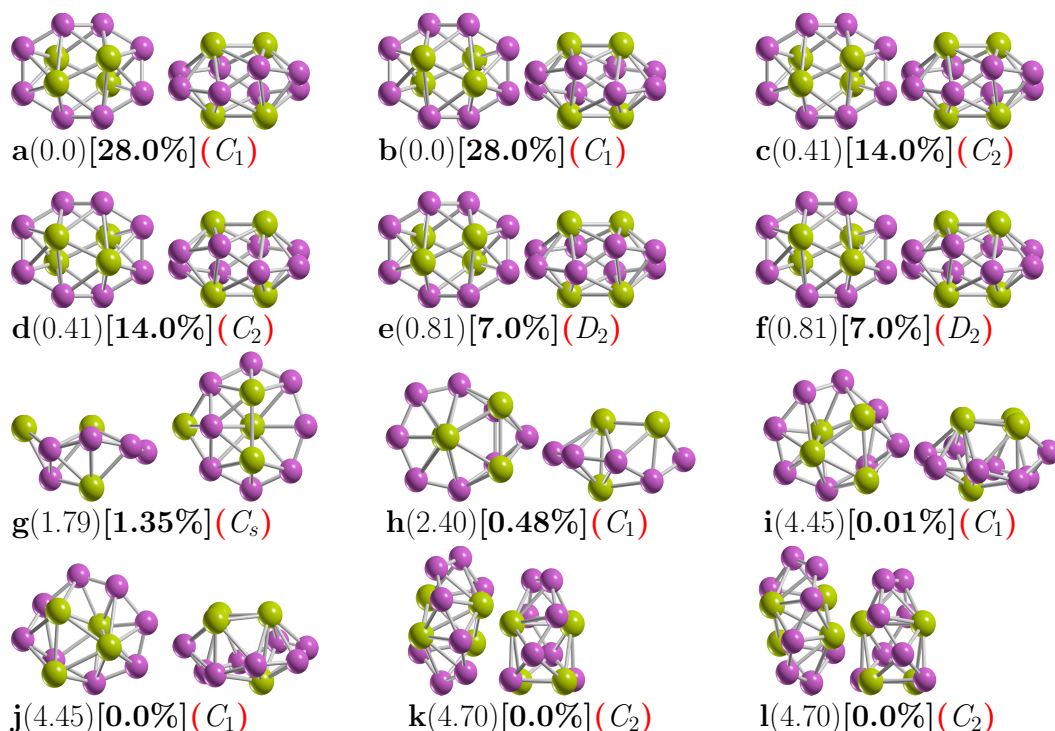
To achieve the mentioned above, we located all low-energy structures on the potential and free energy surfaces of the  $Be_4B_8$  cluster with a genetic algorithm coupled to DFT and computed the Boltzmann weights in temperatures ranging from 20 to 1900 K. We also located the solid-solid transformation point at 739 K, where chiral and achiral structures coexist, and computed the energy barrier ( $E_a$ ) for temperatures ranging from 20 to 1900 K for transformation of enantiomers (plus,  $\mathcal{P}$ ) to an achiral structure. We locate the  $T_{ee}$  point is defined here as the temperature where the reaction change from endergonic to exergonic. Moreover, the energy of enantiomerization was computed between  $\mathcal{P}$  and minus ( $\mathcal{M}$ ) enantiomers, and we defined the  $T_{bb}$  point in scale temperature where the energy barrier of two possible reaction mechanisms is equal to each other, which implies the velocity of the reaction is equal for both mechanisms. We investigated how the symmetry point group affects the Gibbs free energy. Our results show that the chirality on  $Be_4B_8$  arises from the Be-Be dimers capping the boron ring and also of the distorted boron ring, thus, the lowest energy chiral structure is favored by the interaction between beryllium and the boron framework. The high energy of enantiomerization of the  $Be_4B_8$  cluster in temperatures ranging from 20 to 1900 K suggests that it is a good candidate for

applications; only one of the enantiomers shows the desired effect. The computed enthalpy of formation ( $\Delta H$ ) between chiral and achiral structure at 739 K show that there is a change from endo to exothermic reaction. Our results indicate that the Boltzmann weighted VCD spectrum is zero in all range of temperature, whereas, the Boltzmann IR weighted spectrum is strongly dominated by the lowest energy pair of enantiomers. The remainder of the chapter is organized as follows: the computational details and a brief overview of the theory and the algorithms used. The results and discussion are presented next. We discuss the effect of the symmetry in the energetic ordering and clarify the origin of the 0.41 kcal/mol difference energy between two structures with symmetries  $C_2$  and  $C_1$  that appear when we compute the Gibbs free energy. A comparison among energies computed at a single point CCSDT against DFT levels of theory and the  $\mathcal{T}_1$  diagnostic is presented. We do the chemical bonding analysis by employing the AdNDP scheme to  $\mathcal{P}$  minimum energy structure. The interconversion energy barrier between the  $\mathcal{P}$  and  $\mathcal{M}$  enantiomers and between an achiral structure and  $\mathcal{P}$  enantiomer are discussed in terms of temperature. IR spectra are analyzed as a function of temperature, and conclusions are given.

## 4.3 Results and discussion

### 4.3.1 The lowest energy structures and energetics

Figure 4.1 shows the low-energy configurations of  $\text{Be}_4\text{B}_8$  clusters optimized at PBE0-GD3/def2-TZVP level of theory taking into account ZPE energy correction. The optimized average B-B bond length of the putative chiral global minimum is 1.5867 Å, in good agreement with an experimental bond length of 1.57-1.59 Å. [185, 186] and also within agreement with others previous DFT calculations. [1] The most recurring motif within the lower energy isomers of  $\text{B}_8\text{Be}_4$  is a sandwich structure, (SSh) in which the boron atoms form a hollow distorted ellipsoid ring with each of the Be-Be dimers capping the top and bottom with  $C_1$  point group symmetry. Isomers *a* and *b* and also listed as  $i_1$  and  $i_2$  in Table 4.1, are enantiomers differing in the orientation of the Be-Be dimers with respect the boron skeleton. Based on the B-B bond length evolution along the intrinsic reaction coordinate (IRC) between Plus-enantiomer-Minus-enantiomers, and displayed in Figure B.2 appendix B.2 the shortest B-B bond length is located at the transition state structure. In contrast, the largest B-B bond length is located in the reactant and product points. On the other hand, appendix Figure B.2 appendix B.2 shows the distance evolution between (Be-Be)-(Be-Be) dimers; one can see the largest distance between dimers is located at the transition state, whereas the shortest distance is located at the product and reactants points. From the above mentioned, the B-B interaction does not favor the formation of the lowest energy enantiomers structures; meanwhile, the Be-Be interaction promotes the lowest energy structure to be chiral. Here, we infer that the Be-B interaction also favors the chiral lowest energy structures. The Be-Be bond length for the six lowest energy enantiomers is

Figure 4.1: Optimized geometries of neutral  $\text{Be}_4\text{B}_8$  cluster.

1.9874, 1.9876, and 1.9881 Å for symmetries  $C_1$ ,  $C_2$ , and  $D_2$ , respectively, in good agreement with the bond length of the Be-Be in  $\text{Be}_2\text{B}_8$  cluster 1.910 Å. [207] To gain more insight into the chemical bonding, an AdNDP analysis of the lowest energy isomer was performed (Figure 4.2). The AdNDP analysis for this chiral structure revealed the presence of eight 2c-2e B-B  $\sigma$ -bonds with an occupation number (ON) between 1.92 and 1.94 |e| and three delocalized  $\sigma$ -bonds throughout the  $\text{B}_8$  ring with an ON between 1.95 and 1.99 |e|. Additionally, three distorted  $\pi$ -bonds (due to the non-planarity of the structure), one of which is delocalized over all eight boron atoms and the other two involving four boron and two beryllium atoms (one from the top and one from the bottom). Finally, the bonding pattern is completed by two 6c-2e  $\sigma$ -bonds with main contribution coming from the interaction between the two Be atoms from the top and bottom, respectively. The isomers with symmetry  $C_1$  are the most energetically favorable, with 28% each of the Boltzmann population at 298.15 K. An exhaustive and systematic exploration of the potential energy surface considering triplet states revealed that the lowest triplet ground state lays 13.7 kcal/mol above the singlet putative chiral global minimum single ground state, which is too far away energetically to be considered. Next, low-energy SSh-isomers labeled  $i_3$  and  $i_4$  in Table 4.1, and depicted in Figure 4.1(3,4) lies just 0.41 kcal/mol above the putative global minimum, it is a similar-SSh structure than the putative global minimum, only with  $C_2$  point group symmetry, followed by slightly



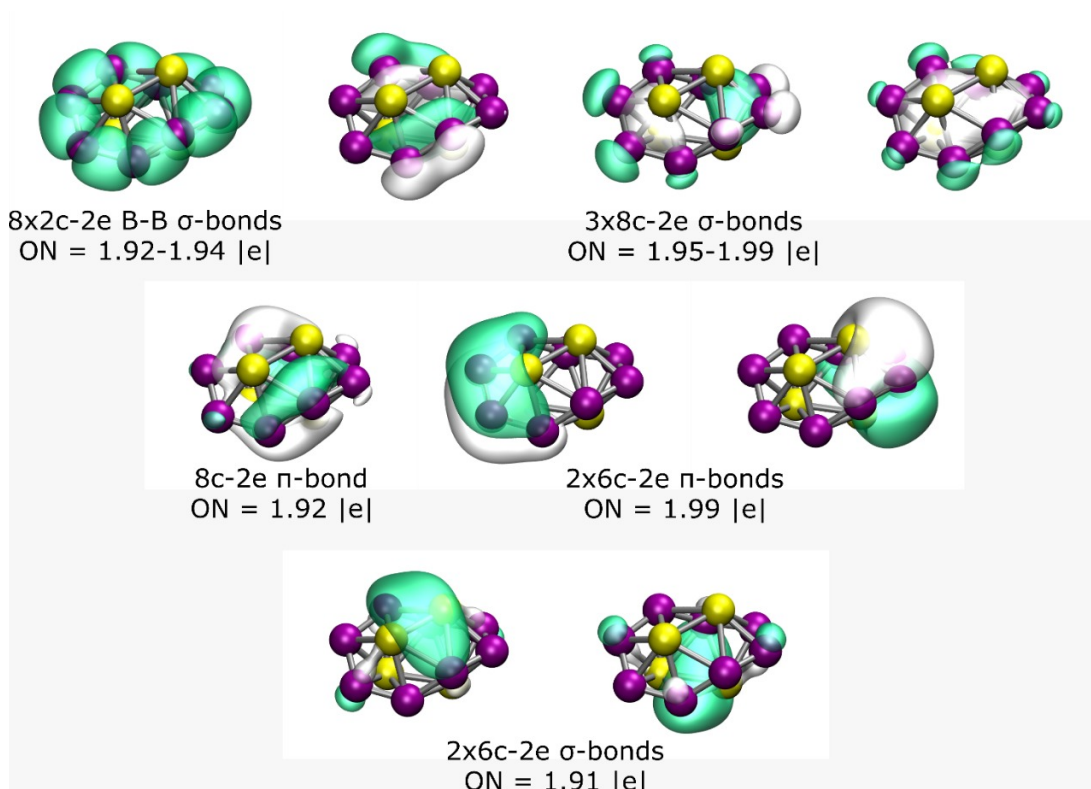


Figure 4.2: Results of the AdNDP analysis of the lowest-energy chiral isomer of the  $\text{Be}_4\text{B}_8$  system.

higher energy and similar-SSh structure located just 0.81 kcal/mol above the putative minimal structure with  $D_2$  point group symmetry. We point out that the unique differences among these chiral structures are the different symmetry point groups. The most energetically favorable is the non symmetry ( $C_1$ ) cluster; moreover, these six structures contribute to 98% to the relative population at 298.15 K. The next higher energy structure, labeled as  $i_7$  in Table 4.1 and depicted in Figure 4.1(g), is located at 1.79 kcal/mol above the putative minimum global at 298.15 K, with symmetry  $C_s$ . It is also a sandwich structure formed by a distorted circular ring in which one of the Be-Be dimers is capping in the center of the ring, and the other one is located on one face of the boron circular ring. This structure is achiral, and its probability of occurrence is 1.35% at 298.15 K. Next achiral isomer lies 2.40 kcal/mol above the putative minimum global with  $C_1$  symmetry, labeled as  $i_8$  in Table 4.1 and depicted in Figure 4.1(8). It is also a sandwich-type structure formed by a distorted circular boron ring with three boron atoms capping one side of the ring and the other Be atom capping the other. The probability of occurrence of this isomer at 298.15 K is just 0.48% and its contribution to chiroptical spectroscopies is negligible. The next two chiral structures lies 4.45 kcal/mol above the putative global minimum with  $C_1$  symmetries, labeled as  $i_9$  and  $i_{10}$  in Table 4.1 and de-

Table 4.1: Single point relative energy calculations of the low energy structures at different levels of theory.

Level	Isomers									
	$i_1$	$i_2$	$i_3$	$i_4$	$i_5$	$i_6$	$i_7$	$i_8$	$i_9$	$i_{10}$
$\Delta G$	0.0	0.0	0.41	0.41	0.81	0.81	1.79	2.40	4.45	4.45
CCSDT	0.0	0.0	0.0	0.0	0.0	0.0	3.61	3.38	5.38	5.38
CCSDT+ $\mathcal{E}_{\text{ZPE}}$	0.0	0.0	0.0	0.0	0.0	0.0	2.71	2.51	4.51	4.51
DLPNO-CCSD(T)	0.0	0.0	0.0	0.0	0.0	0.0	0.75	1.37	5.0	5.0
DLPNO-CCSD(T)+ $\mathcal{E}_{\text{ZPE}}$	0.0	0.0	0.0	0.0	0.0	0.0	-0.20	0.50	4.10	4.10
$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.0	0.0	0.0	0.0	0.0	0.0	2.38	2.80	5.03	5.03
$\mathcal{E}_0$	0.0	0.0	0.0	0.0	0.0	0.0	3.28	3.68	5.90	3.28
Point group symmetry	$C_1$	$C_1$	$C_2$	$C_2$	$D_2$	$D_2$	$C_s$	$C_1$	$C_1$	$C_1$
$\mathcal{T}_1$ Diagnostic	0.019	0.019	0.019	0.019	0.019	0.019	0.016	0.015	0.016	0.016

pictured in Figure 4.1(i,j). They are sandwich-type structures formed by a non-planar distorted circular boron ring with three Be atoms capping one side of the boron ring and the other Be atom is located on the other face, and in the center of the distorted boron ring; Its Boltzmann probability of occurrence is zero at 298.15 K, so as a consequence, at this temperature, its contributions to any chiroptical spectroscopies are negligible. The following chiral higher energy structure, with  $C_2$  point group symmetry, lies 4.70 kcal/mol energy above the putative global minimum. It is a chiral helix type structure depicted in Figure 4.1(12,13); it has four Be atoms located in the center of the boron spiral, this helix structure is similar to those found by previous theoretical works [3, 50, 1] and its probability of occurrence is negligible at room temperature. To gain insight into the energy hierarchy of isomers and validate our DFT calculations, relative energies were computed at different levels of theory, and differences between them are shown in Table 4.1. Energy computed at different methods yield different energies due mainly to the functional and basis-set employed, [236, 2], so the energetic ordering change; consequently, the probability of occurrence and the molecular properties will change. The first line of Table 4.1 shows the relative Gibbs free energy computed at PBE0-GD3/def2-TZVP and room temperature. The small relative Gibbs free energies (0.41, and 0.81 kcal/mol) differences among the six enantiomer structures  $i_1$  to  $i_6$  in Table 4.1 are caused by the rotational entropy being a function of the symmetry number that in turn depends on the point group symmetry. An increase/decrease in the value of rotational entropy changes the Gibbs free energy. The Gibbs free energy computed with and without symmetry will differ by a factor  $RT\ln(\sigma)$ . Here, R is the universal gas constant, T, the temperature, and  $\sigma$  is the symmetry number. Figure 5.3 shows the factor  $RT\ln(\sigma)$  for temperatures ranging from 0 to 1900 K and for different symmetry number values ( $\sigma=2,3,4,5$ ). A closer analysis of Figure 5.3, shows that at room temperature  $RT\ln(\sigma)=0.41$  kcal/mol with  $\sigma=2$ , and  $RT\ln(\sigma)=0.81$  kcal/mol with  $\sigma=4$ , in agreement with the values shown in the first line of Table 4.1. As the temperature increases, the energy differences between the factors  $RT\ln(\sigma)$  be-

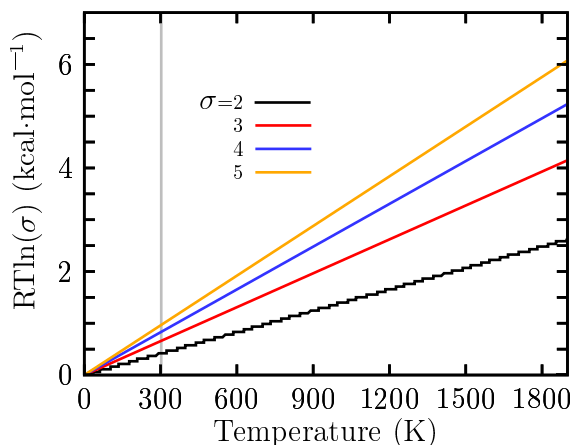


Figure 4.3: The difference of the rotational entropy with and without symmetries.

come larger. These small relative Gibbs free energies are responsible for different values of probability of occurrence at low temperatures for the similar isomers with different point group symmetry. This strongly suggests that there must be atomic clusters with low and high symmetries in the Boltzmann ensemble to compute the molecular properties correctly. The second line in Table 4.1 shows single point (SP) relative energies computed at the CCSD(T)[237], the energetic ordering of isomers listed in the first line of Table 4.1 follows almost the trend of energetic ordering at SP CCSD(T) level, notice that just the achiral isomers label  $i_7$  to  $i_8$  in Table 4.1 are interchanged in energetic ordering. The third line Table 4.1 shows single point relative energies computed at the CCSD(T)[237]/def2-TZVP//PBE0-GD3/def2-TZVP; the energetic ordering is similar to pure CCSD(T) energy. DLPNO-CCSD(T)) relative energies, with and without ZPE correction, are shown in lines four and five of Table 4.1, the first follows the trend of pure CCSD(T) energy, and the second, the ZPE value, interchange the isomers, label  $i_7$  in Table 4.1, to be the putative global minimum. Here we can say that the ZPE energy inclusion is essential in distributing isomers and molecular properties. The sixth and seventh lines of Table 4.1 show the electronic energy with and without ZPE correction, and both of them follow the trend of the Gibbs free energy given in line number one. Line number 8 in Table 4.1 shows the point group symmetry for each isomer. The  $T_1$  diagnostic for each isomer is shown inline nine of Table 4.1, all of them are lower than the recommended value 0.02 [237, 238] so the systems are appropriately characterized.

#### 4.3.2 Structures and Stability at Finite Temperature.

As we mentioned earlier, the determination of the structure is the first step to study any property of a material. Moreover, we have to consider that an observed molecular property in a Boltzmann ensemble is a weighted sum of all individual contributions of each isomer that form the ensemble. At temperature 0 K, the elec-

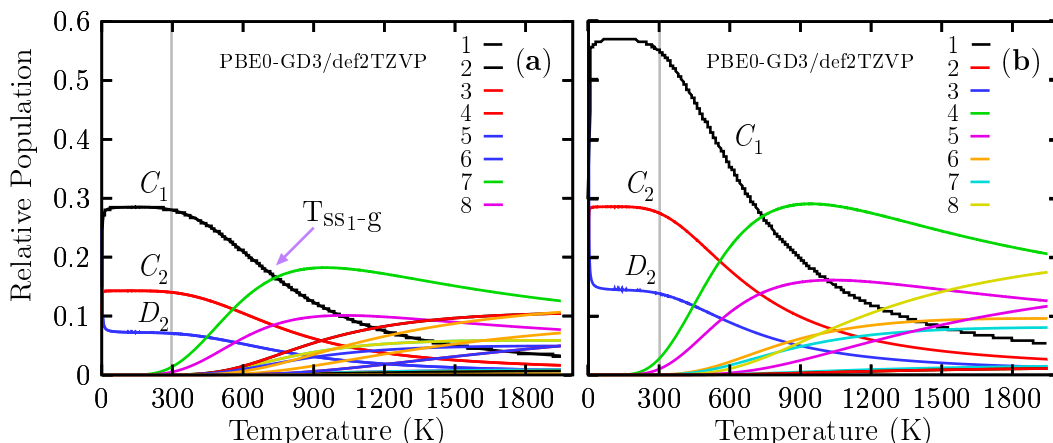


Figure 4.4: The left panels shows the probability of occurrence for temperatures ranging from 20 to 1900 K.

tronic energy plus zero-point energy determine the putative global minimum and all nearby low-energy structures (PGMLES), whereas, at temperatures larger than 0 K, the Gibbs free energy defines the PGMLES. Figure 4.4 shows the probability of occurrence for each particular chiral and achiral  $\text{Be}_4\text{B}_8$  isomers for temperatures ranging from 20 to 1900 K. In panel (a) the probability of occurrence is shown, taking into account the  $\mathcal{M}$ ,  $\mathcal{P}$ , and achiral structures, which implies Boltzmann racemic ensemble (the percent enantiomeric excess is zero (Boltzmann racemic ensemble). whereas panel (b) shows the probability of occurrence only taking into account just the  $\mathcal{M}$  handled and achiral structures, which implies that the percent enantiomeric excess is 100%. then the ensemble is a Boltzmann pure ensemble of only one type of enantiomer. There is a significant difference in the probability of occurrence between the two panels. In panel (a), we consider the  $\mathcal{P}$  and  $\mathcal{M}$  structures, and both structures possess the same probability of occurrence in all ranges of temperature. All the probabilities of occurrence (chiral) shown in panel (b) are approximately two times the probability of occurrence (chiral) shown in panel (a). A closer examination of the panel (a) shown that in the temperature ranging from 20 to 300 K, all molecular properties are dominated by chiral structure depicted in Figure 4.1(a,b) because its probability of occurrence is almost constant. We point out that in this range of temperature, the  $C_1$ ,  $C_2$  and  $D_2$  symmetries strongly dominate with different probabilities of occurrence of 28, 14 y 7% respectively. This different probability of occurrence for the same structure with only different symmetries is due to rotational entropy, that also is responsible for those slight energy differences shown in Table 4.1 and, in turn, it is the reason for the differences in the probability. At temperatures above 300 K, the probability of occurrence of the putative global minimum at cold temperatures and depicted in solid-black line decay exponentially up to 1900 K. The dominant transformation solid-solid point ( $T_{\text{ss1-g}}$ ) is located at 739 K with 16.6% of probability. At this point, there is a co-existence of chiral structures and

achiral structures, shown in Figure 4.1(a,g), above this point the achiral structure (Figure 4.1(g)) become dominant. Its probability of occurrence is depicted in the solid-green line in Figure 4.4a and start to grow up at almost at room temperature. The second transformation solid-solid point located at 1017 K and 10% of probability also coexist the chiral putative global minimum with symmetry C<sub>1</sub> and achiral structure (Figure 4.1(h)) located at 2.40 kcal/mol Gibbs free energy at 298.15 K above the putative global minimum. Figure 4.4b shows the computed probability of occurrence considering the percent enantiomeric excess is one hundred percentage, which implies of a pure Boltzmann ensemble of only one type of enantiomer. With the aim to compute the Boltzmann VCD/IR weighted spectra as a function of temperature, we take the relative population shown in Figure 4.4a. The probability of the dominant achiral putative global minimum with symmetry C<sub>1</sub> is depicted in the solid-green line in Figure 4.4a. Analysis of the probability of occurrence leads to an interesting observation: The individual putative minimum global strongly dominates the VCD/IR at a temperature ranging from 20 to 1240 K. The achiral structures have a zero contribution to VCD in hot temperatures. The probability of occurrence is dependent on the functional and basis set employed as a result of those energies computed at different methods provides different energies [236] Figure B.1 shows the relative population computed at TSPP [239]-GD3/def2-TZVP level of theory. At cold temperatures, strongly dominate the chiral structure with symmetry C<sub>1</sub> and depicted in Figure 4.1(a,b). At hot temperatures, the dominant structure is a chiral helix-type structure depicted in Figure 4.1(k,l) located at 4.70 kcal/mol Gibbs free energy above the putative global minimum. Also, at SP CCSD(T) level, it is located at high energy above the global minimum. The relative population employing this functional does not follow the trend of energetic ordering at CCSD(T) level of theory. The above discussion shows that the probability of occurrence is sensitive to the functional.

### 4.3.3 Enantiomerization Energy Barrier at Finite Temperature.

The process in which pair of chiral molecules or enantiomers undergo to the conversion of one enantiomer into the other is referred to as enantiomerization. Enantiomers each have the same free energy and equal probability of occurrence, as shown in Figure 4.4 The extent of interconversion of enantiomers depends on the energy barriers to enantiomerization. Moreover, this energy barrier determines if an enantiomer can be resolved at temperature T and defines its configurational stability. There are cases where the enantiomerization is undesirable; for example, many drugs are related to chirality, and frequently only one of the enantiomers shows the desired effect while the other shows undesirable effects, moreover chiral molecules with high charge-carrier mobility and fluorescence quantum yield needs high energy barriers of enantiomerization. [240]

Figure 4.5a shows the computed enantiomerization energy barrier (energy activation ( $E_{ae}$ ) or Gibbs free activation energy ( $\Delta G^\ddagger$ )) of the pair of enantiomers  $\mathcal{P}$  and  $\mathcal{M}$  of Be<sub>4</sub>B<sub>8</sub> cluster that has only a single-step for two mechanisms of reaction

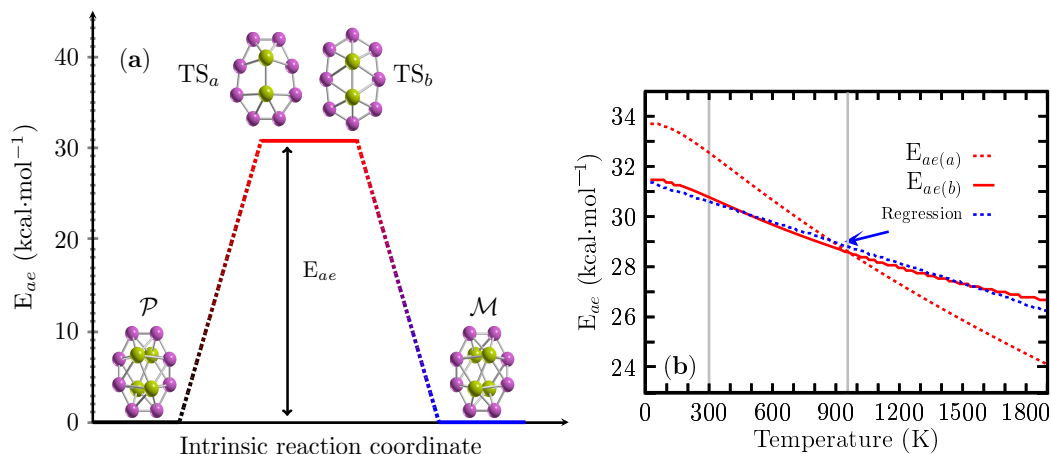


Figure 4.5: There are two transition states close in energy,  $TS_a$  and  $TS_b$ .

whose energy barriers are energetically similar. The transition states ( $TS_a$ ,  $TS_b$ ) depicted in Figure 4.5a, are achiral sandwich-type structures in which the borons form a planar ring with each of the Be-Be dimers capping the top and bottom, and they are aligned parallel to the major axis of the boron ellipse. The main difference between both of them is a shift of ring position concerning the Be-Be dimers. The energy barriers of  $TS_a$  and  $TS_b$  are 32.50 and 30.77 kcal/mol, respectively, and indicates that  $Be_4B_8$  enantiomers are stable at room temperature. Those energy barriers height are similar to that of computed energy barrier height in  $Au_{38}(SR)_{24}$ , [241] clusters that lie in the range of 29.9 to 34.5 kcal/mol. The energy of enantiomerization,  $E_{ea(a)}$  and  $E_{ea(b)}$  corresponding to the  $TS_a$  and  $TS_b$  for temperatures ranging from 20 to 1900 K are displayed in Figure 4.5b respectively. The  $E_{ea(a)}$  is depicted in a red dashed line, whereas the  $E_{ea(b)}$  is depicted in a red solid line. Analysis of the results leads to an interesting observation: In Figure 4.5b, one can see that there is a barrier-barrier temperature point ( $T_{bb}$ ) located at 954 K where the energy barriers of both mechanisms are equal to each other. At  $T_{bb}$ , the probability that reaction takes one path or another is 50/50% which implies that the velocities of reaction for both reaction mechanism are equal to each other. Below the temperature of 954 K, the reaction path b ( $TS_b$ ) is more favorable than reaction path a ( $TS_a$ ), and vice-versa for temperatures above 954 K. In Figure 4.5b. is shows that the energy barrier  $E_{ea(b)}$  decreases linearly in the temperature range from 200 to 740 K. Below 200 K and in temperatures ranging from 740 to 1900 K; the energy barrier behavior is non-linear. To make it clearer, a line depicted in the blue dashed line in Figure B.3 appendix B.3 overlapping to energy barrier in the temperature range 200 to 740 K. Equation 4.1 was found by the linear regression, with correlation coefficients -0.9925, of the energy barrier depicted in a red solid line in Figure 4.5b.

$$\Delta G^\ddagger = 31.41 - 0.00271188 \cdot T \quad (4.1)$$

In Equation 4.1, T is the temperature, and it describes approximately the energy

Table 4.2: Approximate, energy barrier, enthalpy, entropy terms, and the percentage in which the energy barrier decreases

Temperature (K)	$\Delta G$	$\Delta H$	$\Delta S \cdot T$	%(Decrease)
0	31.41	31.41	0.0	0.0
300	30.60	31.41	-0.81	2.58
600	29.79	31.41	-1.62	5.17
900	28.97	31.41	-2.44	7.76
1200	28.16	31.41	-3.25	10.35
1500	27.35	31.41	-4.06	12.94
1800	26.53	31.41	-4.88	15.53

barrier in all ranges of temperature. It is depicted in the blue dashed line of Figure 4.5b. Evaluating Equation 4.1 with  $T=298.15$  K gives 30.59 kcal/mol, just very close to the computed value of 30.77 kcal/mol. The first term of the Equation 4.1 is enthalpy, and the second one is the entropic term. The computed values of  $\Delta G$ ,  $\Delta H$ ,  $\Delta S$ , and the percentage of contribution of  $\Delta S$  to energy barrier are summarized in Table 4.2 for some temperature values. Analysis of results shown in Table 4.2 leads that the enthalpy term is too large compared with the entropic term shown in row 3 and row 4 of Table 4.2, respectively, and evaluated in ranging temperatures given in row 1 of Table 4.2. In row five of Table 4.2 is given the percentage in which the energy barrier decreases as a function of temperature and due to entropic term considering as reference one hundred percent when the energy barrier is computed at  $T=0$ . Notably, the composition of the energy barrier is enthalpic and is too high in all ranges of temperature. We concluded that the interconversion between enantiomers is thermodynamically unfavorable in all ranges of temperature based on our computations. At hot temperatures, the energy barrier still is too high, and the most significant entropic contribution is not more than 15.54%. Similar results are obtained for the  $TS_b$ .

#### 4.3.4 Energy barrier between chiral and achiral structures at finite temperature.

Figure 4.6a displays the height of energy barrier interconversion at room temperature between the chiral  $\mathcal{P}/\mathcal{M}$  structures shown in Figure 4.1(1,2), and achiral structure depicted in Figure 4.17. Remarkable, these structures coexist at the dominant solid-solid transformation point located at 739 K, and according to the probability of occurrence, at hot temperatures, the achiral structure is the putative global minimum. Furthermore, the endergonic to an exergonic temperature point,  $T_{ee}$ , is defined here as the temperature where the reaction type change from an endergonic to an exergonic and in this Be<sub>4</sub>B<sub>8</sub> clusters it coincides with the solid-solid transformation point. When these two points coincide, at least two structures coexist, and there is a change of type reaction from endergonic to an exergonic or vice-versa.

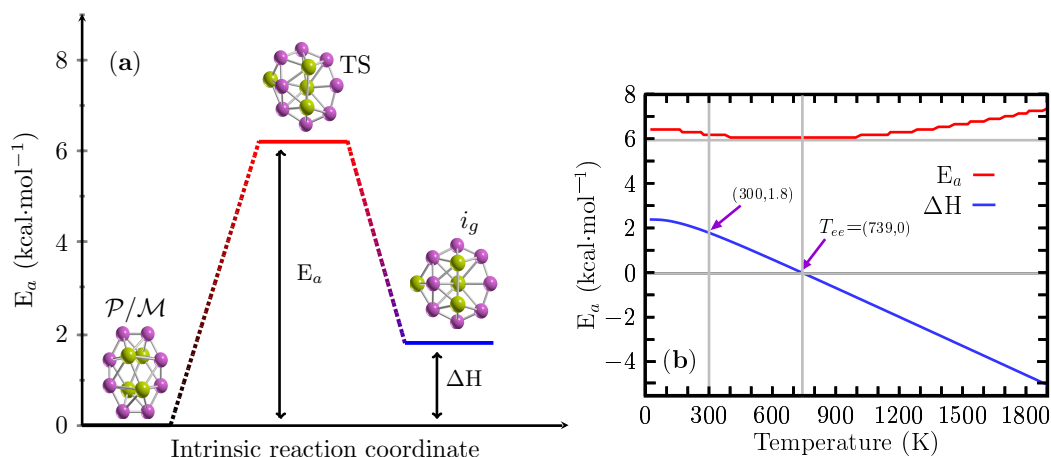


Figure 4.6: The height of energy barrier.

For the interconversion between those structures, the height of the energy barrier at room temperature is 6.20 kcal/mol, and the enthalpy of formation ( $\Delta H$ ) is 1.8 kcal/mol. The TS is depicted in Figure 4.6a, it is also a sandwich type structure formed by a distorted circular ring in which the Be-Be dimers are capping each faces of the ring, it has similar structure to isomer  $i_7$  depicted in Figure 4.1(g). Figure 4.6b shows the height of the energy barrier for chiral and achiral structures depicted in a red solid line, the enthalpy of formation ( $\Delta H$ ) for the same structures is depicted in a solid blue line for temperatures ranging from 20 to 1900 K. An analysis of  $\Delta H$  in Figure 4.6b, shows that the reaction process is endothermic for temperatures ranging from 20 to 739 K because the  $\Delta H$  is positive. At the temperature of 739 K, the  $\Delta H$  is zero, which implies that the chiral structure with  $C_1$  symmetry and achiral ( $i_7$ ) structure with  $C_1$  symmetry coexist. The above discussion is in good agreement with the computed point  $T_{ss-1}$  located at 739 K displayed in Figure 4.4a, and according to the probability occurrence, at this point, the chiral and achiral structures coexist. Furthermore, in this temperature point, the height of the energy barrier, depicted in the red-solid line Figure 4.6b, has a minimum value of 6.0 kcal/mol. At temperatures above 739 K, the reaction process is exothermic due to the  $\Delta H$  is negative, and the height of the energy barrier starts to increase slowly. Analysis of results in more detail leads to several observations. The reaction process is endothermic up to 739 K, which implies the absorption of energy, and the chiral structures strongly dominate as the putative global minimum. At temperatures of 739 K, the chiral and not chiral structures coexist. At temperatures above 739 K, the reaction process is exothermic, which implies a heat of reaction, and the non-chiral structures weakly dominate as the putative global minimum. Based on the  $\Delta H$  behavior in all ranges of temperature, we point out that the reaction is an entropic-driven process due to that type of reaction change from endothermic to exothermic as the temperature increases.



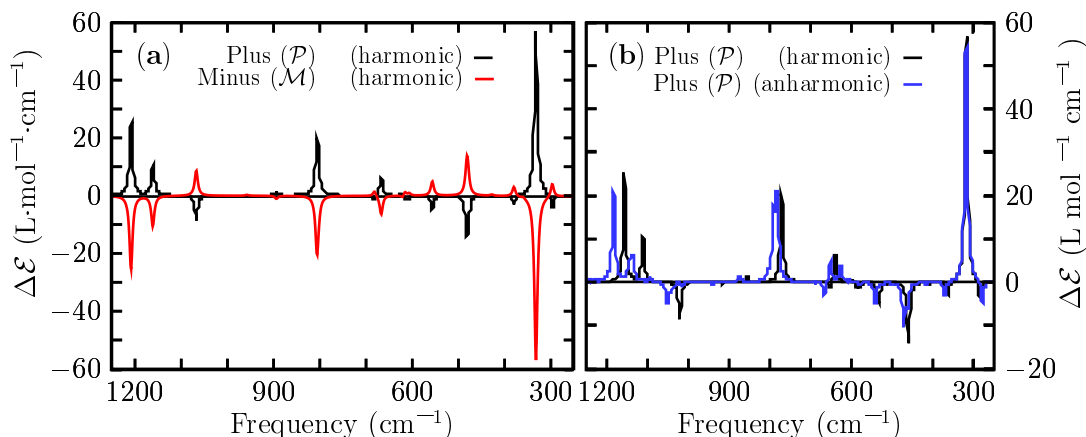


Figure 4.7: The panels Shows a comparison of the VCD spectrum.

#### 4.3.5 VCD and IR spectra

Figure 4.7a. shows a comparison of the VCD harmonic spectra corresponding to  $\mathcal{P}$  and  $\mathcal{M}$  lowest energy structures depicted in solid black- and red lines, respectively. They show a mirror image relationship, thereby ensuring that the two structures are non-superposable. The computed VCD spectrum ( $\mathcal{P}$  structure) is characterized by five main peaks located at frequencies of 330 cm<sup>-1</sup>, 481 cm<sup>-1</sup>, 802 cm<sup>-1</sup>, 1062 cm<sup>-1</sup>, and 1208 cm<sup>-1</sup> respectively. The largest peak positive intensity is located at 330 cm<sup>-1</sup>, and it corresponds to the stretching of the two Be-Be dimers that capped the distorted boron ring. Next, a transition located at 481 cm<sup>-1</sup> is the largest negative and is attributed to bending of the boron distorted ring, a kind of breathing motion. The peaks located in the region 1062 cm<sup>-1</sup> to 1208 cm<sup>-1</sup> corresponds to ring boron stretching. The harmonic approximation works if the potential energy is parabolic and it fails [242] as the temperature increases due to anharmonic effects [242] Under harmonic approximation, strongly anharmonic systems are not well described [243, 244] For high temperatures above 0.7...0.8 melting temperature, explicit anharmonic contributions become relevant, [245] moreover, we have to consider if the cluster whether or not it is highly strongly anharmonic. To estimate the importance of anharmonicities of the  $\text{Be}_4\text{B}_8$  chiral cluster, we show, In panel (b) of Figure 4.7b the anharmonic VCD spectra that is depicted in solid blue line, and for ease comparison overlaying with the harmonic vibrational spectrum depicted in solid black line, both of them computed for  $\mathcal{P}$  lowest energy structure, and employing Gaussian code. [51] A shifting factor of 0.96 is applied to shift the harmonic spectrum to overlaying the anaharmonic spectrum. We found that the frequency shift is 14 cm<sup>-1</sup> towards to high energy. A comparison of two spectra displayed in Figure 4.7b shows that The computed harmonic and anharmonic spectra are in very good agreement. In fact, most of the peaks are correctly computed employing the harmonic approximation. In the low range of energy the harmonic peaks and anharmonic peaks agree well, however, there are slightly discrepancies in

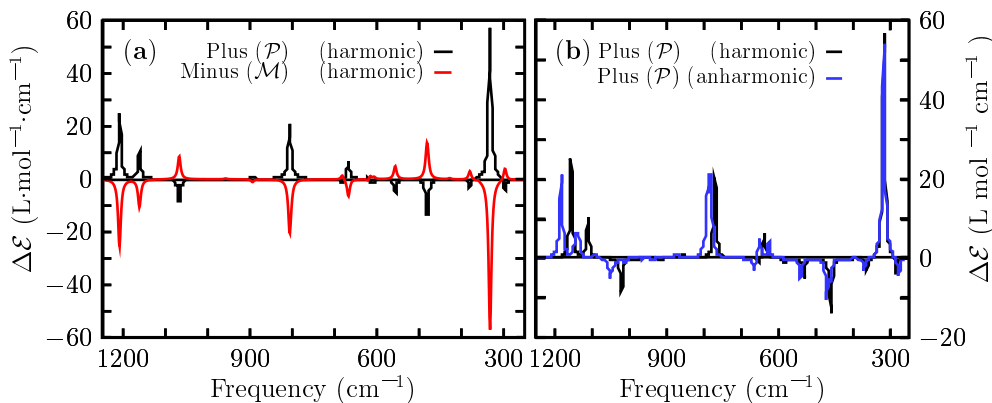


Figure 4.8: The dependent temperature IR Boltzmann-spectra-weighted.

the region  $1100\text{ cm}^{-1}$  to  $1200\text{ cm}^{-1}$ , nevertheless, in this study the computations of the thermodynamic properties and VCD spectra under the harmonic approximation yield reliable results enough to describe the non-strongly anharmonic  $\text{Be}_4\text{B}_8$  chiral cluster. Additionally, the Figure B.4, appendix B.4 show the IR spectra computed under harmonic and anharmonic approximations. The IR-harmonic spectrum is depicted in solid black line, whereas, the IR-anharmonic spectrum is depicted in solid red line. A shifting factor of 0.96 is applied to match the IR-harmonic spectrum over the IR-anharmonic spectrum. Comparing both spectra, it can see that the spectra match over a large range of frequencies. From the above mentioned we infer that the IR spectra under harmonic approximation yield valid results. Regarding dependent-temperature VCD spectra, the Boltzmann weighted overlapping to yield a total VCD spectrum at all ranging temperatures is zero because the Boltzmann ensemble is composed of achiral structures and an equal mixture of both  $\mathcal{P}$  and  $\mathcal{M}$  enantiomers, which implies that the Boltzmann ensemble is racemic. Any chiroptical response in the  $\text{Be}_4\text{B}_8$  cluster is going to be null. The exhaustive exploration of potential and free energy surface revealed that there are twenty two isomers within an energy range of 9.2 kcal/mol, six of which are chiral structures, with symmetries  $C_1$ ,  $C_2$ ,  $D_2$  respectively, and were within 1 kcal/mol. Moreover, these structures compose 98% of relative population at room temperature. With the aim to compute Boltzmann weighting IR spectra, those structures which only differs on symmetries has to be taken into account. The IR spectra, in comparison to VCD spectra, is not null. Figure 4.8 shows the IR spectra for temperatures ranging from 50 to 1900 K. The IR spectrum is composed of five peaks. The largest peak intensity is located  $330\text{ cm}^{-1}$  frequency axis it corresponds to the alternating stretching of the two Be-Be dimers that capped the distorted boron ring, and it is a mode that contributes to interconversion between P and M structures, The other four modes are related to compression/expansion of the boron ring.

Figure 4.8a display the IR spectra for temperatures ranging from 50 to 300 K, in this range, the IR spectra is strongly dominated by the spectrum of the lowest

energy pair of enantiomers with  $C_1$  symmetry, and further the IR intensities remain constants in all range of temperatures. The above mentioned, is in agreement with the relative population depicted in Figure 4.4a where the probability of occurrence of the pair of enantiomers with symmetry  $C_1$  strongly dominate. We have to consider that the contribution to IR spectra of the four enantiomers with  $C_2$  and  $D_2$  symmetries for temperature ranging from 20 to 300 K is equal to the IR spectrum with symmetry  $C_1$ , and there is not presence of other structure. Thus at room temperature all molecular properties, except for the chiral properties, are attributable to the lowest energy pair of enantiomers, depicted in Figure 4.1(a,b). Panel (b) of Figure 4.8 shows the IR spectra for temperature ranging from 400 to 700 K. The IR intensities start with exponential decay, in agreement with the probability of occurrence of the lowest pair of enantiomers of Figure 4.4a. There is a little contribution from other isomers, but not enough to change/alter the IR spectrum. Thus the shape of IR spectrum remains equal to IR spectrum at cold temperatures. The IR spectra for temperatures ranging from 800 to 1200 K are shown in Figure 4.8c, the largest contribution of a particular isomers is less than 17% thus the largest peak of IR spectra trend to be neglected. Panel (d) in Figure 4.8 displays that the IR spectra is almost null, thus at hot temperatures the IR spectra is neglected because of almost all contributions of the isomers to IR spectrum are around 10%.

#### 4.3.6 Molecular Dynamics

We performed a Born-Oppenheimer molecular dynamics employing the deMon2K program [189] (deMon2k v. 6.01, Cinvestav, Mexico City 2011) at different temperatures (1200, 1500 and 1800 K), with the aim to gain insights into the dynamical behavior of  $\text{Be}_4\text{B}_8$  cluster. We employed similar parameters that in a previous work. The simulation time was of 25 ps with a step size of 1 fs. For  $\text{Be}_4\text{B}_8$  cluster we found a dissociation phenomena when the temperature is higher than 1500 K, at 1800 K the dissociation process is stronger, while at 1200 K there is no dissociation. When at temperature T, a cluster dissociate the melting point temperature is lower than temperature of dissociation. [246, 51] a [2, 1, 16, 65, 64, 63]

## 4.4 Conclusions

For the first time, to our knowledge and from our results, we found that the chiral cluster  $\text{Be}_4\text{B}_8$  is the lowest energy structure.

# The Cu<sub>13</sub> cluster

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## 5.1 Abstract

This chapter reports the lowest energy structure of bare Cu<sub>13</sub> nanoclusters as a pair of enantiomers for temperatures ranging from 20 to 1200 K. Moreover, we compute the enantiomerization energy for the interconversion from  $\mathcal{M}$  to  $\mathcal{P}$  structures in the chiral putative global minimum for temperatures ranging from 20 to 1300 K. Additionally, employing statistical thermodynamics and nanothermodynamics, we compute the Boltzmann Probability for each particular isomer as a function of temperature. To achieve that, we explore the free energy surface of the Cu<sub>13</sub> cluster, employing a genetic algorithm coupled with density functional theory and statistical thermodynamics. Moreover, we discuss the energetic ordering of structures computed at the DFT level and compared to high level DLPNO-CCSD( $\mathcal{T}_1$ ) reference energies, and we present chemical bonding analysis using the AdNDP method in the chiral putative global minimum. Based on the computed relative abundances, our results show that the chiral putative global minimum strongly dominates for temperatures ranging from 20 to 1100 K.

## 5.2 Introduction

Transition-metal (TM) nanoclusters have been widely studied due to their potential applications in catalysis [247, 248, 249], photoluminescence [250], photonics [251], magnetism [250], chirality [252], and the design of new materials [253, 254]. Cu is a 3d TM with several oxidation states [255, 256], which explains its reactivity and confers many interesting physical and chemical properties [255, 256]. Moreover, the high boiling point of Cu makes it compatible with high-temperature chemical reactions. Clusters are aggregates of atoms at the nanoscale size, which exhibit unusual physicochemical properties [257]. Cu clusters are particularly fascinating due to their applications in catalysis [256], light-emitting devices [258], and nanotechnology [259], despite presenting some challenges such as their easy oxidation [259]. The most stable structure of small Cu clusters has been investigated by density functional theory (DFT) studies [260, 261, 262, 263] and considering the *Jahn-Teller effect* [264]. In the early 2000s, Poater *et al.* [265] characterized neutral copper clusters (Cu<sub>n</sub> n = 1-9) using computed chemical reactivity descriptors within the DFT framework. Later, atomic structures and reactivity descriptors of Cu<sub>n</sub>CO (n = 1,9) were computed and discussed [265]. Calaminici *et al.* reported the structure

of neutral and anionic Cu<sub>9</sub> clusters, employing DFT [266]. Moreover, in previous combined theoretical-experimental studies, the computed removal energies were compared with the measured photoelectron spectra in anionic Cu<sub>n</sub> (n = 9, 20) clusters [267], and later, the optical absorption of small Cu clusters was presented [268]. Based on their geometry and electronic structure, atomic clusters could be characterized by magic numbers [269, 247, 270, 271] that form highly symmetric structures; for example, icosahedron (ICO) and cuboctahedron (CUB) shapes [247]. From the geometrical point of view, the first magic number that appears is 13. Experimental studies have found magic TM<sub>13</sub> clusters for Fe and Ti, amongst others [272, 247]. Previous theoretical studies based on the empirical potential of Cu<sub>13</sub> clusters showed that the low-energy structures were the icosahedron and the cuboctahedron [273]; those structures consist of a central atom surrounded by 12 Cu atoms. In contrast, Guvelioglu *et al.* [274], within the framework of DFT, found that the lowest energy structure of Cu<sub>13</sub> is the double-layered structure, and in the same year Itoh *et al.* [275] reported a similar double-layer structure as the putative global minimum. Yang *et al.* explored the structural evolution of Cu<sub>n</sub> (n = 8-20) anions and found platelike structures [276]. Later, larger Cu<sub>n</sub> (n = 20-30) clusters were investigated, and it was found that the structures are based on a 13-atom icosahedral core [277]. In the previous studies, Cu<sub>13</sub> was investigated because it was found to have an icosahedral structure that has a high percentage of edge and corner sites and high-index facets, resulting in increased catalytic activities [278, 279, 280]. In most cases, low-energy Cu clusters have preferentially lower symmetry structures [281], although some present distorted structures [281, 282]. Although there are many studies on Cu clusters, the chirality of Cu<sub>13</sub> clusters has not been discussed. In general, chirality plays a decisive role in biological activity and life processes. [88]. Remarkably, chiral nanoclusters have attracted attention because they have applications in chiral materials with novel properties [283, 87, 2]. Recently, theoretical studies on beryllium boron cluster Be<sub>4</sub>B<sub>8</sub> at the DLPNO-CCSD( $\mathcal{T}_1$ ) theoretical level found chiral structures as the lowest energy structures [2]. Previous theoretical studies on PtPd co-doped silicon clusters reported chiral and fluxional low-energy structures [284]. Recently, Kong *et al.* reported propeller-like chiral AIE copper (I) clusters with exciting properties [285]. However, clusters properties depend on their putative global minimum and low-energy structures, considering achiral and chiral structures. Hence, we need to know the distributions of isomers at different temperatures [1, 2, 16]. The lowest- and low-energy geometries, composition, and temperature of the ensemble determine all the properties of a cluster at temperature T [1, 286, 16], i.e., its electronic, structural, thermodynamics, vibrational, and optical properties, as well as its chemical reactivity. Moreover, the atomic structure is the first level at which it is possible to manipulate the macroscopic properties of a cluster.

In this chapter, intending to elucidate the lowest- and the low-energy structures of neutral Cu<sub>13</sub> clusters at finite temperature, we explored their free energy surface by employing a genetic algorithm coupled to DFT, statistical thermodynamics and nanothermodynamics. We computed the probability of occurrence of each particu-

lar isomer, employing Boltzmann probabilities for temperatures ranging from 20 to 1500 K. Our findings show that the putative global minimum is a chiral structure at room temperature. Moreover, we computed the transition state (TS), i.e., the enantiomerization energy for temperatures ranging from 20 to 1300 K, for interconversion of a pair of enantiomers (Plus,  $\mathcal{P}$ , and Minus,  $\mathcal{M}$ ). Our computations showed that enantiomerization barriers led to persistently chiral structures and enabled the complete separation of enantiomers at room temperature [287, 2]. The remainder of the manuscript is organized as follows. Section 2 provides the computational details and a brief overview of the theory and the algorithms used. The results and discussion are presented in Section 3. We discuss the low-energy structures, the effect of the DFT functionals on the energetic ordering of isomers and comparison to DLPNO-CCSD( $\mathcal{T}_1$ ) [288] reference energies; T1 diagnostic is presented. The effect of the symmetry number on the Gibbs free energy and on the thermal populations at temperature T; and the origin of the slight 0.41 kcal/mol energy differences are investigated. We analyze the interconversion energy barrier between  $\mathcal{P}$  and  $\mathcal{M}$  enantiomers, the effects of the temperature in the energy barriers, and the thermal population.

### 5.2.1 Computational Details

All geometrical structures are optimized locally without imposing any symmetry, the self-consistent-field procedure was performed with a convergence criterion of  $10^{-6}$  a.u. The energy, maximum force and maximum displacement convergence were set to  $10^{-6}$  Ha,  $0.002 \text{ Ha}/\text{\AA}$  and  $0.0005 \text{ \AA}$  respectively. All calculations were performed using the Gaussian suite code [14] employing the Beck’s hybrid three parameter [289, 6] exchange-correlation functional in combination with the Perdew and Wang GGA functional PW91, [290, 291] this combination is known as B3PW91 exchange-correlation functional. The B3PW91 has been employed in other studies of reactivity in copper clusters with a good performance [292, 293], It is worth point out that hybrid functionals including a portion of Hartree-Fock exchange have shown a superior performance [292, 294, 295]. For the basis set, we employed the The LANL2DZ basis set is used for transitions metals due to its low computational cost [296] With the aim to refine the optimization and the energies, we used Ahlrichs-type triple- $\zeta$  quality extended valence def2TZVP basis [297, 298] that is more accurate for transition metals [299] despite it has a considerably higher computational cost. [300] In this study the dispersion corrections are taking into account trough the D3 version of Grimme dispersion [181] as it is implemented in Gaussian code. In a previous work, the effect of the dispersion corrections on the structural and energetic properties of the pure BeB clusters were studied founding that the energetic ordering of isomers can change when the dispersion is taking into account [1, 2]. Transition states are discarded through a vibrational analysis, making sure that the minimum energy structure is a true structure minimum energy. Calculation of Gibbs free energy properties of  $\text{Cu}_{13}$  cluster requieres an exhaustive and systematic sampling of the free energy surface with the aim to find all possible low-energy

structures. [1, 301] First of all, the search of the global minimum in atomic clusters is a complicated task due mainly that degrees of freedom of a molecule increases with the number of atoms; as a consequence, the number of local minimum increase exponentially with the number of atoms, moreover the calculated total energy of the cluster requires high level of quantum mechanical methodology to produce a real energy. In spite of that, several algorithms coupled with DFT to search the lowest energy structures on the potential energy surface of atomic clusters has been employed until nowadays, as kick methodology [302, 41, 303, 44, 48, 47, 49, 304], genetic algorithms [1, 28, 3, 29, 30] Our computational procedure to elucidate the lowest energy consisted of employing a hybrid genetic algorithm called *GALGOSON* [1, 2] *GALGOSON* employ a multi-step search strategy where in the first step it makes optimizations employing LANL2DZ basis set and in second step-refine it employs the def2TZVP basis set, the creation of the initial population take into account the 2D and 3D structures [28, 42] with an initial population of 650 random structures for the  $\text{Cu}_{13}$  cluster and the criterion to stop the algorithm is until the five generations converged. This methodology based on previous works [305, 238, 3] consists of a multi-step approach (cascade) to efficiently sample the potential/free energy surface coupled to the *Gaussian* code [51]. Chemical bonding was examined using the Adaptive Natural Density Partitioning (AdNDP) method [92, 2]. AdNDP analyses the first-order reduced density matrix and recovers Lewis bonding (1c-2e or 2c-2 e, i.e., lone pairs (LPs) or two-center two-electron bonds) and delocalized bonding elements (associated with the concept of electron delocalization).

## 5.3 Results and Discussion

### 5.3.1 The lowest energy structures and energetics

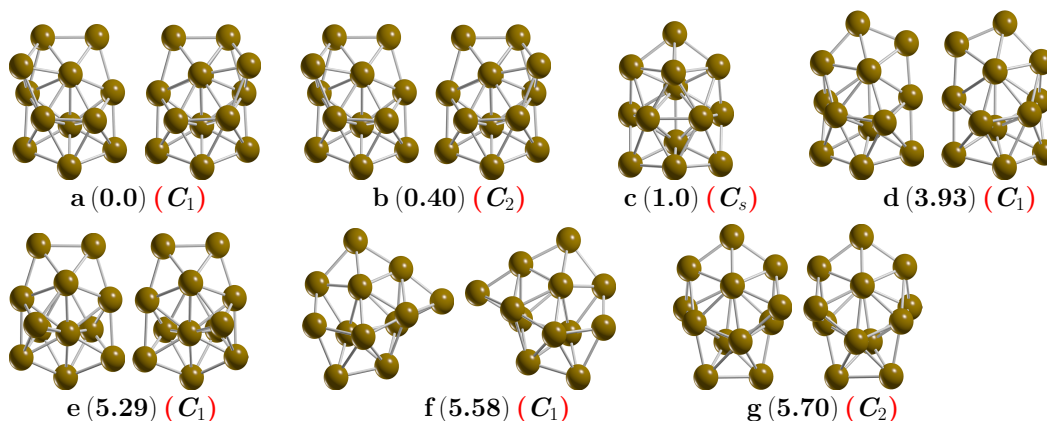


Figure 5.1: The chiral and achiral lowest energy structures.

The most important low-energy structures of a neutral  $\text{Cu}_{13}$  cluster optimized at the B3PW91-GD3/def2TZVP level of theory found in this study are shown in

Figure 5.1. At room temperature, the isomers depicted in Figure 5.1 contributed to 94% of the molecular properties in a Boltzmann ensemble; thus, almost all molecular properties were due to those isomers. Additionally, they are chiral structures. The putative chiral global minimum is depicted in Figure 5.1a with symmetry  $C_1$ . These are bilayered structures composed of a shared pentagonal bipyramid interspersed with a distorted hexagonal ring with a Cu atom capping one of its faces and two Cu atoms capping the other face of the hexagonal ring, in good agreement with similar structures [306, 274, 307]. The pentagonal bipyramid interspersed with the hexagonal ring is built with 12 Cu atoms. One more Cu atom caps the pentagonal bipyramid; this capping Cu atom is responsible for the chirality of the  $Cu_{13}$  cluster. Our calculated Cu-Cu bond length on the putative chiral global minimum is 2.432 Å, in good agreement with other reported DFT calculations of a Cu-Cu dimer of 2.248 Å [308] and also with an experimental bond length of 2.22 Å [309, 310], just slightly above 5.3% of the experimentally determined value. The calculated vibrational frequency of  $Cu_{13}$  was 60  $cm^{-1}$ , whereas the computed vibrational frequency of the Cu-Cu dimer was 245  $cm^{-1}$ , again in good agreement with the experimental value of 265  $cm^{-1}$  [310]. We also explored the higher multiplicity of quartets and found that the lowest energy structure lay 20.5 kcal/mol above the doublet putative chiral global minimum energy structure. The second structure that was higher in free energy lay at 0.41 kcal/mol at room temperature; it was also a bilayered structure, similar to the putative global minimum, but with  $C_2$  symmetry. Iwasa *et al.* [311] reported a similar double-layer structure as a putative global minimum with  $C_2$  symmetry, but without taking into account the temperature. One of our previous studies showed that these tiny Gibbs free energy differences are derived from rotational entropy [2]. The  $C_1$  and  $C_2$  symmetry clusters adopted a hollow layered structure. The following higher energy isomer lay at 1.0 kcal/mol at room temperature and was an achiral buckled-biplanar (BBP) structure with  $C_s$  symmetry, which agrees with previous work [312]. At room temperature, its contributions to the molecular properties were less than 6%. The average bond length on isomer BBP was 2.432 Å, similar to the average bond length of the chiral putative global minimum. Next, higher energy structures lay 3.9 kcal/mol above the chiral putative global minimum, and their average bond length was 2.444 Å, slightly larger than the average bond length of 2.432 Å of the putative global minimum. This also appeared as a bilayered chiral structure with a shared hexagonal bipyramid interspersed with a hexagonal bipyramid. The following higher energy structure lay 5.29 kcal/mol above the putative minimum global. It was a bilayered structure consisting of 12 atoms, with 1 atom capping one of its faces. It is depicted in Figure 5.1e. Structures located at higher energy than 5.5 kcal/mol above the putative global minimum are depicted in Figure 5.1f,g. Those structures also adopted a layered structure with no interior atoms, with similar morphology to that of low-energy isomers. These two structures did not contribute to the molecular properties in the studied temperature range. The  $Cu_{13}$  cluster low-energy structures preferentially adopted morphologies of bilayered structures rather than highly symmetric 3D structures. In contrast,  $Au_{13}$  clusters prefer planar structures due to relativistic effects [281]; therefore, fur-



ther studies are needed to investigate why bilayered structures in the  $\text{Cu}_{13}$  cluster are energetically preferred. For the  $\text{Cu}_{13}$  cluster, the icosahedron structure is not energetically favorable in the temperature range examined, which is consistent with previous work where the authors did not take into account the temperature [247]. In this study, the icosahedron structure was located at 24.6 kcal/mol above the putative global minimum at room temperature. To get an idea of the bonding situation

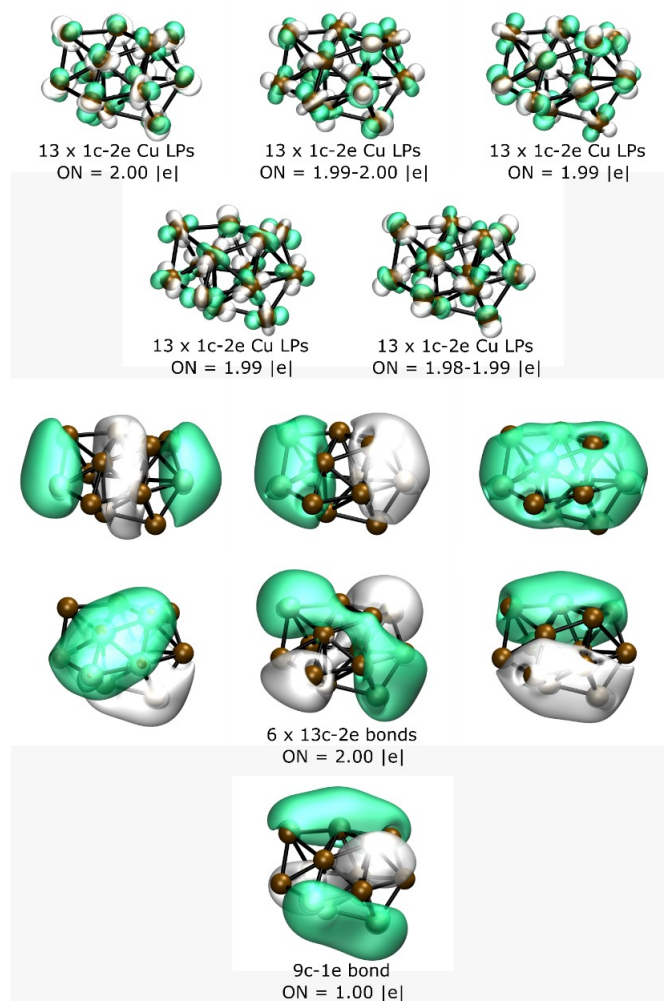


Figure 5.2: Results of the AdNDP analysis of the lowest-energy chiral isomer of the  $\text{Cu}_{13}$  system.

in the chiral putative global minimum structure, we performed an AdNDP analysis; the results are shown in Figure 5.2. This analysis revealed the presence of 5 sets of 13 1c-2e bonds with occupation numbers (ONs) between 1.98 and 1.99 |e|, i.e., lone pairs (LPs) corresponding to the fully filled 3d shell in each Cu atom. The bonding in this cluster was then due to the 4s shell electrons for which the bonding

pattern, as revealed by AdNDP, consisted of 6 sets of 13c-2e completely delocalized bonds, plus a 9c-1e bond corresponding to the unpaired electron which, as shown in Figure 5.2, was mostly delocalized in the peripheral atoms of the cluster.

### 5.3.2 Energetics

Table 5.1: Relative energy in kcal/mol of the low-lying isomers depicted in Figure 5.1 labeled from a to f.

Level	Isomers									
	$i_a$	$i_a$	$i_b$	$i_b$	$i_c$	$i_d$	$i_d$	$i_e$	$i_e$	$i_f$
$\Delta G(\text{B3PW91})$	0.0	0.0	0.3953	0.4091	0.9946	3.9338	3.9357	5.2967	5.2967	5.5728
$\Delta G(\text{TPSS})$	0.0	0.0	0.4010	0.4016	0.7248	5.6017	5.6029	5.5477	5.5477	7.5438
$\Delta G(\text{PBE})$	0.0	0.0	0.4145	0.4217	0.5491	3.8478	3.8491	5.5283	5.7284	5.7310
$\Delta G(\text{BP86})$	0.0	0.0	0.4079	0.4035	0.8634	3.5611	5.4291	5.4291	5.2817	7.2798
DLPNO-CCSD(T)	0.0	-0.1298	-0.2154	-0.2144	0.6827	5.0246	5.8771			
DLPNO-CCSD(T)+ $\mathcal{E}_{\text{ZPE}}$	0.0	-0.1298	-0.2216	-0.2170	0.7084	4.9022	5.7886			
$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.0	0.0	0.0	0.0	0.9262	4.5877	4.5877	5.6124	5.6124	6.3327
$\mathcal{E}_0$	0.0	0.0	0.0	0.0	0.9002	4.7096	4.7098	5.7013	6.4969	6.4966
Point group symmetry	$C_1$	$C_1$	$C_2$	$C_2$	$C_s$	$C_1$	$C_1$	$C_1$	$C_1$	$C_1$
$\mathcal{T}_1$ Diagnostic	0.023	0.023	0.023	0.023	0.023	0.023	0.023	0.023	0.023	0.023

Temperature drastically affects the Gibbs free energy of the isomers; therefore, in a molecular ensemble (collection), the energetic ordering of isomers changes. Besides, from a theoretical point of view, the energetic ordering can also change when computing energies using different levels of theory [1, 313]. To wit, energy computed at different methods yield different energies due mainly to the functional and basis-set employed, [1], so the energetic ordering change; consequently, the probability of occurrence and the molecular properties will change. Moreover, we compute the  $\mathcal{T}_1$  diagnostic to determine if the computed DFT energies are properly described by a single reference method or contain a multireference character. To gain further insight into the energetic ordering of the low-lying isomers, we optimized the low-lying energy structures employing three more DFT functionals: TPSS [314], PBE [7], and BP86 [6] with def2-TZVP basis set, and single point (SP) relative energies computed employing the domain-based local pair natural orbital coupled-cluster theory (DLPNO-CCSD(T)), with TightPNO setting [288], and with and without ZPE energy correction. The purpose was to ascertain the origin of the slight 0.41 kcal/mol differences (below the chemical accuracy of 1 kcal/mol) in the relative Gibbs free energy (Table 5.1) and that these are not due to numerical errors, algorithmic approximations, integration grids, or functional and basis set dependence, to name a few. In Table 5.1, lines first through the fourth show the relative Gibbs free energies computed at B3PW91-D3/def2-TZVP, TPSS-D3/def2-TZVP, PBE-D3/def2-TZVP, and BP86-D3/def2-TZVP, respectively. DLPNO-CCSD(T) relative energies, with and without ZPE correction, are shown in the fifth and sixth line of Table 5.1, electronic with zero-point energy and electronic energy, at the B3PW91-D3/def2-TZVP level of theory are shown in the seventh and eighth lines of Table 5.1, and

line ninth shows the point group symmetry, the  $\mathcal{T}_1$  diagnostic for each isomer is shown in line tenth of Table 5.1, our results confirm that the computed  $\mathcal{T}_1$  diagnostic values are slightly above the recommended threshold of 0.02 [315, 2]; So, these values suggest that multireferential studies have to be carried out for Cu<sub>13</sub> cluster. At the CCSD(T) theoretical level, the lowest-energy structure is the pair of enantiomers with symmetry C<sub>2</sub>; despite that, at finite temperature, the lowest energy structure is the pair of enantiomers with symmetry C<sub>1</sub>. A more detailed analysis of the results in Table 5.1 shows that the relative electronic energy of the four chiral low-energy isomers labeled in Table 5.1 (a, b, c, d), with symmetry C<sub>1</sub>, C<sub>1</sub>, C<sub>2</sub>, and C<sub>2</sub>, respectively, is zero, considering the ZPE; also the relative electronic energy is zero. In contrast, the relative Gibbs free energy at 298.15 K shown in the fifth column is 0.41 kcal/mol. The relative Gibbs free energy at 298.15 K for the TPSS, PBE, BP86 DFT-functions, between the putative global minimum and the second isomer, is also 0.41 kcal/mol. This Gibbs free energy difference does not depend on the functional employed, as shown in Table 5.1. At temperature T=0, the total energy of an isomer is the electronic energy plus ZPE ( $\varepsilon_0 + ZPE$ ). If the temperature increases, entropic effects start to play, and Gibbs's free energy determines the global minimum. At any temperature T, the isomers, represented in Figure 5.1 and Figure 5.1b, differ only in molecular symmetry. The isomer with C<sub>2</sub> symmetry has a Gibbs free energy equal to  $RT\ln(\sigma)$  less than the non-symmetric C<sub>1</sub> isomer. Here R is the universal gas constant, T temperature, and  $\sigma$  is the symmetry number. The symmetry number appears in the denominator of the molecular rotational partition function [316, 1, 2, 317]. This implies that the less symmetric isomers at finite temperature are more thermodynamically stable than the more symmetric ones due to the energy factor given by  $RT\ln(\sigma)$ . The factor becomes zero at T=0 and increases linearly with temperature. Figure 5.3 shows the factor as a function of temperature

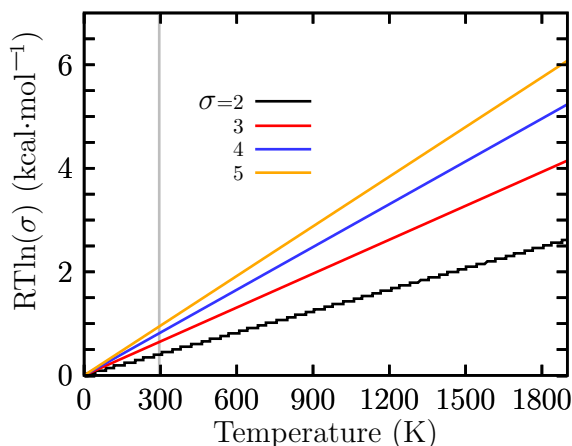


Figure 5.3: The difference of the Gibbs free energy with and without symmetry.

and for different symmetry numbers. Moreover the  $\mathcal{T}_1$  diagnostic indicate that a multireference c For our optimized low-energy isomers with C<sub>2</sub> symmetry, the sym-

metry number is 2, so the Gibbs free energy at 298.15 K with and without symmetry will differ by 0.41 kcal/mol regardless of the DFT method. This value is higher at high temperatures and with higher symmetry numbers. For example, the benzene molecule with  $D_{6h}$  symmetry has a symmetry number 12, the Gibbs free energy at 298.15 K with and without symmetry will differ by 1.47 kcal/mol, which is greater than the chemical precision. Here, we call this the effect of the symmetry number on the Gibbs free energy and on the thermal populations at finite temperature; the symmetry number appears when identical atoms are considered indistinguishable and are determined solely by the point group symmetry of the molecule. We emphasize the importance of symmetry in calculating thermal populations at absolute temperature  $T$  or the so called population probability or relative populations, hence the molecular properties. For example, the melting temperature for a symmetrical molecule is higher than a non-symmetrical molecule; moreover, the activation energy barrier could be higher when we consider a non-symmetrical molecule in the calculation of the transition state. The energy computed at different theoretical levels influences the energy distribution of the isomers and, as a consequence, the Boltzmann weights. For the four DFT functionals used in this study, the energy ordering is preserved, although differences in the energy between the isomers occur; for each DFT functional, the main contributors to any molecular property of  $\text{Cu}_{13}$  are always the chiral isomers depicted in Figure 5.1a.

### 5.3.3 Structures and Stability at Finite Temperature.

In chemistry, physics, and biology, the lowest energy structure and all the low-energy structures near the global minimum are crucial because all molecular properties are statistical averages derived from the ensemble of molecular conformations [2]. The probability of occurrence of each particular isomer is depicted in Figure 5.4 for the  $\text{Cu}_{13}$  cluster. It was determined by employing Equation 3.1 and temperatures ranging from 20 to 1500 K at the B3PW91-D3/def2TZVP level of theory. Figure 5.4 shows the probability of occurrence considering all chiral and achiral structures. The analysis of these results led to an interesting observation. The pair of enantiomers that appeared as the putative global minimum at temperature 0 K was strongly dominant in the temperature range from 20 to 1500 K. Moreover, there were no solid-solid transformation points in any temperature range, which means no interchange of dominant low-energy structures at high temperatures. A closer inspection of Figure 5.4 shows that the decay of probability of occurrence of the pair of enantiomers with symmetry  $C_1$ , depicted by a red solid line, is closer to linear rather than exponential for temperatures ranging from 20 to 600 K. Above 600 K and up to 1500 K, the decay is exponential. At 300 K, the chiral structure has a probability of 32%, whereas the second isomer located 0.4 kcal/mol above the putative global minimum has a probability of 16%. The above discussion shows that all molecular properties of the  $\text{Cu}_{13}$  cluster are attributed to the chiral putative global minimum at absolute temperature zero. The probability of occurrence of the chiral putative global structures, is depicted by blue and yellow solid lines in Figure 5.4. The

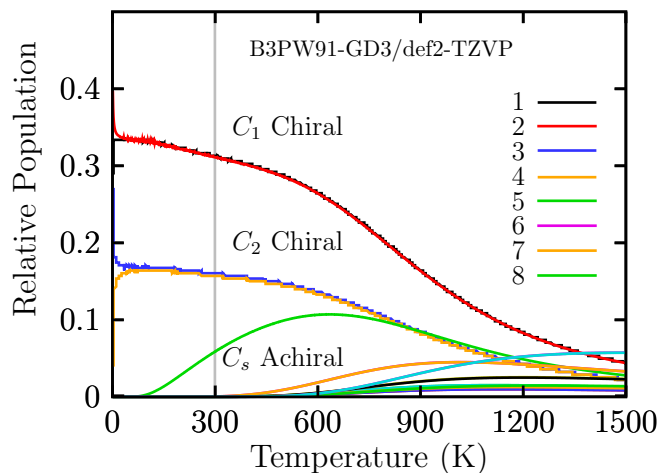


Figure 5.4: Probability of occurrence for all isomers at temperatures.

probability of occurrence for structures with  $C_1$  and  $C_2$  symmetries showed similar behaviors but different values; even so, the molecular properties are attributed to only one pair of enantiomers with symmetry  $C_1$ . The probability of occurrence for the achiral structure, which is shown in Figure 5.1c, located 1 kcal/mol above the putative global minimum, is depicted by a green solid line in Figure 5.4; it started to increase around a temperature of 120 K, and at room temperature, it has a probability of 5%. At 700 K, the highest probability of occurrence was reached, corresponding to 12%; above this temperature, up to 1500 K, it started to decrease. Note that above 800 K and up to 1200 K, the achiral structure with  $C_s$  symmetry and the putative global minimum structures with  $C_2$  symmetries coexisted. Interestingly, the Boltzmann ensemble was composed of an equal mixture of  $\mathcal{M}$  and  $\mathcal{P}$  enantiomers; thus, the chiral properties were null in all ranges of temperature, i.e., the Cu<sub>13</sub> cluster did not exhibit properties such as vibrational/electronic circular dichroism. In ranging temperatures from 1200 to 1500 K, all isomers coexist with less than ten percent probability. To wit, all isomers are equally populated for hot temperatures or when the temperature increases to large values. The bulk melting temperature of copper, 1358 K [63]; So, we must consider that the anharmonic effects become strong at high temperatures [2]. From the thermal population, we consider the entropic-temperature term has a small effect on the Cu<sub>13</sub> cluster distribution of isomers on the scale of temperature, as shown in Figure 5.4.

#### 5.3.4 Enantiomerization Energy Barrier at Finite Temperature.

The process in which one enantiomer in a pair is converted into the other is known as enantiomerization; enantiomers each have an equal probability of occurrence, and the same energy. The enantiomerization energy or activation energy at temperature  $T$  defines the configurational stability. In some cases, a low enantiomerization energy is undesirable [318]. Two reaction mechanisms compete for the interconversion

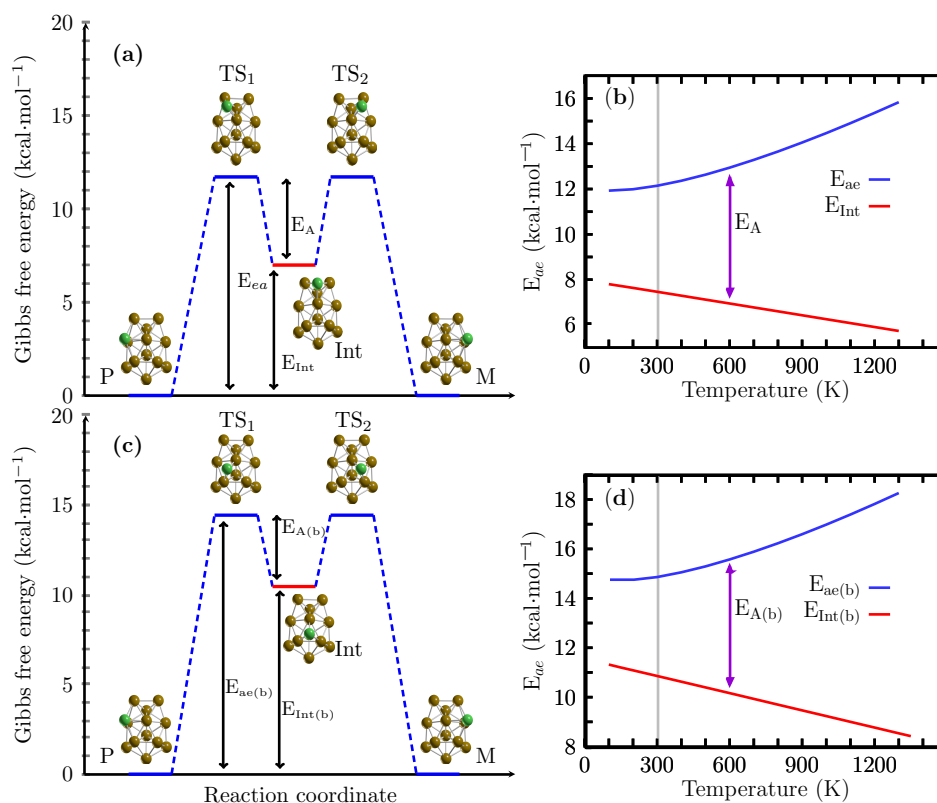


Figure 5.5: Figure shows the energy profile of a chemical reaction.

from  $\mathcal{P}$  to  $\mathcal{M}$  structures, and the shape of the energy barriers (or IRC) is similar to the inverted double-well potential [319] Figure 5.5a shows the reaction mechanism for the interconversion between  $\mathcal{P}$  and  $\mathcal{M}$  structures for route A, which proceeds via a two-step mechanism consisting of two symmetric steps with only one intermediate. Figure 5.5a shows the reaction mechanism for the interconversion between  $\mathcal{P}$  and  $\mathcal{M}$  structures for route B, which proceeds via a two-step mechanism consisting of two symmetric steps with only one intermediate. Figure 5.5a depicts the transition states TS1 and TS2, the intermediate (Int), and the putative lowest energy pair of enantiomers  $\mathcal{P}$  and  $\mathcal{M}$ . The energy of enantiomerization was 12.15 kcal/mol, whereas the activation energy for the interconversion of the intermediate to  $\mathcal{P}/\mathcal{M}$  structures was 5 kcal/mol at room temperature. The intermediate state was located at 7.13 kcal/mol above the putative chiral lowest energy structure The structures of the TS1 and TS2 states are depicted in Figure 5.5a. They appeared to be bilayer structures composed of a shared pentagonal bipyramid interspersed with a distorted hexagonal ring. The green atom represents the Cu atom that caps one edge of the pentagonal bipyramid and is responsible for the chirality of the Cu<sub>13</sub> cluster. The intermediate state structure for the same bilayer presented 12 Cu atoms and the green Cu atom caps one of the faces in the pentagonal bipyramid. Figure 5.5a shows the enantiomerization energy  $E_{ae}$  depicted by a solid blue line. The relative energy of

the intermediate,  $E_{Int}$ , for the putative global chiral structures is depicted by a solid red line. As the temperature increased, the enantiomerization energy increased almost linearly. In contrast, the relative energy of the intermediate with respect to the putative global minimum decreased linearly, implying that the inverted double-wall became energetically greater. The activation energy for the interconversion between the intermediate and the  $\mathcal{M}$  structure was 5 kcal/mol at room temperature; this increased linearly, from 4 kcal/mol at a temperature of 100 K to 9.5 kcal/mol at a temperature of 1200 K. As a consequence. In contrast, at low temperatures, the enantiomerization energy trend reached a minimum, whereas the relative energy of the intermediate increased; thus, the energy activation for the interconversion of the intermediate to the  $\mathcal{P}/\mathcal{M}$  states tended to be smaller. These results suggest that at high temperatures, the enantiomerization barrier energy increased, and the intermediate state energy became more significant, stabilizing chirality and allowing the separation of enantiomers at room temperature. To elucidate the behavior of the interconversion from  $\mathcal{P}$  and  $\mathcal{M}$  structures; We computed the reaction rate constants based on Equation 5.1 (Eyring equation) that used the activation barrier  $\Delta G$  between the putative global minimum  $\mathcal{P}/\mathcal{M}$  structures and the transition state and did not take into account the tunneling effect. The Eyring equation relates the rate constant to temperature and the activation free energy.

$$k = k_0 \frac{K_B T}{h} e^{-\Delta G/RT} \quad (5.1)$$

Table 5.2: Table shows the values of enantiomerization energy ( $E_{ea}$ ), relative energy of intermediate ( $E_{Int}$ ), and activation energy ( $E_A$ ).

Level of theory	Reaction A			Reaction B		
	$E_{ea}$	$E_{Int}$	$E_A$	$E_{ea}$	$E_{Int}$	$E_A$
B3PW91-D3/Def2TZVP	12.15	7.13	5.0	14.85	10.86	3.99
B3PW91/Def2TZVP	12.36	6.38	5.97	15.60	11.31	4.28

In Equation 5.1,  $k$  is the rate constant,  $k_0$  transmission coefficient that in the absence of other kinetic data is set to 1,  $K_B$  is Boltzmann constant,  $T$  is the temperature,  $h$  is the Planck constant,  $R$  is ideal gas constant, and  $\Delta G$  is the activation energy barrier. We consider the rate-determining step in the overall reaction is the rate of interconversion between  $\mathcal{P}/\mathcal{M}$  and intermediary structures, and it is the slowest step; besides, its high activation energy characterizes it. (Notice, the activation energy barrier  $\Delta G$  is computed with the statistical thermodynamics). The height of the activation energy barrier at room temperature for interconversion between  $\mathcal{P}/\mathcal{M}$  and intermediary structures in route A is 12.14 kcal/mol, which leads to a rate constant of  $7.84 \times 10^3$  1/s, whereas the activation energy barrier at 900 K is 14.0 kcal/mol, which leads to a rate constant of  $7.47 \times 10^9$  1/s. This show that the rate constant increases at high temperatures, and it agrees with the thermal populations where the contribution of all isomers is less than 10% at high temper-

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atures. We also have to consider that the melting point for copper is 1358 K, thus around this temperature, the glass state will dominate. Regarding dispersion, if it is not considered, the energy barriers tend to increase. For ease of comparison, Table 2 shows the values of the two similar reaction mechanisms A and B, taking into account the D3 dispersion of Grimme. Energetically, the reaction mechanism of route B is not so different from that of route A, as we can see in Figure 5.5c,d and in Table 5.2.

## 5.4 Conclusions

For the first time, to our knowledge and from our results, we computed the effect of symmetry on the Boltzmann populations on TM Cu clusters.





# The Cu<sub>38</sub> cluster

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## 6.1 Abstract

The UV-visible and IR properties of the Cu<sub>38</sub> nanocluster depend to a great extent on the temperature. Density functional theory and nanothermodynamics can be combined to compute the geometrical optimization of isomers and their spectroscopic properties in an approximate manner. In this chapter 6, we investigate entropy-driven isomer distributions of Cu<sub>38</sub> clusters and the effect of temperature on their UV-visible and IR spectra. An extensive, systematic global search is performed on the potential and free energy surfaces of Cu<sub>38</sub> using a two-stage strategy to identify the lowest-energy structure and its low-energy neighbors. The effects of temperature on the UV and IR spectra are considered via Boltzmann probability. The computed UV-visible and IR spectrum of each isomer is multiplied by its corresponding Boltzmann weight at finite temperature. Then, they are summed together to produce a final temperature-dependent, Boltzmann-weighted UV-visible and IR spectrum. Additionally, Molecular Dynamics simulation of the Cu<sub>38</sub> nanocluster was performed to gain insight into the system dynamics and make a three-dimensional movie of the system with atomistic resolution. Our results show the thermal populations at the absolute temperature of Cu<sub>38</sub> cluster, and the disordered structure that dominates at high temperatures

## 6.2 Introduction

Nano clusters are of interest due they allow us to study the transition from free atoms to bulk condensed systems[320] as a consequence, analyze the size-dependent evolution of their properties.[321] Especially, Noble-Metal Nanoclusters (NMC) have attracted attention in many fields of science due to interesting plasmonic, catalytic properties,[322, 323] and photophysical properties at nanoscale,[324] Particularly, Nano Cu clusters embedded in the dielectric matrix have attracted attention because of their tunable longitudinal surface plasmon resonance.[322] Besides, copper is cheaper than gold and silver, and it has large photosensitivity, high thermal and electric conductivity, and optical properties [325] that makes it a good candidate to develop nanodevices [326] and nanoelectronics. [327] In particular, Cu<sub>38</sub> attracted attention due to it has a magic structures, [328] defined in terms of geometric and energetic factors and related to the closing of electronic shells [329] as it happens

in small sodium clusters.[330] For the Cu<sub>38</sub> cluster its magicity is due to only energetic considerations.[331, 329] In contrast, small packed barium clusters with magic numbers, the stability is dominated for geometrical effects rather than electronic effects.[330] It is believed that magic structures are the putative global minimum energy structures on the potential energy surface, thus reflect the molecular properties of the system.[329] From the experimental point of view, the Cu<sub>38</sub> cluster has been widely studied by photoelectron spectroscopy technique (PES). Pettiette *et al.*[332] employing PES extract the electronic gap of anionic Cu<sub>38</sub> cluster and found a semiconductor type with 0.33 eV.[332, 325] However, the geometrical structure was not investigated. In contrast, Kostko *et al.* also studied the anionic Cu<sub>38</sub> and from the PES inferred that putative global minimum should be an oblate structure instead of a high symmetric structure,[333, 325] despite that computations for 38 atom clusters on noble metal clusters frequently found high symmetric (cuboctahedral) structures.[331, 334, 333] From the theoretical point of view, Taylor *et al.* presented a study based on density functional theory (DFT) of thermodynamic properties of Cu<sub>38</sub> cluster,[335] Previous works employing DFT studied the transition states and reaction energies of water gas shift reaction in a Cu<sub>38</sub> cluster and Cu slab.[336] In other previously DFT studies the high symmetry octahedral structure was reported as the lowest energy structure[337] employing PW91[291] functional, plane wave basis set and pseudopotential approximation.[260] Hijazi *et al.* [338] investigated the Cu<sub>38</sub> cluster employing hybrid strategy; they used the embedded atom method potential followed by DFT computations using the PBE functional and pseudopotential approximation and reported that octahedral (OH) symmetry is the putative global minimum structure followed by the incomplete-Mackay icosahedron (IMI) located at 0.26 eV above of the putative global minimum. On the other hand, search for the lowest energy structure employing many body potentials gives a cuboctahedral structure.[331, 339] Erkoç *et al.* [340] employing an empirical potential-energy function, which contains two-body atomic interactions [341] found that the fivefold symmetry appears as putative global minimum in Cu<sub>38</sub> cluster. In contrast, the cuboctahedron structure was reported as putative global minimum in a previous studies[342] employing empirical *many-body Gupta* and *Sutton-Chen* potentials. Nevertheless, there has been some discussion which is the lowest energy structure, some previous works consider the Cu<sub>38</sub> octahedron cluster, as the putative global minimum[338, 337, 260], in contrast, several others found that Cu<sub>38</sub> cluster with the truncated octahedron geometry is energetically more stable than other configurations[343, 338, 260, 344, 345, 346]. We point out that the energy computed with different methods such as DFT, MP2, or CCSDT, just to mention few of them, yield different energetic ordering.[1, 347, 236] In the case of DFT, the functional and basis set employed, ZPE energy correction, or energy of dispersion among others can interchange the putative global minimum. Moreover, practical molecular systems and materials needs warm temperature [348], so the molecular properties at temperatures T are dominated by Boltzmann distributions of isomers,[1, 77, 2] therefore, their properties are statistical averages over the ensemble of conformations.[1] The structure corresponding to the global minimum ceases

to be the most likely at high T so other structures prevail. Furthermore, in small Ag clusters, the temperature leads the transition from the initial FCC phase to other structural modifications,[349] so it promotes the changes of phases in materials. Interesting, at different temperatures than zero, the molecular system minimizes the Gibbs free energy and maximizes the entropy.[1, 2] Although the search of the global and local minima is useful in understanding reactivities and catalytic efficiencies, but such studies most of the time neglect temperature dependent entropic contributions to free energy when increasing temperature. Taking temperature into account requires dealing with nanothermodynamics.[1, 2, 52, 65, 64, 16, 63, 161] The thermodynamics of clusters have been studied by a variety of tools,[163, 1, 65, 64] like molecular-dynamics simulations on boron clusters [106] and Cu<sub>38</sub> clusters.[325] The cluster properties depends strongly of the structure, size, composition, and temperature, so the first step in order to understanding molecular properties is the elucidation of the lowest energy structure and its isomers close in energy; [2, 1, 16, 157] This is a complicated task due to several factors.[1, 2] As second step for understanding cluster properties relies on their spectroscopy which gives insight into its structure and it was proposed as a way of detecting structural transformations into clusters. The influence of temperature on the spectroscopy has been computed before for a variety of clusters, for instance, [350, 1, 2] such in the present study, for the neutral Cu<sub>38</sub> cluster, we use the statistical formulation of thermodynamics or nanothermodynamics[65, 1, 64, 2] to compute thermodynamics properties and define the putative global minimum at temperatures diferent from zero, evaluated the relative populations among the isomers and computed UV-Visible and IR spectra as a Boltzmann weighted spectrum sum of individual spectra. Our findings show that at hot temperatures at amorphous structure strongly dominate the putative global minimum whereas the truncated octahedron dominates at cold temperatures. The remainder of the manuscript is organized as follows: Section 2 gives the computational details and a brief overview of the theory and the algorithms used. The results and discussion are presented in section 3; The putative global at room temperature and relative population in ranging temperatures from 20 to 1500K, and the IR spectra as a function of temperature.

### 6.3 Results and Discussion

The ball and stick model shown in Figure 6.1 depicted the lowest-energy structure and the low-energy structures of neutral Cu<sub>38</sub> clusters along with some competing isomers. At B3PW91/def2SVP level of theory and taking into account the dispersion pairwise correction of Grimme (DFT-GD3),[181] ZPE energy corrections and at room temperature and 1 atmospheric pressure. We found a tetrakaidecahedron as the lowest energy structure which has 14 faces: six equivalent square FCC(100) and eight equivalent hexagons, this shape is obtained when cutting the corners off 3D diamond shape, and it is a fcc-like truncated octahedron (TO). The calculated structure belongs to point group symmetry C<sub>1</sub>, electronic ground state <sup>1</sup>A, its lowest IR

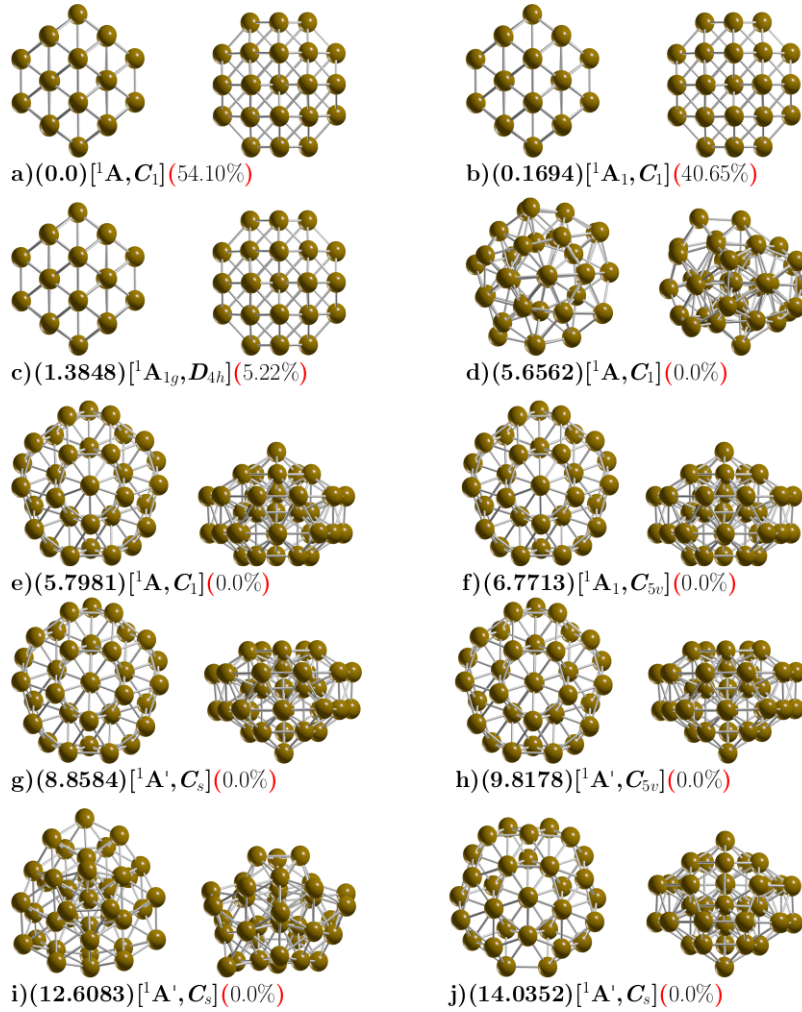


Figure 6.1: Optimized geometries in front and side views of neutral  $\text{Cu}_{38}$  cluster.

active vibration frequency is  $32.57 \text{ cm}^{-1}$  and is a semiconductor with electronic gap  $0.623 \text{ eV}$ . It is known that the bulk rare gas crystals have a face centered cubic (FCC) crystalline symmetry. Previous works on exploration of the potential energy surface of  $\text{Cu}_{38}$  cluster using genetic algorithms with Gupta potential often find highly symmetric TO structure,[333] other reported previous work employing *Sutton-Chen* potential with monte Carlo simulation also find TO structure.[273] The optimized Cu-Cu bond length is found to be  $2.4670 \text{ \AA}$  which is in good agreement with other reported DFT calculations Cu-Cu dimmer[351, 308] of  $2.248 \text{ \AA}$  and is consistent with the experimental bonding distance Cu-Cu  $2.22 \text{ \AA}$ . [351] Our computed diameter of TO structure is  $7.8 \text{ \AA}$  and also is in good agreement of  $8 \text{ \AA}$  reported in previous theoretical DFT calculations.[308] The second structure higher in energy lies at  $0.16 \text{ kcal/mol}$  at temperature of  $298.15 \text{ K}$  also is a TO structure with point group symmetry  $C_1$ , electronic ground state  $^1A$ , the lowest IR active vibration frequency

is  $32.13 \text{ cm}^{-1}$ , and is a semiconductor with electronic gap  $0.623 \text{ eV}$ , similarly to that of the putative global minimum. The next structure is slightly higher in energy located at  $1.38 \text{ kcal/mol}$  also is a TO structure, but with  $D_{4h}$  point group symmetry and electronic ground state  $^1A_{1g}$ , and the lowest IR active vibration frequency is  $33.44 \text{ cm}^{-1}$ . We also explored TO structure, initializing the geometry from the high-symmetries OH and TH and after geometry optimization without constrains, the OH and TH symmetries become  $C_1$  and  $D_{H4}$  symmetries. The perfect OH symmetry it could be deformed due to the *Jahn-Teller effect*[308, 351] and would have to be taken into account in the calculation of total energy[352, 353] and the relative population at temperature  $T$  could change as consequence in the optical properties. [354] Recently, in one of our previous works, we clarify the origin of Gibbs free energy differences between two similar structures just with different group symmetry, that is due to the rotational entropy, specifically the  $R T \ln(s)$  factor.[2] In this work, the energy difference of  $0.16$  between the two isomers depicted in Figure 6.1a with symmetry  $C_1$  and RMSD, the difference is  $0.08$  and is due to the Jean teller effect. The structure located at  $1.38 \text{ kcal/mol}$  above the putative global minimum with  $D_{4H}$  symmetry is due to rotational entropy. The next structure, shown in Figure 6.1d is located at  $5.65 \text{ kcal/mol}$  above the putative global minimum, with point group symmetry  $C_1$ , and electronic ground state  $^1A$ , the lowest IR active vibration frequency is  $24.16 \text{ cm}^{-1}$ , it is a distorted structure semiconductor with electronic gap of  $1.0 \text{ eV}$ , the calculated Cu-Cu bond distance is  $2.50 \text{ \AA}$  and the molecular diameter of this structure is  $9.1 \text{ kcal/mol}$ , slightly larger Cu-Cu bond distance and diameter than the global minimum, this structure possesses the the smallest relative ZPE energy, as shown in Figure, as well as the smallest frequency of the vibrational modes of all isomers. The next two higher energy structures shows in Figure 6.1(e,f) are located up to  $5.8 \text{ kcal/mol}$ , an both of them are the incomplete-Mackay icosahedron (IMI) with  $C_1$  and  $C_{5V}$  point group symmetries and electronic ground state  $^1A$  and  $^1A_1$  respectively. For both cases, the molecular diameter is  $8.54 \text{ \AA}$  electronic gap of  $0.97 \text{ eV}$  and the Cu-Cu bonding distance is  $2.47 \text{ \AA}$ . There are other higher energy structures shows in Figure 6.1(g,h,i,j), these do not contribute to any molecular property in all temperature range. In the Figure C.5, Appendix C.6, we depicted the lowest energy structures screening at B3PW91/def2SVP level of theory and without taking into account the atom-pairwise correction of Grimme GD3. The lowest energy structure is IMI structure with point group symmetry  $C_1$  and electronic ground state  $^1AH$ . The molecular diameter is  $8.69 \text{ \AA}$ , slightly larger than those found at TO structure of  $7.8 \text{ \AA}$  the average bond distance is  $2.50 \text{ \AA}$ . At PBE-GD3/Def2SVP level of theory, we found a IMI structure to be the most stable structure whereas at the PBE-GD3/LANL2DZ level of theory we found the TO structure as the putative global minimum energy. The complete description of the structures located at higher energies is in the Supplementary Information. We point out here, for the  $\text{Cu}_{38}$  clusters, the order energetically of the isomers and the energy gap among isomers as well as the putative global minimum interchange when we take into account the dispersion interactions.

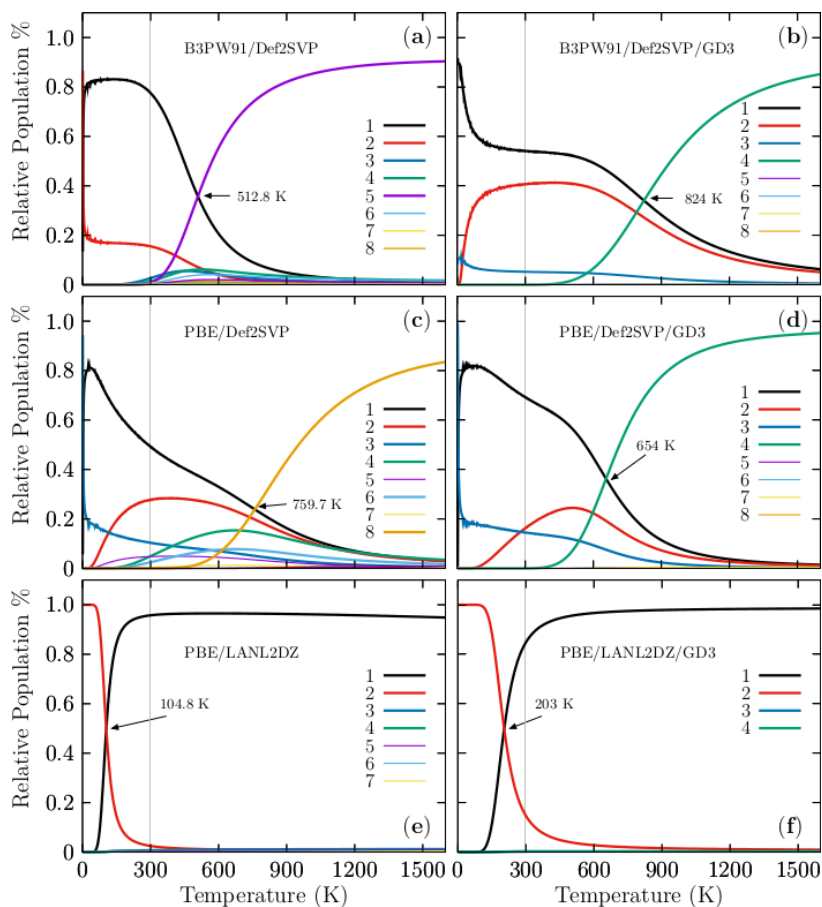


Figure 6.2: The thermal populations.

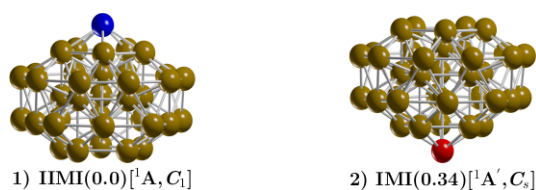


Figure 6.3: We depicted the inverted incomplete Mackay icosahedron, and the incomplete Mackay icosahedron.

### 6.3.1 Energetics

In the computation of energies employing different methods yield different results due to the functional and basis sets and therefore the energetic isomer ordering changes.[2, 236] The comparison of two different exchange-correlation functionals and two basis set and with and without taking into account the dispersion D3 the Grimme are shown in the Table 6.1. The optimizations performed at the

Table 6.1: The energetic isomer ordering.

Level of theory	Energy	Isomers (energy kcal/mol)									
		$i_a$	$i_b$	$i_c$	$i_d$	$i_e$	$i_f$	$i_g$	$i_h$	$i_i$	
B3PW91/Def2TZVP/GD3	$\Delta G$	0.0	0.16	1.38	5.65	5.79	5.81	6.76	8.85	9.81	
	$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.0	0.09	0.0	5.01	5.01	5.01	5.01	5.01	8.17	
	$\mathcal{E}_0$	0.05	0.0	0.10	8.76	4.89	4.89	4.88	4.88	4.88	
B3PW91/Def2TZVP	$\Delta G$	0.0	0.95	2.0	2.40	2.73	2.91	2.94	3.28	3.32	
	$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.0	0.0	2.14	3.29	6.52	3.84	2.14	3.27	3.84	
	$\mathcal{E}_0$	0.0	0.0	2.09	3.27	6.13	3.76	2.09	3.28	3.76	
PBE/Def2TZVP/GD3	$\Delta G$	0.0	0.86	0.92	5.02	7.23	7.59	7.81	8.88	12.27	
	$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.0	0.89	0.0	8.70	7.94	7.92	8.61	7.94	14.24	
	$\mathcal{E}_0$	0.0	0.90	0.0	9.14	7.92	7.93	8.84	7.94	12.47	
PBE/Def2TZVP	$\Delta G$	0.0	0.34	0.92	1.37	1.38	1.77	2.82	5.79	8.70	
	$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.0	0.0	0.37	0.41	1.77	1.77	1.77	9.08	15.75	
	$\mathcal{E}_0$	0.0	0.0	0.38	0.39	1.73	1.73	1.74	9.47	9.86	
PBE/LANL2DZ/GD3	$\Delta G$	0.0	1.02	3.37	3.46	8.63	9.11	9.59	9.62	9.74	
	$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	2.03	0.0	2.12	2.14	8.31	8.77	8.73	9.34	8.71	
	$\mathcal{E}_0$	1.97	0.0	2.01	2.01	8.08	8.60	8.52	9.12	8.45	
PBE/LANL2DZ	$\Delta G$	0.0	2.15	2.87	3.03	3.26	4.31	8.89	9.66	9.85	
	$\mathcal{E}_0 + \mathcal{E}_{\text{ZPE}}$	0.97	0.0	1.46	1.38	1.64	1.68	7.98	9.19	9.58	
	$\mathcal{E}_0$	0.86	0.0	1.27	1.11	1.48	1.42	8.03	8.99	9.37	

B3PW91/PBE-def2TZVP considering the dispersion yield the same type of lowest energy equilibrium geometry and similar energetic isomer ordering when we employ the electronic energy with and without ZPE correction energy and Gibbs free energy computed at room temperature. From the energetic point of view, the inclusion of dispersion is more important than the type of functional and basis set, i.e. The first line of the Table 6.1 show the relative Gibbs free energies computed at the B3PW91-D3/def2TZVP level of theory, the isomer label  $i_b$  in the Table 6.1 and depicted in Figure 6.1b is located 0.16 kcal/mol above the putative global minimum whereas the second line of the Table 6.1 show the relative Gibbs free energies computed at the B3PW91/def2TZVP level of theory and the isomer  $i_b$  in the Table 6.1 and depicted in Figure 6.1b is located 0.95 kcal/mol above the putative global minimum as it is shown in Table 6.1. For isomer  $i_b$ , the effect of the dispersion on the energy is decrease the relative Gibbs free energy with respect to the putative global minimum. (from 0.95 to 0.16 kcal/mol). The effect of dispersion, in the case of isomers  $i_c$ , is also decrease the relative Gibbs free energy with respect to the putative global minimum from 2.0 to 1.38 kcal/mol whereas for isomer label  $i_d$ , the relative Gibbs free energy increase from 2.4 to 5.65 kcal/mol. In summary, the effect of dispersion reduces the Gibbs free energy in the lowest energy structures where the Boltzmann factors are different from zero. A overall comparison of free energies computed with functional B3PW91, second line of the Table 6.1, and PBE in four line in the Table 6.1, versus free energies computed with functional PBE, four line



of the Table 6.1, and PBE in four line in the Table 6.1, shows a reduction in the relative Gibbs free energies when the PBE functional is employed. For the case of the basis set the LANL2DZ increase the relative Gibbs free energy in the low energy isomers as it is shows a comparison of line 6 of Table 6.1 versus line 1 of Table 6.1.

### 6.3.2 Relative stability

The probability of finding the TO structure with  $C_1$  symmetry at B3PW91/def2-SVP level of theory is depicted in black-solid line in panel (a) of Figure 6.1(4). It strongly dominates from 0 to 300 K, thus all the molecular properties are due only to this structure. From slightly before 300 K, it start to decay exponentially and almost disappear at 900 K, at the same time, the probability of finding the amorphous structure with point group symmetry  $C_1$ , is depicted in violet-solid line in Figure 6.2(a), it start to grow exponentially and become dominate at temperature above 512.8 K and at 900 K it become strongly dominate. At solid-solid transition temperature of 512.8 K the TO and the amorphous structure co-exist. The effect of dispersion can be appreciated in panel (b) of Figure 6.2. The relative population is computed at B3PW91-G3/def2-SVP level of theory. The effect of the dispersion is dramatic, the solid-solid transformation point is shifted from 512.8 to 824 K, an increase of 160% and from the panel (b) one can see that the molecular properties below 600 K, are due to only the TO structure. Slightly before 600 K, The probability of finding the amorphous structure, depicted in green-solid line in panel (b), start to grow up exponentially and at temperature of 824 K the TO and amorphous structure co-exit. Whereas a temperature of 600 K the probability of find the TO structure start do decay exponentially and at 900 K its value still around 20%. The probabilities of occurrence at the PBE/def2-SVP level of theory of a particular Cu<sub>38</sub> isomer are displayed in panel (c) of Figure 6.2. The dominant putative global minimum structure at T=0, is the inverted incomplete-Mackay icosahedron (IIMI) structure depicted in Figure 6.3a with  $C_1$  symmetry and its probprobability of finding it is depicted as a black solid line in panel (c) of Figure 6.2. Its probability decays almost linearly until 1000 K where it almost disappears. At temperature of 759.7 K, the solid-solid transformation point, the IIMI structure co-exist with an amorphous structure. The probability of finding the amorphous structure start to grew up at 600 K, and above of solid-solid transformation point, it start to strongly dominate as putative global minimum. Where the probability of finding the IMI structure is depicted in red-solid line on panel (c) of Figure 6.2, the largest probability is 30% at room temperature. Interesting, the probabilities of IIMI and IMI structures does not cross at cold temperature. Zhang *et al.* [325] reported that IMI structure could be highly competitive at finite temperatures, but our findings shows that the amorphous structure with  $C_1$  symmetry is highly dominant at hot temperatures, whereas the IIMI structure is highly dominant at cold temperatures.

For ease comparison, the Figure 6.3 display the IIMI and the IMI structures side by side. At cold and the IIMI structure dominate. The effects of dispersion is shift the solid-solid transformation point to lower temperatures from 759.7 K to

654 K as one can see in panel (d) Figure 6.2. The probability of finding the IIMI structure as a function of temperature is depicted in black solid-line and it decays approximately linearly from 50 to 500 K, after that it decays exponentially until 900 K where it disappears. At around 400 K, the probability of finding the amorphous structure, depicted in green solid-line in panel (d) of Figure 6.2, start to grow up in exponential way, and at temperature of 654 K it co-exit with the IIMI structure. Above 654 K, the amorphous structure becomes energetically favorable.

### 6.3.3 IR spectra at finite temperature

The properties observed in a molecule are statistical averages over the ensemble of geometrical conformations or isomers accessible to the cluster, so the molecular properties are governed by the Boltzmann distributions of isomers that can change significantly with the temperature primary due to entropic effects.[2, 1, 64] The major contributions to the entropy are the many soft vibrational modes that the clusters possesses. The IR spectrum is related to vibrations or rotations that alter the dipole moment, and it will happen in molecules that have a dipole moment. Also, the IR spectrum is related to the curvature of the potential curve versus interatomic distances. Complete information about molecular vibrations allows us to analyze catalytic chemical reactions.[355, 356] IR spectra are used to identify functional groups and chemical bond information. However, assigning IR bands to vibrational molecular modes in the measured spectra can be difficult and requires DFT calculations; as we mentioned earlier, the temperature is not considered in these computations and discrepancies between experimental and computed IR spectra can result from finite temperature, anharmonic effects, and multi-photon nature of experiments, whereas IR computations assume single-photon processes.[1, 2] The IR spectra of isolated metal clusters in the gas phase for vanadium cluster cations as well as for neutral and cationic niobium clusters were measured.[357] Even though Cu clusters are important in catalysis and were the first clusters experimentally produced,[358] the available structural information is limited to study photoelectron spectroscopy for anions, mass spectrometry, and photodissociation spectra in the visible range.[359] Recently, Lushchikova *et al.* [359] determine the structure of small cationic copper clusters based on a combination of IR spectroscopy of  $\text{Cu}_n^+-\text{Ar}_m$  complexes and DFT calculations. In this chapter 6, the IR spectra of isomers computations were carried out using the Gaussian package under harmonic approximation at level of theory PBPW91-D3[360]/def2TZVP and full width at half maximum (FWHM) of  $8 \text{ cm}^{-1}$  taking into account the dispersion of Grimme D3 as implemented in Gaussian code. Negative frequencies were checked in all calculations to ensure that there were not transitions states. The computed frequencies were scaled by 0.98 to estimate the observed frequencies. Here, the total IR spectrum is computed as a weighted Boltzmann sum of the single IR spectrum of each isomer of the distribution at finite temperature[2, 1, 268, 361] given by:  $\text{IR} = \sum_{i=1} w_i \text{IR}_i$ , and the probabilities of occurrence displayed in Figure 6.2. To our knowledge, there are a few theoretical studies on IR spectra of noble metal clusters computed considering a weighted sum

of the IR spectra of isomers. [361] Computed weighted Boltzmann IR spectra of  $\text{Cu}_{38}$  clusters at different temperatures are shown in Figure C.3, Appendix C.4. Notice that the transition metal clusters are very stable, and its vibrational frequencies are found below  $400\text{ cm}^{-1}$ [362] in good agreement with our computed spectra displayed in Figure C.3, Appendix C.4.

### 6.3.4 UV-Visible spectra at finite temperature

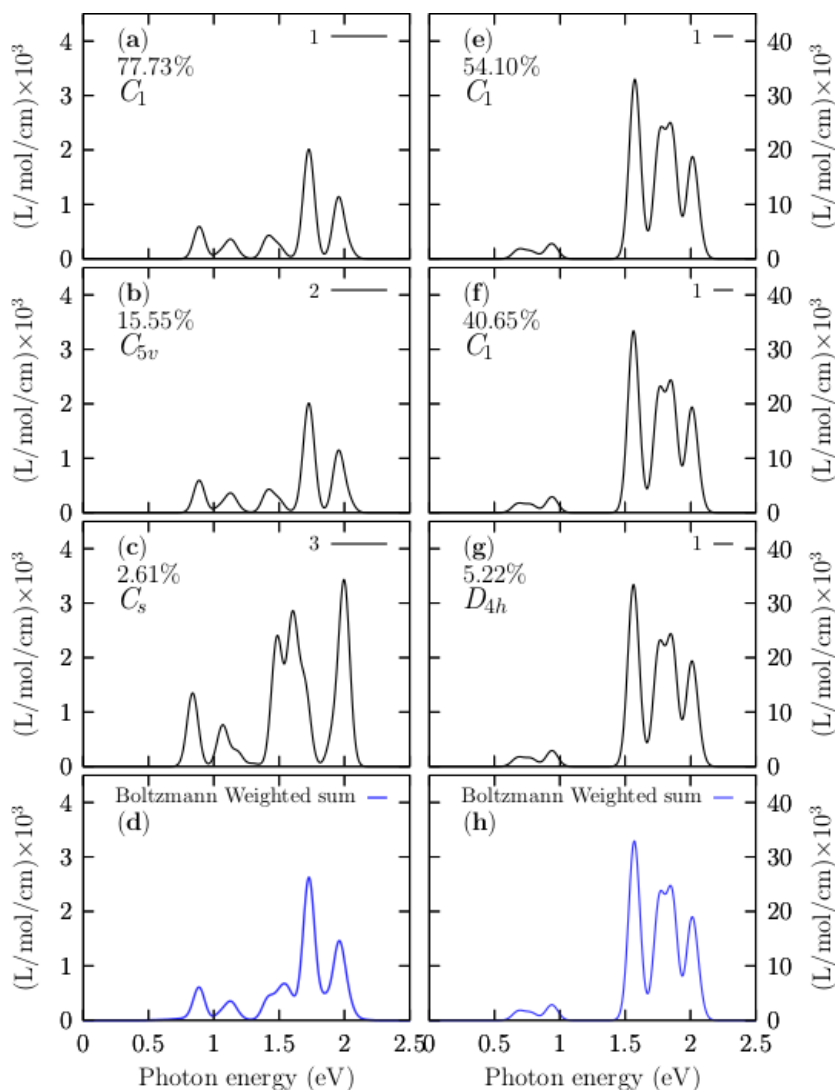


Figure 6.4: The UV-visible Boltzmann spectra weighted at room temperature of the neutral  $\text{Cu}_{38}$  cluster.

The optical properties are a source of structural information, and their electronic structure determines them.[363, 364] In this paper the TD-DFT was used

to compute the optical absorption spectra in the UV-visible range  $0.5 < \hbar\omega < 2.5$  eV for the  $\text{Cu}_{38}$  cluster. We employ the CAM-B3LYP functional, Def2-TZVP basis set, and 50 singlets and 50 triplets states. The transition metals clusters allow us to study the influence of the **d** electrons on the optical properties; it is known that the **d** electrons strongly influence the surface plasmon response.[268] We show in Figure 6.4 the UV-spectra for the  $\text{Cu}_{38}$  cluster with and without the Grimme's dispersion D3. To take into account the effects of temperature on the UV-visible spectra. We consider that the UV-visible spectrum of a molecular ensemble is a weighted sum of all the individual contributions of each isomer that forms the ensemble. In panel labeled (e) is displayed the UV spectra considering the Grimme's dispersion GD3 and for the lowest energy structure with symmetry  $C_1$ ; this structure contribute with 54% to the total Boltzmann spectrum. In panel (f) is displayed the UV-visible for the low-energy structure located at 0.16 kcal/mol at room temperature and above the putative global minimum with  $C_1$  symmetry, and this contributes to 40% to the Boltzmann spectrum. In panel (g) is displayed the UV-visible for the low-energy structure located at 1.38 kcal/mol at room temperature and above the putative global minimum with  $D_{4h}$  symmetry, and this contributes to 5.22% to the Boltzmann spectrum. In panel (h) is displayed the Boltzmann weighted UV-Visible spectrum at room temperature. Notice that all absorption spectra, (g) to (h), are similar; The Boltzmann weighted UV-Visible spectrum presented in Figure 6.4, panel (h) is composed of three peaks located between 1.5 to 2 eV and smaller intensity peaks located at 0.5 and 1.0 eV. The most significant absorption peak is located at 1.6 eV. Our computations show five absorption peaks of the UV-visible spectrum starting at 0.5 eV and finishing at 2.5 eV. Notice that the total optical spectrum is due only to the putative global minimum; despite the number of isomers growing exponentially, the main contribution to the optical properties comes from those low energy structures very close to the global minimum where weights Boltzmann factors temperature dependents are different from zero. Interestingly, the second low-energy structure located at 0.16 kcal/mol (room temperature) above the putative lowest energy structure screen or blocked the contributions to the Boltzmann optical spectrum of the other structures. In this paper, we called those structures as *shielding structures*. In Figure 6.4, panels (a) to (d) are displayed the optical absorption spectra in the UV-visible range computed with structures optimized without the Grimme's dispersion D3. Notice the effects of dispersion on UV-visible spectra is introduced by the change of the relative population when the optimizations are computed without, and with dispersion, e.g., the contribution, to the Boltzmann weighted UV-Visible spectrum, of the lowest energy structure computed without Grimme's dispersion D3 is 77% meanwhile, the contribution is 54% when an optimized structure is computed with Grimme's dispersion D3. The complete evolution of the Boltzmann weighted UV-Visible spectra for temperatures ranging from 10 to 1500 K is displayed in Figure C.4, Appendix C.5.

### 6.3.5 Molecular Dynamics

We performed Born-Oppenheimer molecular dynamics (MD) of the Cu<sub>38</sub> cluster employing the deMon2K program[189] (deMon2k v. 6.01, Cinvestav, Mexico City, Mexico, 2011) at temperature of 600 K, aiming to gain insight into the dynamical behavior of the Cu<sub>38</sub> cluster. The MD started from global putative minimum structure. The simulation time was 25 ps with a step size of 1 fs. All computations were performed under scheme of ADFT,[365] and for the basis set we employed the double zeta plus valence polarization (DZVP) all-electron basis. We employed the Nosé-Hoover thermostat to fix the temperature and the linear and angular momenta of the cluster Cu<sub>38</sub> were initialized to zero and conserved.

## 6.4 Conclusions

For the first time, to our knowledge and from our results, we proposed the inverted incomplete-Mackay icosahedron (IIMI) with symmetry C<sub>1</sub> as low-energy structure[55] than the incomplete-Mackay icosahedron (IMI) with symmetry C<sub>s</sub> and located 0.34 kcal/mol energy above the putative minimum global at 298.15 K. The yellow, the IIMI structure is the result of interchanging the red Cu atom depicted in the IMI structure to the position of blue atom in the IIMI structure. The IMI structure was reported in The HOMO-LUMO gap of the IMI structure is 0.24 eV (0.356 eV reported by previous DFT studies[325]) whereas for the HOMO-LUMO gap for IIMI structure is 0.30 eV, suggesting why the IIMI structure is energetically more stable.

# Conclusions

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## 7.1 Conclusions

In this chapter, I list the main findings and the theoretical contribution made in this thesis to the nanoclusters and nanothermodynamics fields. I also propose new lines of investigation and perspectives.

1. Effects of temperature-symmetry in atomic nanoclusters
2. The effect of temperature on molecular properties
3. The development of the methodology based in nanothermodynamics and DFT to compute the molecular properties as a function of temperature.

The major conclusions of this doctoral thesis on different nanoclusters were as follows:

### 7.1.1 The $\text{Be}_6\text{B}_{11}^-$ cluster

We computed the relative population as a function of temperature using Boltzmann factors and the IR spectra dependent on temperature as a Boltzmann weighted sum of each IR spectrum's isomer. Here, we demonstrate that the temperature and entropic effects produce several competing structures, so a mixture of isomers co-exist at a specific temperature. Our computations showed (with relative population) that the low-symmetry isomers have a higher stability than isomers with high symmetry at high temperatures as a result of the entropic effect. The coaxial triple-layered structures with  $C_s$  symmetry are the putative global minima above 377 to 1500 K due to entropic effects. There are four  $T_{ss}$  points in the relative population of the  $\text{Be}_6\text{B}_{11}^-$  cluster; the most important and dominant of these is the  $T_{ss}$  point located at 377 K with a relative population of 33%. Additionally, our results give insight into the long-range *van der Waals* interactions effects on the solid-solid transformation temperature points, hence the molecular properties. Indeed, the effect of dispersion shifts up in temperature the dominant  $T_{ss}$  point, keeping the relative population almost invariant. The other  $T_{ss}$  points shifted down on the temperature axis, so there is no clear trend in the up/downshifts in the  $\text{Be}_6\text{B}_{11}^-$  cluster. Remarkably, the coaxial triple-layered structures with  $C_s$  and  $C_{2v}$  symmetries have the lowest B-B bond length, and the same geometrical structures have the lowest relative zero-point energy. This suggests that both trends shortening of the B-B bond length and lowest

relative zero-point energy are correlated with entropic effects. Analysis of our results leads to an interesting observation: The strong dominant putative global minimum, under high-temperature conditions, has the shortest B-B bond length and the lowest relative zero-point energy. The low vibrational modes significantly contribute to entropy, whereas high vibrational modes provide small contributions to entropy. The  $\text{Be}_6\text{B}_{11}^-$  cluster has 45 vibrational modes. We found the range of frequencies—the lowest to the highest vibrational modes that contribute to zero-point energy by computing the zero-point energy as a function of vibrational modes. We needed to sum the first 38 modes that contribute to zero-point energies; the frequency range was between 46 and 1026  $\text{cm}^{-1}$ . Vibrational modes outside of this range do not contribute to the zero-point energy. At the energy single-point CCSD(T) level of theory, the energetic ordering of isomers changes with respect to employing the electronic or Gibbs free energies. The inclusion of the zero-point energy in CCSD(T) energies illustrates that the energy difference among isomers reduces drastically, which suggests that the dominant putative global minimum at zero temperature when we employ the CCSD(T) energies will change with the inclusion of temperature. The properties observed in a molecule are statistical averages over the ensemble of geometrical conformations or isomers accessible to the cluster, so the molecular properties are ruled by the Boltzmann distributions of isomers, which can change significantly with temperature, primarily due to entropic effects. We computed the IR spectra dependent on temperature as a Boltzmann weighted sum of each IR spectrum's isomer. Our computations showed that the competing structures provide a different percentage to the entire molecular properties and IR spectra, in detail, the molecular properties can not be attributed to only the lowest energy structure. The structures located at high energy above the putative global minimum that have a significant energy difference among isomers on the potential/free energy surface do not contribute to the entire IR spectrum. Despite the number of isomers growing exponentially, the main contribution to the molecular properties comes from the low-energy structures close to the global minimum where the weighted Boltzmann factors temperature dependence are different from zero. (This depends strongly on the energy separation; if the energy separation is significant, the IR spectrum does not change.) The spectra that belong to the low-energy structure dominate the IR spectrum of the  $\text{Be}_6\text{B}_{11}^-$  cluster at low-temperature structures, whereas at high temperatures, it is strongly dominated by the spectra of structures located at high energy above the putative lowest energy structures. The increase/decrease in a peak/band in the IR spectra as a function of temperature is a clear signature of an interchange of the dominant lowest energy structure. With the IR spectra, we illustrated that the main contributions to the molecular properties are from the low-energy structures that are very close to the global minimum where the weighted Boltzmann factors temperature dependence is different from zero. The present thesis highlights the importance of entropy-temperature effects and what happens when some low-energy structures are not considered. We show that symmetry plays an important role in the definition of the global minimum and hence in molecular properties. We demonstrate that dispersion effects has a little the changes of the  $T_{SS}$  points in temperature scale.

All of these effects have an impact on the spectroscopic and any other property of a molecular system. The Boltzmann-IR-spectra as a function of temperature were presented. The spectra unravel that the peak located at  $1500\text{ cm}^{-1}$ , shows in Figure 8, panels (a-d), is present only in temperatures higher than 300 K, where the coaxial-triple layered structures start to be the lowest energy structures. The above mentioned reasons indicate that the vibrational modes located in the range of  $1036$  to  $1518\text{ cm}^{-1}$  are responsible for the cluster's fluxionality. An immediate future project is the computation of the optical spectra and other molecular properties employing the methodology described in this chapter and the computation of the relative population in many atomic and molecular clusters of interest employing higher levels of theory.

### 7.1.2 The $\text{Be}_4\text{B}_8$ cluster

We initially sampling the potential energy surface with 2400 candidates of neutral  $\text{Be}_4\text{B}_8$  structures, and with an efficient cascade type algorithm coupled to DFT; We were able to locate twenty-two final isomers within an energy range of 9.2 kcal/mol, six of which are chiral low energy structures with symmetries  $C_1$ ,  $C_2$ , and  $D_2$  respectively, as far as we know not yet reported as chiral structures. They are constituted by a sandwich structure type in which the boron atoms from a distorted ellipsoid ring with each Be-Be dimers are capping each side of the sandwich. Our findings show that the chirality that exhibits the  $\text{Be}_4\text{B}_8$  cluster emerges from the Be-Be dimers' mirror position. Additionally, based on the AdNDP analysis and the computed transition state and IRC between  $\mathcal{P}$  and  $\mathcal{M}$  enantiomers, we can deduce that the Be-Be and Be-B interaction favors the  $\text{Be}_4\text{B}_8$  to be chiral and energetic minimum structure. According to our calculations, the enantiomerization energies barriers of the transformation  $\mathcal{P}$  to  $\mathcal{M}$  and  $\mathcal{M}$  to  $\mathcal{P}$  is equal to each other, moreover the activation energy between  $\mathcal{P}$  to an achiral structure and  $\mathcal{M}$  to an achiral structure are equal, thus the Boltzmann ensemble is composed of an equal mixture of  $\mathcal{M}$  and  $\mathcal{P}$  enantiomers. The enantiomerization energy between the chiral putative global minima in the ranging of temperatures from 20 to 1900 K is mainly composed of enthalpic than entropic term. The entropy-temperature term reduces the interconversion energy barrier like maximum in 28%; thus, the barrier is not influenced significantly by the entropic term. On the other hand, our results show that the energy barrier is 6.20 kcal/mol at room temperature between the lowest energy enantiomer ( $\mathcal{P}/\mathcal{M}$  and the first achiral structure located at 1.79 kcal/mol at 298.15 K. The barrier does no increase significantly neither at cold temperatures nor at hot temperatures, the barrier high at 20 K is 6.43 kcal/mol. In contrast, it is 7.32 kcal/mol at 1900 K. Remarkably, the interconversion between enantiomers and achiral structure is more favored than the interconversion between a pair of enantiomers in all ranges of temperature. Furthermore, our results show that in the temperature range from 20 to 738 K, the interconversion between an enantiomer ( $\mathcal{P}/\mathcal{M}$  and the achiral structure is an endothermic type reaction. At the transformation solid-solid point located at 739 K, the enthalpy of reaction is zero, and the energy barrier is



a minimum. In this point coexist the  $\mathcal{P}$  and  $\mathcal{M}$  structures with an achiral structure. At 739 K, above the interconversion between enantiomers-achiral structures are exothermic, which implies the heat of reaction. Notice that the change from endo to exothermic reaction is driven by entropic-temperature term. In this study and for the first time, we defined two novel points on a scale of temperature. a) The first one is the  $T_{ee}$  where the change in the reaction type occurs, and b) the second is the  $T_{bb}$  where the activation energy of two different reaction mechanisms are equal to each other, so the reaction rate equals. The energetic ordering of the isomers when we employing the Gibbs free energy computed at 298.15 K agree with the energy ordering employing the single point CCSD(T) energies computed with DLPNO-CCSD(T), and the energy ordering change just with the interchange of the two achiral structures located at 3.61 kcal/mol and 3.38 kcal/mol above the putative global minimum. Furthermore, Our results on  $\mathcal{T}_1$  diagnostic confirm that energies computed at the DFT level of theory do not contain a large multireference character, so the  $\text{Be}_4\text{B}_8$  cluster is well characterized. Regarding relative population, our findings show that the putative global minimum that clearly and strongly dominates at cold temperatures is the pair of enantiomers. At 739 K, above, an achiral structure dominates as a putative global minimum with less than 20%. We also show that the relative population or Boltzmann distribution could depend on the functional and the basis set employed. The energy separation among isomers affects the relative population strongly. The Boltzmann distribution is composed of six isomers at 298.15 K with only different symmetries, and its contribution is approximately 98% thus, at room temperature, the molecular properties are strongly dominated by the pair of enantiomers putative global minimum. We analyzed the effects of the point group symmetry on Gibbs free energy as a function of temperature. The small Gibbs free relative energy differences of 0.41 and 0.81 kcal/mol between different symmetries at 298.15 K are due to rotational entropy that in fact, it is a function of number of symmetry, and it become larger at the temperature increase. This strongly suggests that we need to explore the free energy surface taking into account clusters with low symmetries. The low symmetries trends to dominate as putative global minimum as the temperature increases. For total VCD/IR spectra as a function of temperature, we compute the Boltzmann weighted superposition of each isomer's VCD/IR spectrum that yields a total VCD/IR spectrum. Boltzmann VCD weighted spectra for this particular chiral cluster is null in all range of temperature because in the ensemble P and M enantiomers are present in equal mixture. However, a clear temperature dependence of the Boltzmann IR weighted spectra is driven just by the probability of the putative low-energy isomers in the temperature ranging from 20 to 739 K. At temperature above 739 K, the IR spectra decay strongly, whereas, at a temperature above 1200 K, the IR spectra are almost null. In summary, IR spectra at room temperature are dominated by pair of enantiomers putative global minima, whereas at hot temperatures, the IR spectra are almost null. Our molecular dynamics corroborate that the melting point is located in the temperature ranging from 1400 to 1500 K, because and in accordance with molecular dynamics, the dissociation phenomenon occurs at 1500 K, and the melting point is

located below this point. As future work, the inclusion of anharmonic effects should be taken into account also the relative population at CCSDT(T) level of theory is going to be calculated. The melting point also should be computed. At finite temperature the entropy is maximized, taking into account this, a future project is a implementation of an algorithm to search on the free energy surface employing the entropy as an objective function instead of energy. Finally, we point out that in any reaction, the activation energy at finite temperature must be computed considering the reactants and products with non-symmetry ( $C_1$ ), by reason of the small energy differences dependent on symmetry and temperature (i.e 0.41 kcal/mol for  $C_2$  at 298.15 K) increase the energy barrier between the reactants and products, hence the velocity of the reaction could be miscalculated. The Boltzmann Optics Full Adder (BOFA) *Python* code supporting the findings of this study is available from the corresponding author upon reasonable request.

### 7.1.3 The $Cu_{13}$ cluster

Our computed  $\mathcal{T}_1$  diagnostic 0.023, determine that the computed DFT energies are not properly described by a single reference method or contain a multireference character. So, further studies needed to be done. We explored the potential and free energy surface of the neutral  $Cu_{13}$  cluster with an efficient cascade-type algorithm coupled to DFT. We found that the putative global minimum was a pair of enantiomers that strongly dominated at room temperature. Our findings show that the chirality exhibited by the  $Cu_{13}$  cluster emerged from the Cu atom capping a face of the core  $Cu_{12}$  cluster. We showed that for the interconversion between  $\mathcal{P}$  and  $\mathcal{M}$  structures, two similar reaction mechanisms were possible. Both of them closed in their energy barriers and proceeded via two symmetric steps. The energy of enantiomerization and the energy barrier between the intermediate and the  $\mathcal{P}/\mathcal{M}$  structures increased as the temperature increased. We computed the reaction rate constants based on the Eyring equation; our findings show that at high temperatures, enantiomerization is favored. The entropic-temperature term did not significantly influence the energy barriers; thus, they are mainly composed of enthalpic energy. Regarding Grimme’s dispersion D3, this lowers the energy barriers, i.g., in route B, the EA decreased by 7% (from 4.3 to 4.0 kcal/mol). We showed that the pair of enantiomers with  $C_1$  symmetries strongly dominated at room temperature revealed by the thermal population. Hence, at body temperature, all the molecular properties were attributable to those structures. For each DFT functional (B3PW91, TPSS, PBE, and BP86) used in this study, the thermal population and energetic ordering of the isomers are preserved, although differences in the energy between the isomers occur; the main contributors to any molecular property of  $Cu_{13}$  are always the chiral isomers. The bonding in the lowest energy chiral  $Cu_{13}$  cluster is due to the 4s shell electrons for which the bonding pattern, as revealed by AdNDP, consisted of 6 sets of 13c-2e completely delocalized bonds, plus a 9c-1e bond corresponding to the unpaired electron. Future work will focus on the computation of UV absorption of the Cu clusters employing Boltzmann weighted spectra,

comparing it with a single UV spectrum of the putative global minimum.

#### 7.1.4 The $\text{Cu}_{38}$ cluster

We computed the effect of symmetry on the Boltzmann populations on  $\text{Cu}_{38}$  clusters. In spite that the number of isomers grows exponentially, the main contribution to the optical properties comes from those low energy structures very close to the global minimum where weights Boltzmann factors temperature dependents are different from zero. We performed an unbiased global search for minimum energy  $\text{Cu}_{38}$  clusters structures using a two-stage strategy. First a global search using a semi empirical methodology, followed by a density functional theory optimization of the best structures from the first stage was done at different levels of theory. The temperature and entropic effects cause several competing structures because energy separation between isomers on the free energy surface is small and changes the dominant structure, so probably a mixture of isomers interconverted at temperature finite. Those energetically competing structures provide a different percentage of the entire IR spectrum. On the other hand, those higher energy structures with significant energy separation among isomers on the potential energy surface do not contribute to the entire IR spectrum. Despite that, the number of isomers grows exponentially. The main contribution to the molecular properties comes from those low-energy structures very close to the global minimum, where weight's Boltzmann factors temperature dependents are different from zero. (depends strongly on the energy separation, if the energy separation is significant, the IR spectrum going to be rigid, not changes) A motif is dominant in cold conditions, whereas the other motif is dominant in other hot conditions; additionally, the level of theory is decisive in the computations of TSS point dependent-temperature Our computations clearly show (relative population) that the low-symmetry isomers become more stable at high temperatures due to the entropic effect and the fact that energy states of molecules follow Boltzmann distribution in all six different levels of theory. Our unbiased global search on the free energy surface show that there is an amorphous structure that strongly dominate at hot temperatures, as far as we know this is a novel putative global minimum at hot temperatures. As immediate work is the computations of the relative populations at high level of theory and compute the  $\mathcal{T}_1$  diagnostic to determine that the computed DFT energies are not properly described by a single reference method or contain a multireference character. So, further studies needed to be done.

## 7.2 Perspectives and future work

The cluster proprieties depends strongly on the structure, size, composition and temperature and with the aim to compute molecular properties is necessary to consider statistical thermodynamics; the first step in order to understand the molecular properties is the elucidation of the lowest energy structure and its isomers. I underline that the temperature is a key in the chemical reactions, so to compare the-

oretical computations and experiments, the temperature must be considered. The experiment studies are carrying out in non-zero temperatures and its necessary to understand what are the effect of the temperature. Future work should be adressed in these points:

- Computations at a high level of theory, like CCSD(T) level.
- Corrections at high temperatures.
- Computations on nitrogenous bases and nucleic acids like DNA and RNA.



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# Appendices



# Appx. Congress

## A.0.1 Attendance certificate *LatinXchem* 2021.



September 24, 2021



Gabriel Merino  
on behalf of the  
#LatinXChem Organizing Committee

Andrés Cisneros  
#LXChemComp.organizer

Fernanda Duarte  
#LXChemComp.organizer

Joaquín Barroso  
#LXChemComp.organizer


Figure A.1: Attendance certificate of work presented in the: LatinXchem 2021, Nov. 2012, Virtual Twitter

A.0.2 Attendance certificate *LatinXchem* 2021.

September 24, 2021



Gabriel Merino  
in behalf of the  
#LatinXChem Organizing Committee



Andrés Cisneros  
#LXChemComp organizer



Fernanda Duarte  
#LXChemComp organizer



Joaquín Barroso  
#LXChemComp organizer

Figure A.2: Attendance certificate of work presented in the: LatinXchem 2021, Nov. 2012, Virtual Twitter

# Appx. $\text{Be}_4\text{B}_8$

## B.1 Probability of occurrence computed at TPSS-GD3/def2TZVP level of theory.

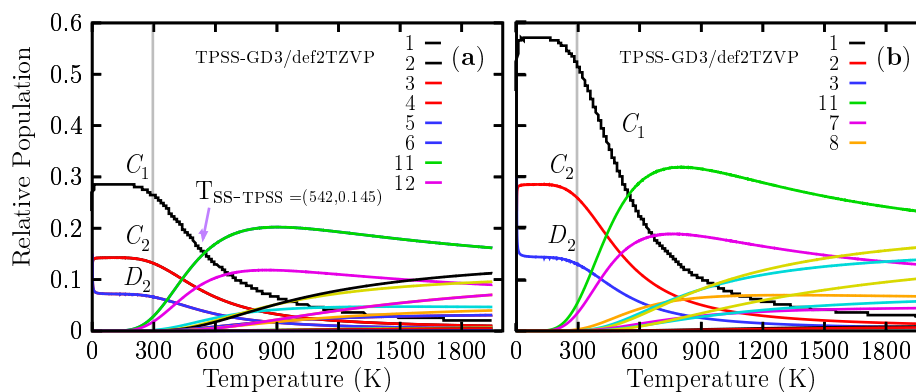


Figure B.1: Probability occurrence.

For temperatures ranging from 20 to 542 K, the chiral structure, depicted in Figure 4.1(a), strongly dominates as a global minimum. At 542 K, a type-helix chiral structure coexists, depicted Figure 4.1(k), with the chiral putative global minimum at cold temperatures. For temperatures ranging from 543 to 1600 K, the chiral structure's type-helix chiral structure dominates as the putative global minimum. A large difference between the TSS point computed with TPSS functional [239] and that computed with PBE0 functional [179]. Thus, it is important to choose the DFT functionals and basis that better describe the system to calculate the relative population and any Boltzmann weighted property.

## B.2 Be-Be and B-B bond length evolution for enantiomers

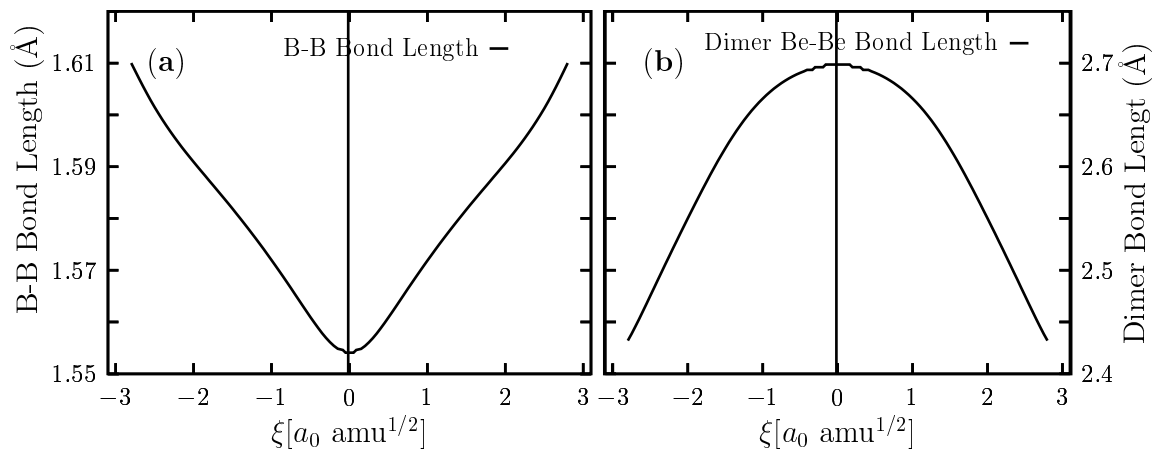


Figure B.2: Figure shows the bond length evolution of the Be-Be dimer.

## B.3 Energy of enantiomerization

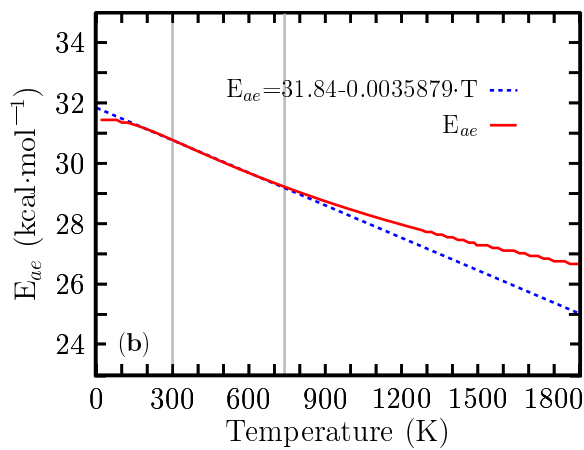


Figure B.3: We show a perfect line depicted in the blue dashed line.

## B.4 IR Harmonic vs Anharmonic spectra

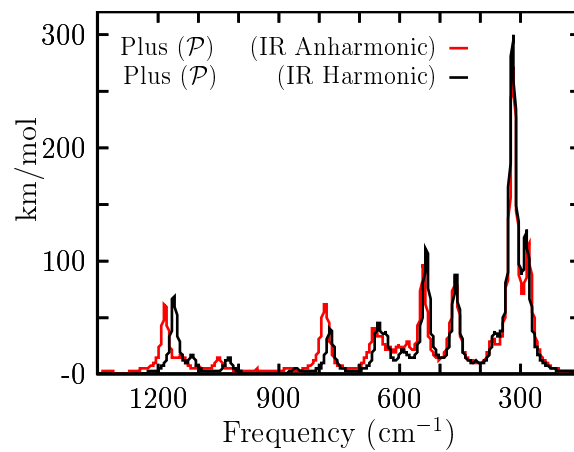


Figure B.4: We show a comparison between IR Harmonic vs IR Anharmonic spectra.





Appx.  $\text{Cu}_{13}$ 

## C.1 TPSS/def2-TZVP PBE/def2-TZVP PB68/def2-TZVP

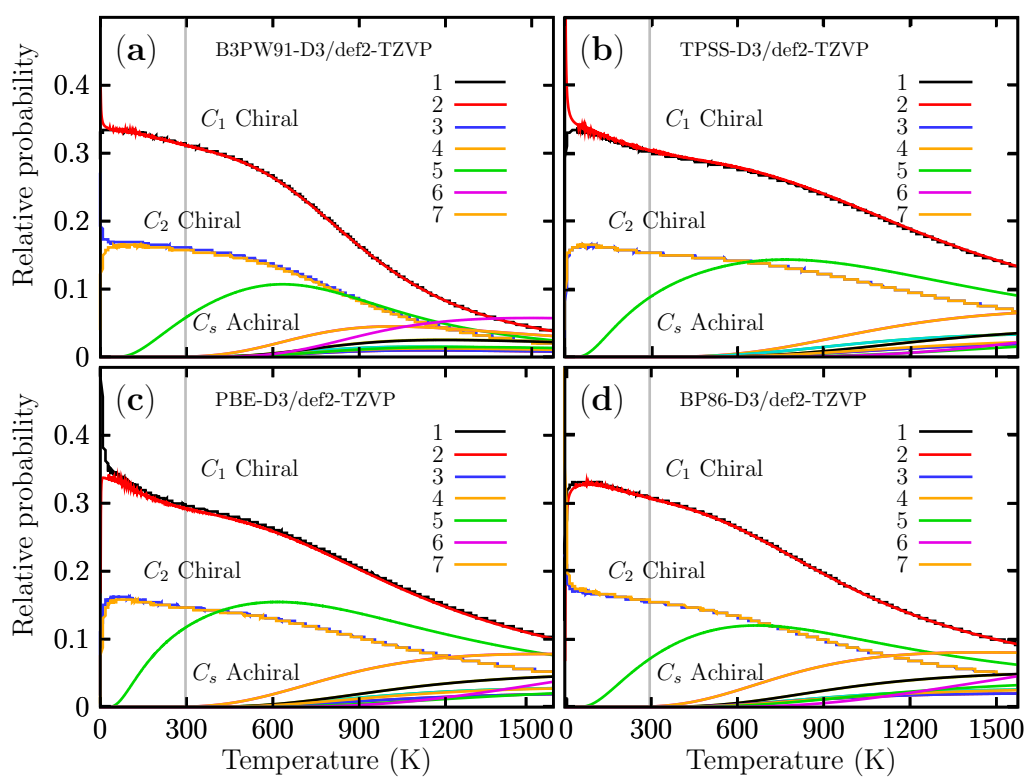


Figure C.1: Probability of occurrence for all isomers.

C.2 XYZ atomic coordinates of  $\text{Cu}_{13}$ 

13

0.0

Cu	-0.990009000000	0.202990000000	0.910273000000
Cu	0.989148000000	0.203204000000	-0.910494000000
Cu	1.307754000000	0.817211000000	1.506707000000

---

Cu	-0.756524000000	-1.521352000000	-1.012184000000
Cu	-2.995439000000	-0.494575000000	-0.267184000000
Cu	-0.000551000000	2.308713000000	-0.000120000000
Cu	1.705678000000	-2.128579000000	-1.124758000000
Cu	2.995766000000	-0.493776000000	0.267529000000
Cu	0.756822000000	-1.521006000000	1.012214000000
Cu	-1.308834000000	0.816218000000	-1.506262000000
Cu	-1.705107000000	-2.129263000000	1.124856000000
Cu	2.516484000000	1.969366000000	-0.285914000000
Cu	-2.515188000000	1.970848000000	0.285338000000
13			
0.0			
Cu	0.000000000000	1.344973000000	0.202955000000
Cu	0.000000000000	-1.344973000000	0.202955000000
Cu	-1.995454000000	0.058043000000	0.817297000000
Cu	1.256550000000	-0.129438000000	-1.520715000000
Cu	2.225189000000	2.023127000000	-0.494441000000
Cu	0.000000000000	0.000000000000	2.309851000000
Cu	-0.329078000000	-2.016616000000	-2.128802000000
Cu	-2.225189000000	-2.023127000000	-0.494441000000
Cu	-1.256550000000	0.129438000000	-1.520715000000
Cu	1.995454000000	-0.058043000000	0.817297000000
Cu	0.329078000000	2.016616000000	-2.128802000000
Cu	-1.493610000000	-2.046117000000	1.968780000000
Cu	1.493610000000	2.046117000000	1.968780000000

## C.3 ZPE descomposition

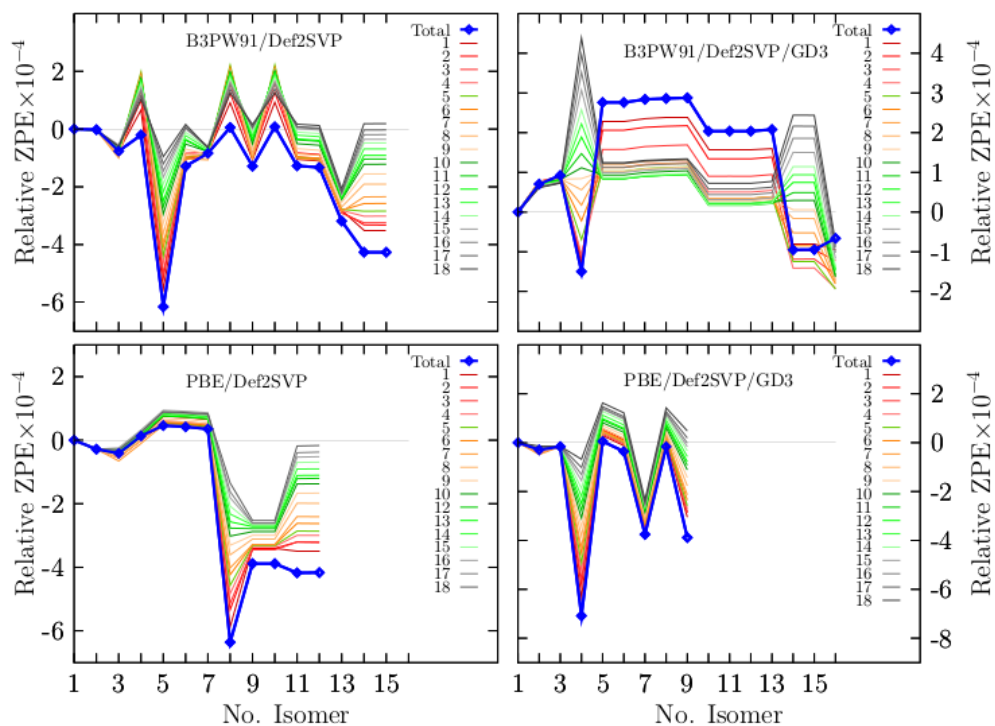


Figure C.2: We show the relative zero-point energy.

## C.4 IR spectra

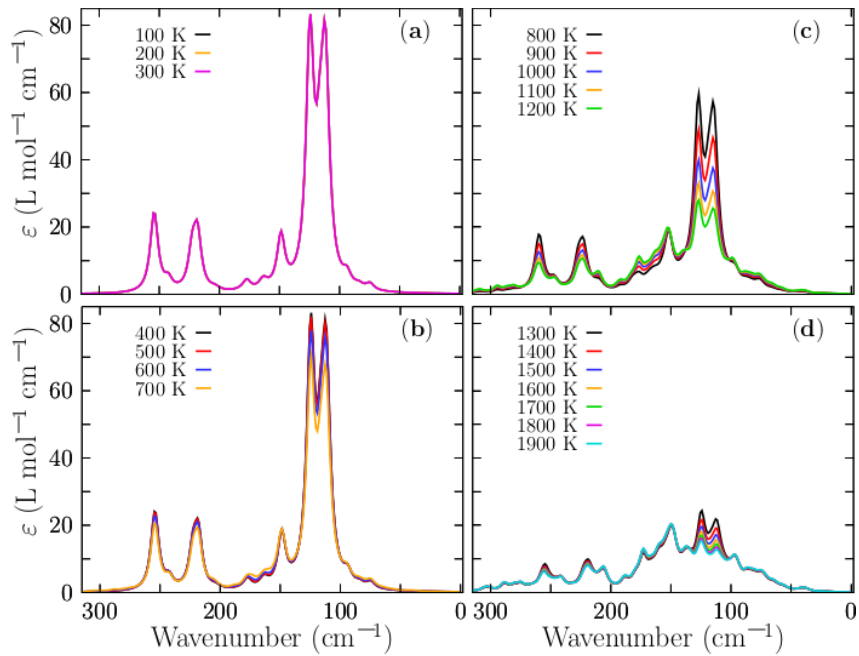


Figure C.3: The IR Boltzmann-spectra-weighted

## C.5 UV-Visible spectra for different temperatures

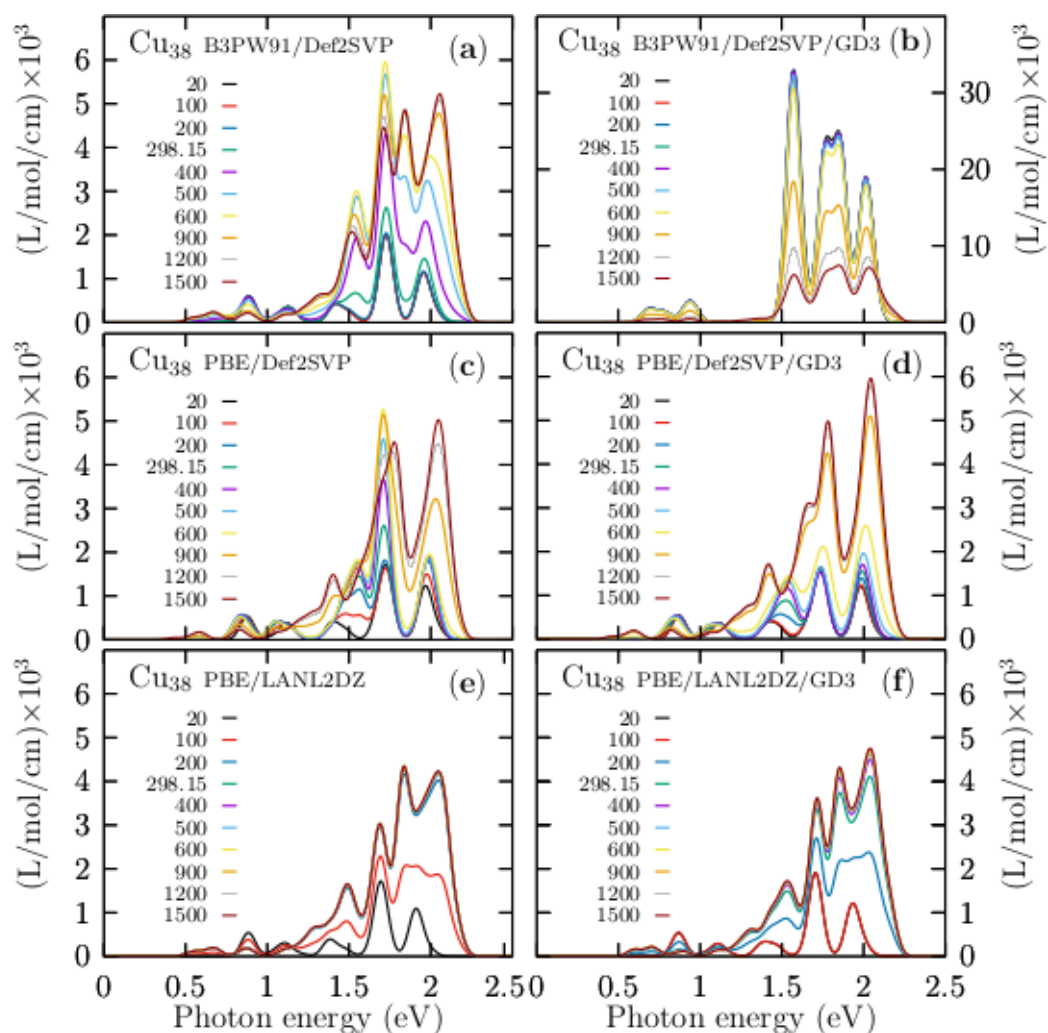
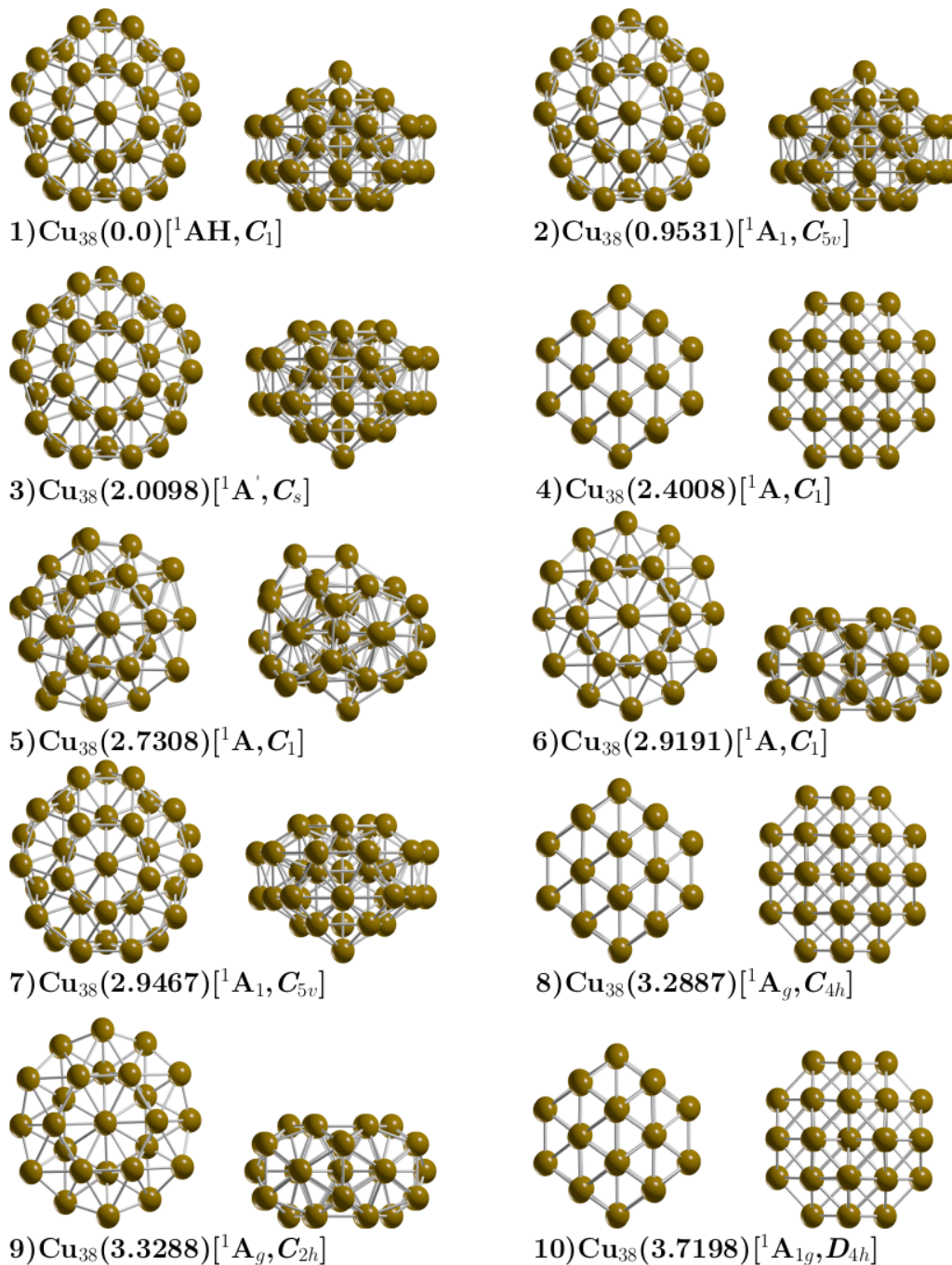


Figure C.4: The UV-visible Boltzmann-spectra-weighted.

## C.6 Geometry at B3PW91/Def2svp level of theory

Figure C.5: Optimized geometries in front and side views of neutral Cu<sub>38</sub> cluster.

# Appx. results

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## List of publications that support this doctoral thesis

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List of publications that support the thesis, including publications in journals, and international and national congresses.

1. Materials 2021, 14(1), 112, *Exploration of Free Energy Surface and Thermal Effects on Relative Population and Infrared Spectrum of the  $Be_6B_{11}^-$  Fluxional Cluster*
2. Molecules 2021, 26(13), 3953, *Theoretical Prediction of Structures, Vibrational Circular Dichroism, and Infrared Spectra of Chiral  $Be_4B_8$  Cluster at Different Temperatures*
3. Molecules 2021, 26(18), 5710, *Effects of Temperature on Enantiomerization Energy and Distribution of Isomers in the Chiral  $Cu_{13}$  Cluster*
4. Front. Chem., 01 March 2022 Sec. *Theoretical and Computational Chemistry, Relative Populations and IR Spectra of  $Cu_{38}$  Cluster at Finite Temperature Based on DFT and Statistical Thermodynamics*
5. Book chapter, *Boltzmann Populations of the Fluxional  $Be_6B_{11}^-$  and Chiral  $Be_4B_8$  Clusters at Finite Temperatures Computed by DFT and Statistical Thermodynamics*
6. Poster presentation. LatinXchem 2021 (A.0.1)
7. Poster presentation. LatinXchem 2021 (A.0.2)
8. Poster presentation. At the *XXX International Materials Research Congress 2022*
9. Poster presentation RMFQT. *Exploration of free energy surface and thermal effects of  $Be_6B_{11}$  fluxional cluster* on November 2020.
10. Poster presentation RMFQT. In the *GALGOSON hybrid-algorithm in quest of the lowest energy structure* on November 2020.



11. Poster presentation RMFQT. In the *Relative abundances of the chiral  $Cu_{13}$  cluster at finite temperature* RMFQT on November 2020.
  12. Poster presentation. In the XIV Coloquio bienal de ciencias de materiales 2021
    - Google scholar, Emiliano Buelna-García
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